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OPTIMIZATION OF MULTI-ELEMENT AIRFOILS

K.P. Misegades

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20. Abstract A review of techniques aimed at maximizing C_L/C_D and C_L for multi-element airfoils showed the need for more exhaustive testing of possible configurations of flap deflection, slot geometry and airfoil angle of attack. For a typical 4-element airfoil, the number of possible configurations can easily be in the billions. A new technique, based on evolution strategy, has been developed for the problem of optimizing a multi-element airfoil with respect to its envelope of maximum C_L/C_D versus C_L . This technique was applied to an airfoil having a slotted leading edge flap and a double-slotted trailing edge flap using an existing computer program for 2D subsonic multi-element airfoils to provide values of aerodynamic coefficients. Although limitations of the program precluded the full determination of the envelope of C_L/C_D vs C_L , the problem of maximizing C_L/C_D for a minimum C_L constraint was solved. The result of testing approximately 400 configurations generated by the random mutation-natural selection procedure of evolution strategy was an 8-fold increase in C_L/C_D with a 12 % increase in C_L .		


Continued..

→ over the initial geometry. (The conclusions reached from this work are 1) evolution strategy applied to the optimization of multi-element airfoils can yield substantial improvements in aerodynamic performance, 2) the number of configurations required to find the optimum can be reduced from the total number possible to a small fraction of the total with the same final result, 3) the inherent simplicity and speed of the technique developed lends itself well to further application in wind tunnels, 4) evolution theory appears to be the best choice for techniques aimed at the optimization of systems defined by a large number of degrees of freedom.

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This report has been reviewed by the EOARD Information Office and is releasable to the National Technical Information Service (NTIS). At NTIS it will be releasable to the general public, including foreign nations.

This technical report has been reviewed and is approved for publication.


JOHN W. BAILEY
Major, USAF
Chief, Electronics

FOR THE COMMANDER


GORDON L. HERMANN
Lt Colonel, USAF
Deputy Commander

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Finally, the author would like to acknowledge the sponsorship of Detachment 1, Air Force Office of Scientific Research (EOARD/AFSC), USAF.

"But it can't fly, Newtons laws prove it !"

Th. von Karman, early 1900's

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1 INTRODUCTION

1.1 Multi-Element Airfoil Optimization

It is no secret today that competition among civilian and military aircraft manufacturers in the international marketplace is tough. This competition has demanded improved flight efficiency, and as a result a strong emphasis has been placed on design optimization with respect to take-off, cruise, and landing aerodynamic characteristics. Design considerations for take-off and landing aerodynamics are primarily directed towards the reduction of wing area, increase in maximum take-off weight, improved fuel efficiency, reduced field length requirements and lowered ground noise levels. The relative importance of the nondimensional coefficients of lift and drag, C_l and C_d respectively, for take-off and landing are shown in figure (1)¹.

Over the entire regime of flight, the performance at take-off, when aircraft weight and engine noise are at a maximum for the flight, is the most critical factor in the design of lifting surfaces. To achieve the maximum rate of angle of climb, thus reducing runway requirements and noise footprint, maximum C_l/C_d is desired for a given C_l . The envelope of values of maximum C_l/C_d versus C_l for the Boeing 727 wing, obtained from flight measurements, is given in figure (2), and is more or less similar to the envelope obtained for all other airfoils².

The complexity of multi-element airfoils, as seen in figure (2) and in more detail in figure (3A), has been dictated by the need for a smooth, and for high-speed transport aircraft shock-free airflow at cruise conditions, combined with the high-lift configurations required at take-off and landing^{2,3}. Although significant effort has been devoted to the study of advanced high-lift devices such as those employing blown flaps, jet flaps, boundary layer control or augmentor wings, it is reasonable to expect the continued use of mechanical devices for the next generation of civilian and military aircraft. Indeed, as shown in figure (4), values of $C_{l_{max}}$ for large, high-subsonic aircraft nearly doubled between 1950 and 1970 as a result of improved design of mechanical flap systems⁴. Once the choice of high-lift system and associated flap and airfoil geometries has been made, the relative positioning of the elements must be determined such that the obtainable values of C_l and C_l/C_d are sufficient to meet performance demands (or preflight promises!). The ideal set of configurations would be those that would result in the largest C_l/C_d -vs- C_l envelope. The number of all possible

configurations, however, is very large even for the typical case of an airfoil having a double-slotted trailing edge flap and a slotted leading edge flap, as depicted in figure (3B).

1.2 Empirical Methods

The most common means of determining the best airfoil-flap configurations involves many hours of wind tunnel testing for a representative set of variations of slot gap width and overlap, flap deflection and angle of attack. Optimum configurations are then made by adding to the main airfoil the leading and trailing edge devices, whose individual slot geometries have been optimized with respect to only one adjacent element. An example of this empirical method, reproduced from the work of Ljungstrom⁵, appears in figure (5). Although this empirical method can greatly improve the aerodynamic performance of a multi-element airfoil, there are two significant disadvantages that must be considered. First, the accuracy of an empirical method is dependent on a large number of test configurations; however, for even the most well-funded design relatively few different configurations are actually tested. For instance, for a 4-element airfoil, 500 test cases is only $5 \cdot 10^{-6}$ % of the number of possible cases, if each of the 10 degrees of freedom can be varied across 10 increments. Increasing the number of test cases comes at the expense of time and direct operating cost of wind tunnels. If wind tunnel time and cost trends increase at the rate depicted in figure (6), however, it is doubtful that empirical methods will produce better results than at the present time, when a great emphasis is being placed on improving high-lift device performance⁶. The second disadvantage of empirical methods is that by combining elements optimized with respect to only adjacent elements, the important viscous interaction between all elements is unaccounted for. This interaction, however, is strong and tests have shown that the combination of individually-optimized components rarely results in an optimum overall configuration⁵.

1.3 Self-Optimizing Airfoils

It would be desirable then to have a self-optimizing scheme, where the system seeks its own best configuration without the need for testing every possibility. Far from speculative, such schemes have been used with a good deal of success in several different problems where systems are described by several degrees of freedom and relative 'factors of fitness' result for each variation of parameters. One such application described by Levinsky⁷ attempted to

maximize C_l for a fixed maximum C_d and minimize C_d for a fixed minimum C_l . For a flexible 2-dimensional airfoil mounted in a transonic intermittent wind tunnel. Results of this work, and results of further investigation of a 3-dimensional flexible airfoil⁸ in a transonic continuous wind tunnel are given in figures (7) and (8). In both cases, the hydraulically-actuated leading and trailing edges were modified automatically by on-line computers programmed with a gradient-strategy optimization scheme. This is described in section 2. The only human input was the factor of fitness to be maximized or minimized (C_l , C_d , or volume) and a constraint. Gradient strategy has also been used in the work of Hicks⁹, where 2-dimensional transonic airfoils were modified to improve C_l , C_d or maximize volume. Some of the more significant results of this work, performed numerically as opposed to the above mentioned wind tunnel work, are shown in figure (9). Although these examples have resulted in substantial improvements in airfoil performance, the application of their optimization methodology was found to be more cumbersome than the method described in this work. Existing optimization methods are compared below to a new scheme based on 'evolution strategy'. This scheme has been developed to determine the configurations of a 4-element airfoil giving maximum C_l/C_d for each value of C_l , where only the geometry of each element is known initially.

2 THEORY

2.1 Simple Optimization Problem-Existing Solution Methods

Consider the optimization problem faced by an experimentalist standing above a room in which there is a single geographical peak whose location with respect to a 2-dimensional coordinate system is to be determined. In this problem, the 'system', this being the human, has two degrees of freedom, his location with respect to the x-axis and the y-axis. At each x,y coordinate position, the value is determined of the geographical 'fitness factor', or the distance between the x-y plane and the surface below. The most rudimentary method to find the peak would be to make a number of random soundings in order to obtain a rough impression of the surface. In order to improve accuracy, the grid could be divided into a fine mesh and the height is then recorded at each mesh point. Although this scheme guarantees that all possible x,y combinations have been checked, the number of possible combinations increases with the square of the number of grid divisions and with a power equal to the number of degrees of freedom for higher order systems. Figure (10) depicts these 2 basic schemes along with two gradient-based strategies that were developed to converge to the peak with a reduced amount of effort¹⁰.

In the first of these two gradient-based strategies, known as the Gauss-Seidel Strategy, the experimentalist, trying to find the peak with the least amount of effort, simply proceeds in the direction of the steepest positive gradient, determined at the starting point, until the gradient becomes zero or negative. From this point, he turns in the direction of a new, locally-steepest gradient and continues in this new direction. This procedure is continued until the peak is found, that is, a position has been reached on the x-y plane where no positive gradients exist below. The second of these techniques, known as the 'general gradient strategy', is similar to the first except that at each step the magnitude of gradients in all directions is re-evaluated. Although the second scheme may result in the shorter total distance between the starting point and the peak with respect to the first scheme, it requires more work per step. Clearly, the use of either of the gradient strategies represents a substantial improvement over the inspection of every possible combination of the variable parameters. It is noted that in order to reduce the amount of effort involved in scheme B of figure (10), one is tempted to increase the grid spacing. The

danger of this, of course, is that there is a strong possibility that the peak will be completely missed; this is precisely the point mentioned previously related to optimizing airfoils by empirical methods. The danger of using gradient strategies in more complicated systems is that only a relative optimum may be reached, as the smaller of two peaks for the simple problem just described.

2.2 Simple Optimization Problem-Evolution Strategy Solution

A fifth, and relatively new optimization scheme that may further reduce the effort required to improve a system described by a number of degrees of freedom is based on 'evolution strategy'. 'Relatively' new is stressed, because the basis of this strategy is derived from the theories of natural selection first postulated by the 19th century biologist, Charles Darwin. As in biological systems, which in their simplest classifications can be grouped according to a number of parameters, such as size, number of appendages, means of reproduction or mobility, an engineering system survives if the combination of each of its defining parameters results in a 'beast' that is superior to all other combinations. Only recently has this concept been applied to realistic physical problems, the majority of the work to date being attributed to Professor Ingo Rechenberg, of the Technischen Universitat Berlin. In order to describe this scheme, we consider again the task of the experimentalist. Using evolution strategy, as depicted in figure (11A), a number of test points are selected randomly over a region near the starting point. The height is recorded at each point, then the experimentalist moves to the highest of these points. From there, the same number of new points are randomly chosen, and the procedure continues as before.

The distance from one 'high point' to each new point in a successive set is controlled by the previous distance, that is if a large step resulted in a larger height than a smaller step, all new points would be determined using steps approximately equal to the large step. This important factor of evolution strategy allows large steps to be taken early in the optimization process, and decreasing step size as the optimum position is approached. The inclusion of large mutation steps also prevents the convergence to local maxima, a problem associated with gradient strategies. In the case of a local maxima or small barrier in the optimization process, evolution strategy will jump ahead as the result of a large

mutation length.

2.3 Evolution Strategy Examples

Several examples of evolution strategy application are shown in figures (11) and (12)^{10,11}. As a simple verification test, figure (11B) depicts a segmented plate having 5 degrees of freedom that is mounted in a wind tunnel. The objective is to reduce the overall drag of the plate as measured by the momentum defect between the leading and the trailing edges. From the initial configuration, several new configurations, or cases, were created by random modifications of the angle of each segment with respect to an adjacent segment. After 140 cases, the segmented plate became nearly planar, the expected result. The important result is that 140 cases represents only $4.06 \cdot 10^{-5}\%$ of the total possible, 345 million.

The second example is an attempt to modify a system whose optimum configuration is unknown¹¹. In this case, shown in figure (12A), the objective was to maximize the efficiency of a two-phase supersonic nozzle constructed from a number of discs. The optimal configuration is radically different from conventional designs and verifies the ability of evolution strategy to converge to unknown solutions. It is also interesting to note that flow mixing regions seen in the figure have been previously suggested for improving nozzle efficiency.

The third example, that of reducing the head loss for a 90° bend of flexible tubing, also has an unpredictable result. As depicted in figure (12B) the final shape is a subtle change from the initial, a standard circular arc, but the result of 300 mutations is a halving of the head loss¹¹.

2.4 Selection of Optimization Method

The advantages of using evolution strategy over an exhaustive evaluation of every possible configuration are clear, except perhaps for the case of a system having only one degree of freedom. The advantages of evolution strategy over a 'strictly determined mathematical strategy', such as gradient methods, have been summarized by Rechenberg¹⁰:

1 When a large number of parameters are involved, the evolution strategy attains the desired result more rapidly than the more familiar strictly determined search strategies, assuming the size of the search steps to be the same in both cases. So far, this could only be proved for the case of an n-dimensional hyperplane rising in any arbitrary direction. A more general proof is being attempted.

2 Whereas the mathematical search strategies used so far

require very small steps (in the sense of the truncation of the Taylor series after the first term), the evolution method can and should operate also with much larger steps which exceed the linear region in the neighborhood. Taking larger steps signifies

(a) in many situations a more rapid advance towards the desired aim, and

(b) a shorter time to decide whether the step taken has been successful or not. (The change in the value of a function will generally be greater in the case of a large parameter change than in the case of a small change.)

3 A so-called "steady signal" in the measurement of the value of a function is a mathematical fiction. Disturbances are always present, which give rise to errors in measurement. The effectiveness of the strictly determined mathematical search strategies is markedly reduced by small errors of measurement. It is of the nature of the evolution method (as a stochastic search method) that small random errors of measurement cannot have a decisive influence on the development of the process.

4 There are cases in which the more familiar mathematical search strategies must reach deadlock. Such cases are frequently observed in physics: examples are hysteresis phenomena and locally limited extremal values. The evolution method can generally cope with such situations without difficulty.

5 The algorithm of the evolution strategy is extraordinarily simple. This implies that the effort required for an automatization of the search process is relatively low.

Since the work associated with this report was strictly numerical, as opposed to experimental, the small error effect noted above related to the use of mathematical strategies could not have any significance; thus an argument could still be made in favor of gradient methods. Rechenberg, however, has found that a cross-over point exists at which search effort for improved configurations using evolution strategy is less than the effort required for gradient strategies⁹. This point is for systems having 5 or more degrees of freedom.

The system of interest in the work described here is a 4-element airfoil described by 10 parameters as shown in figure (13). Three pivot points describe the relative position of adjacent elements. The individual geometry of an element is given with respect to a local coordinate system with the origin on its leading edge. Pivot points 1 and 2 are fixed with respect to element 2 and are variable with respect to elements 1 and 3. Likewise, pivot point 3 is fixed with respect to element 3 and variable with respect to element 4. The two degrees of freedom for each of the pivot points plus the relative deflection between adjacent elements define 9 degrees of freedom. The 10th degree of freedom is the angle of

attack between the main airfoil and the freestream velocity vector.

As previously stated, the objective of this optimization is to obtain the best envelope of C_l/C_d -vs- C_l values. The fitness factor for this system is the magnitude of C_l/C_d for each value of C_l , which is equivalent to minimizing C_d for fixed C_l . This implies a series of individual optimizations over all desired values of C_l . The flexible nature of evolution strategy allows a two-step procedure, however. First C_l/C_d is maximized while maintaining C_l above the initial value; the limit of this maximization is a point on the envelope. The second step is then to move along this envelope with moderate mutation lengths, selecting those configurations having the best combination of C_l/C_d and C_l . It is because of this flexibility coupled with the abovementioned aspects of evolution strategy that this method was chosen over gradient strategies as a basis for multi-element airfoil optimization.

3 CALCULATION OF AERODYNAMIC COEFFICIENTS

3.1 Description of Program Theory and Use

Aerodynamic Coefficients are calculated by the program detailed in reference 13. This program is composed of the following task areas:

- A. Potential Flow Solution
- B. Ordinary Boundary Layer Solution
- C. Confluent Boundary Layer Solution
- D. Slot-Flow Analysis
- E. Combined Solution

The inviscid, potential flow solution makes use of the distributed vortex concept with the vortex singularity comprising the fundamental solution to the Laplace equation. Airfoils, arbitrarily arranged and composed of from one to four elements, have surfaces approximated by a closed polygon whose linear segments are represented by distributed singularities. Airfoil contours are limited to smooth, regular shapes with sharp or pointed trailing edges. The only restriction on the slot formed by two adjacent elements is that the magnitude of flap overlap must be greater than about 1% of the airfoil chord.

The ordinary boundary layer solution is comprised of mathematical models for laminar, transition, and turbulent boundary layers in subsonic flow. The laminar boundary layer model is based on the basic approach of Cohen and Reshotko modified to suit the needs of the program. Laminar stall criterion developed by the author of the program predicts the formation of short or long separation bubbles or bubble burst, a flow condition which causes the termination of further program execution. The transition model, evolving from the instability criteria of Schlichting and Ulrich, establishes limiting conditions for defining the position of transition on the airfoil. Two separate mathematical models for ordinary turbulent boundary layer development are used. The first, an approximate model developed by Goradia, is used in the initial iterative calculations. The second and more accurate model, based on the methods of Nash, determines the turbulent boundary layer in the final, viscous solution.

A significant feature of the program is the inclusion of a confluent boundary layer model that reflects the merging of an upper surface boundary layer with slot efflux. This model, developed from the experimental and analytical work of Goradia, accounts for the

highly complex viscous phenomena associated with slotted airfoils. Associated with the confluent boundary layer, a slot-flow model is defined for flow between slot regions.

The final viscous solution uses an iterative technique to combine the inviscid solution with the boundary layer calculations. The geometry of the 'equivalent airfoil', reflecting local boundary layer thicknesses, is successively defined over a variable number of iterations until pressure distributions have converged to a steady condition. As the work described in this report was more of a qualitative nature than quantitative, only one iteration between viscous and inviscid calculations is made, in the interest of reduced computation time. A comparison of predicted and experimental pressure coefficients using the program for a two-element airfoil appears in figure (15). A listing and description of program input is given in appendix (i) for the 4-element airfoil considered in this work.

4 OPTIMIZATION PROCEDURE

4.1 Geometry Modifications

The choice of evolution strategy required the preliminary development of the following:

- A. Scheme for Random Geometry Modifications
- B. Mutation Length Control
- C. Criterion for Convergence to Optimum
- D. Initial Airfoil Geometry

Of fundamental importance to the effectiveness of evolution strategy is the combination of large and small mutation lengths. If only small sizes are used, the number of improved cases will be high, but the rate of progress will be slow. On the other hand, if only large sizes are used, the optimum may be entirely skipped over. For this reason, new cases were divided into 3 groups, one having all mutation lengths of a base value, the second group having lengths of 50% of the base value, and the third group having lengths 150% of the base. The control of the value of this base mutation length will be described below. For each new geometry, then, 18 new configurations are generated, divided into 3 groups of 6 cases each. The choice of 18 cases per set was somewhat arbitrary, but it was felt that this would be a good trade-off between effort and resulting improvement. As the optimization procedure was carried out, it was found that 18 cases was a safe choice, as the program used to determine C_l and C_d had certain limitations. In experiment, a smaller number of cases per set might be desirable.

All mutations were generated by a computer program, whose listing appears in appendix (ii) and is described by its logic diagram in figure (16A). The random choice required by this program is made using a random number generator that determines for each case which of the 10 parameters is to be modified, and in the event of a modification, whether the increment is positive or negative. As seen in figure (16C), two columns of mutation lengths are printed. The first gives the three lengths used to modify the x,y position of pivot points. These values represent a percentage of the range defined for each pivot point, as shown in figure (16B). The second column is degrees of mutation for flap deflection and angle of attack.

The Random number generator is a computer system function that returns an even distribution of real values in the range 0.0-1.0. A description of its algorithm is given in appendix (iii).

4.2 Mutation Length Control

As described above, three modification lengths are used for each new set of configurations. The control of the base, or middle length is critical, as rapid convergence to an optimum requires an expansion of mutation size far from the optimum and a compression close to it. In this optimization problem, the base length for a new set was controlled by the best case from the previous set. For instance, if case 1, a member of the third mutation length group, is the best in its set, its mutation length will be used as the base value for the next set. In this way, increasing lengths will be favored. On the other hand, if case 3 is the most improved, smaller lengths will be favored in the next set. Using this scheme, the optimization strategy self-adjusts to the distance from convergence.

4.3 Convergence Criterion

Concerning the question as to when convergence has been reached, a criterion is used that recognizes that mutation lengths will automatically compress as the point of convergence is approached. When the modification of an improved configuration fails to increase C_l/C_d for a minimum C_l , the airfoil has 'approximately converged'. For absolute convergence, an additional set of configurations is generated, based on the best case of the set that failed to improve over the point of approximate convergence. If again there is no improvement, convergence is said to exist.

The procedure proposed to determine the envelope of aerodynamic coefficients is comprised of the following two basic steps:

1. Maximize C_l/C_d while maintaining C_l greater than $C_{l_{min}}$, the value obtained from the initial geometry
2. Move across the envelope from the maxima point found from step 1 to the maximum C_l limit, when flow separation occurs

Results from this procedure are presented in section 5.

4.4 Initial Airfoil Geometry

The initial airfoil configuration was an arbitrary but realistic placement of elements so as to guarantee good flow conditions through the slots. The value of the 10th parameter, angle of attack, was determined from the polar shown in figure (14). An angle of 0.5° was used as it resulted in the maximum C_l/C_d . This initial configuration and angle of attack thus set the value of $C_{l_{min}}$ at 2.1. In all subsequent program calculations, mach number and Reynolds number, referenced to an airfoil chord of 350mm, were 0.125 and $1.26 \cdot 10^6$, respectively. Element profiles were

taken from reference 14, with appropriate modification to meet the requirement of smooth contours.

5 RESULTS

5.1 First Three Configuration Sets

The first step of the optimization procedure, the maximization of C_l/C_d with the constraint of C_{lmin} , was started at the initial geometry. Figure (17) shows the scatter of data points for the first three sets (54 cases) of airfoil configurations. Some points have been omitted for clarity. Circled data points are best cases for each set; these cases serve as the bases for subsequent modifications. The automatic mutation length control reacts well in these first sets, far from the point of convergence, with an increase in base lengths between sets one and two and a constant base length between sets two and three. As expected, points scattered in the immediate vicinity of the initializing case were from the first mutation length group, and points scattered further away were from the second and third groups. As seen in figure (17), the ratio C_l/C_d appears more sensitive to airfoil modification than C_l . This effect continued for all other sets, with most points located in a narrow C_l band between 2.0 and 3.0 and a scatter of other points in a relatively low C_l/C_d - low C_l region. The tabulation of all configurations (37 sets, 656 cases) is given in Appendix (iv) together with initial and final configuration data.

5.2 Description of Complete Optimization

Figure (18) shows the result of continued maximization of C_l/C_d , plotting the best case for each of 37 sets. Up to set 11, mutation lengths generally expanded or remained constant. Sets 12-14, however, resulted in a compression of lengths, and convergence was thought to be imminent. Beyond set 14, lengths began to expand again until the base value stabilized at approximately 2% and 1° for pivot point location and deflection angles, respectively. This effect was considered to be a 'small barrier' in the optimization process, which the evolution strategy was able to step over with the larger of the three mutation lengths. A gradient strategy-based technique would have converged to such a barrier, or local maximum.

Beyond set 22, the accuracy of the aerodynamic coefficients became questionable, resulting in erratic behavior of the optimization process. When the process was continued without the C_{lmin} constraint, large changes in C_l/C_d and C_l occurred for relatively small geometry modifications. As an attempt to return to smaller variations of coefficients, the process was restarted at set 24

with a forced reduction of step sizes, as shown by the dotted lines of figure (18). This resulted in sets 27 and 28 which again were characterized by large variations of coefficients for small modifications. This sequence of forced length compression and optimization restart was continued to the 37th, but by this point values of C_l/C_d were unrealistically high, even for the simplified two-dimensional airfoil model without induced drag or body interference effects. Indeed, during the process of optimization, numerous configurations resulted in unsuccessful program termination or extremely high values of C_l/C_d and in several cases, negative C_d ! The reasons for this inaccuracy are thought to be one or a combination of the following:

- 1 Invalid geometry; i.e., overlap less than 1% of chord
- 2 Confluent boundary layer or slot flow model failures for small slot cross-sections
- 3 Inadequate verification of program by authors for 4-element airfoil configurations (note-the frequency and severity of inaccuracies were substantially less for the preliminary optimization of a 2-element airfoil)

In the further presentation of results, sets 21-22 are taken to be the approximate limit of data accuracy, although all points are shown.

C_l/C_d and C_l are shown with respect to set number in figure (19). The points again are from the best cases for each set. As seen in this figure, the result of 22 sets of configurations and 296 total cases, C_l/C_d has been increased from 4.28 to 36.6, a factor of 8.55. At the same time, C_l has been increased from 2.31 to 2.59, a result that evolved by favoring the configuration having the larger C_l when two or more had approximately the same C_l/C_d . Increasing C_l , however, was not the primary objective of the optimization.

Because of the limit of data accuracy, the optimization process was terminated at the 37th set, thus making it impossible to find the envelope of aerodynamic coefficients and thus carry out the second step of the proposed optimization.

5.3 Initial-Final Configuration Comparison

Figure (20) shows polars generated for the initial configuration and the configurations resulting from the process of C_l/C_d maximization. The resulting dramatic improvement in aerodynamic performance is apparent. During the process of optimization, a number of configurations produced values of C_l/C_d and C_l that when plotted fell to the right of the polar for maximized C_l/C_d . A polar

was generated from the point that was furthest to the right and is denoted as the 'optimized C_l configuration'. This configuration, it is interesting to note, was a member of the optimum C_l/C_d set, number 22. The dotted lines have been added to these polars to show the real flow behavior for multi-element airfoils such as shown in figure (2).

A comparison of initial and final configurations is given in figure (21). A noticeable effect of the optimization is the reduction of slot area and improved contour smoothness of the trailing edge flaps. Both of these effects have been shown experimentally to improve aerodynamic performance. The same changes did not occur for the leading edge flap. It was found that the multi-element airfoil program was very sensitive to reduction of slot area of the leading edge device when both trailing edge flaps were present. It is suspected that the reasons for this sensitivity are the same as those mentioned above.

A comparison between the optimum C_l/C_d configuration found using evolution strategy and that suggested by the empirical recommendations of reference 5 was attempted, but the slot geometries required were not capable of being modelled by the airfoil program. Any change from these recommendations so as to suit program input requirements would have resulted in a meaningless comparison.

CONCLUSIONS

Although the inaccuracy of the program used to determine aerodynamic coefficients precluded the full solution of the airfoil performance envelope, the problem of maximizing C_L/C_D was easily handled by the evolution strategy-based optimization technique. A review of existing techniques showed that evolution strategy is the best choice for systems described by 5 or more degrees of freedom, due to its relative incompleteness, flexibility to handle a wide variety of problems, and to the knowledge that the converged solution is an absolute optimum within the range of variation of these degrees of freedom.

The problem experienced with the use of the above-mentioned program reinforces the opinion that as of yet numerical solution methods are severely limited in their range of application to complex engineering systems, such as for a multi-element airfoil with its large number of configurations. The value of numerical methods, however, lies in their ability to provide preliminary results to be used as a starting point for further design refinement in the laboratory. Of course, as long as the limits of numerical methods are not exceeded, experimental optimization may be well predicted.

The next logical step related to the work described here is the application of evolution strategy to optimization in a wind tunnel. A setup is envisioned, similar to those of references 7 and 8, where modifications to the airfoil, analysis of aerodynamic coefficients, and optimization procedure are carried out by on-line computers. The importance of using the wind tunnel is that all configurations of an airfoil are capable of being tested, as opposed to computer model-imposed restrictions such as slot geometry and separation-free flow. An important note is that multi-element airfoils often are designed to perform with separated flow and negative overlap, two conditions that can not exist for the successful use of the program of reference 13.

The effect of increasing C_L/C_D through the modification of slot geometries while at the same time maintaining adequate C_L is best seen for the design trade-off between take-off and cruise flight. Increased C_L/C_D at take-off allows increased rate or angle of climb, decreased overall distance to reach a required screen height, increased take-off weight for the same runway requirement, or a combination of the three. An increase in C_L/C_D at take-off also has a strong influence on cruise flight efficiency through the reduction of the installed power needed for take-off.

By using an evolution-based strategy, the converged optimum is an 'absolute' optimum within the range of variations of the degrees of freedom of a particular system. The question of whether convergence has been obtained or not is thus eliminated; this was not the case for the design of the Boeing 737. This is seen in figure (4) by the 3 increments in $C_{l_{max}}$ for its high-lift devices. At each point, the design was probably considered to be an optimum!

Other areas of aerodynamic design that should lend themselves well to evolution-strategy optimization are the wing-fuselage junction, empennage, supercritical airfoils, engine nacelles, and fuselage rear up-sweep. These design areas are currently approached using procedures similar to those of flap design, the wind tunnel testing of a relatively small number of different configurations. Each of these problems is described by many degrees of freedom, a characteristic that has been shown to be well-suited to evolution strategy. The technique described in this work is by no means restricted to aerodynamic design, however. A wide range of applications can be imagined; the examples included in this report are only a few preliminary cases whose results show promise for this new technique to be used as a powerful tool in the design process.

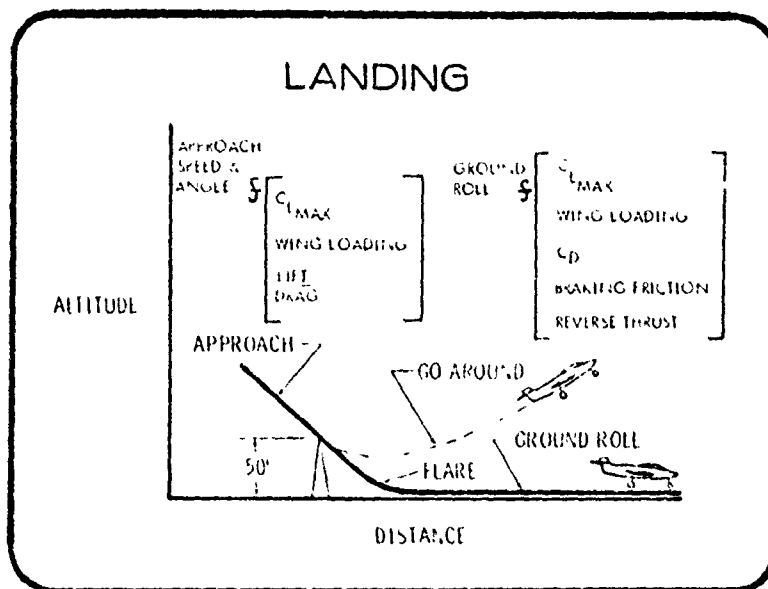
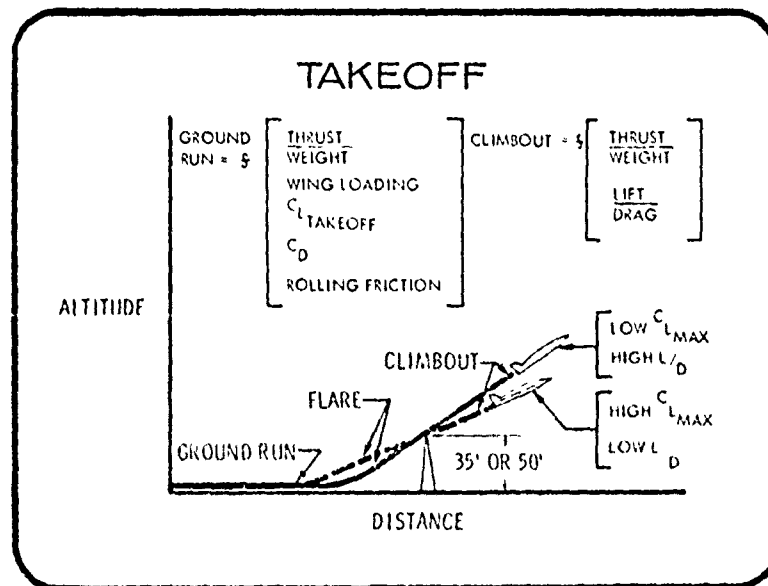
One can consider the development of evolution strategy as a result of man learning from his observations of nature. Figure (22) depicts what might result if nature learns from the aerodynamic achievements of man.

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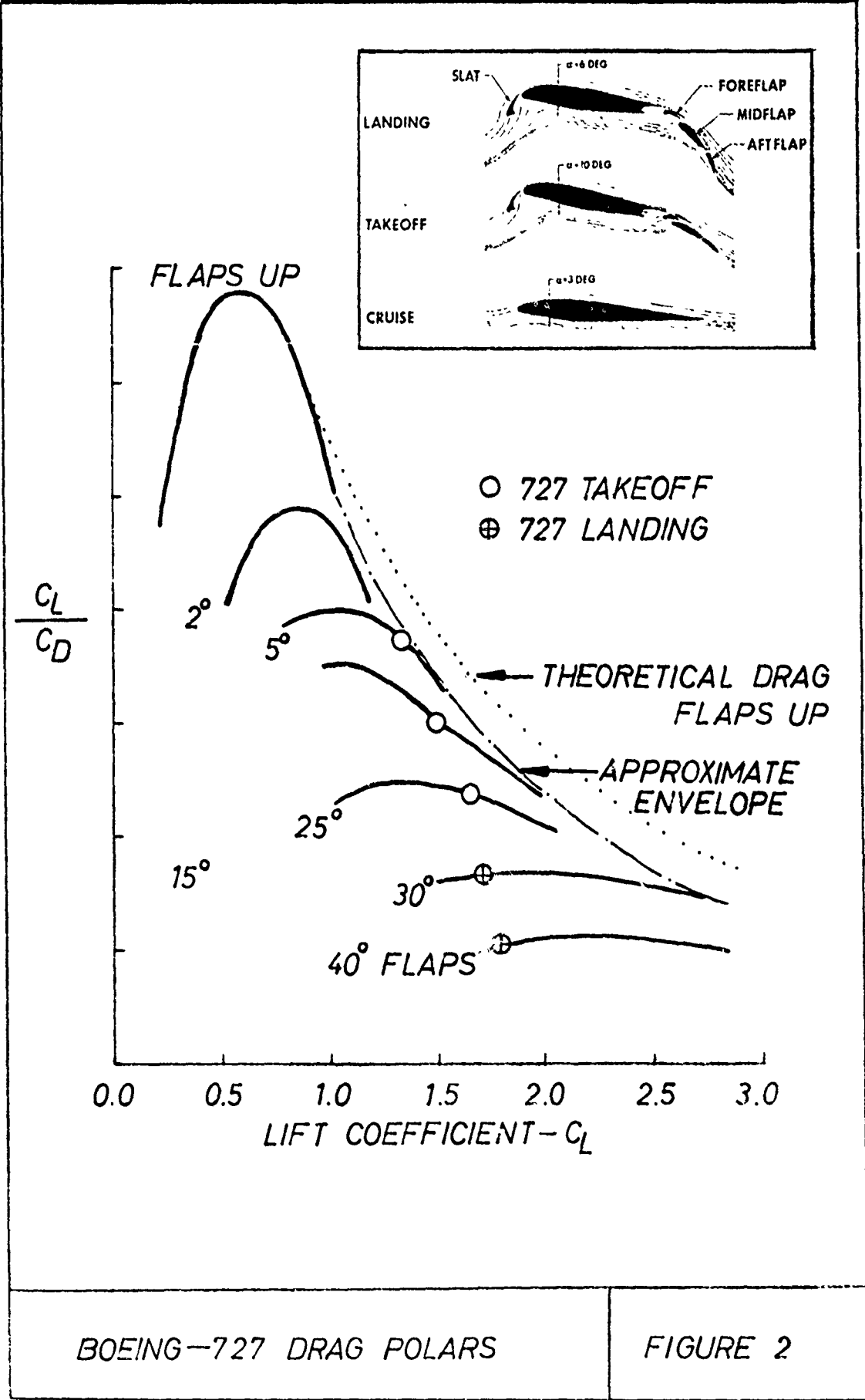
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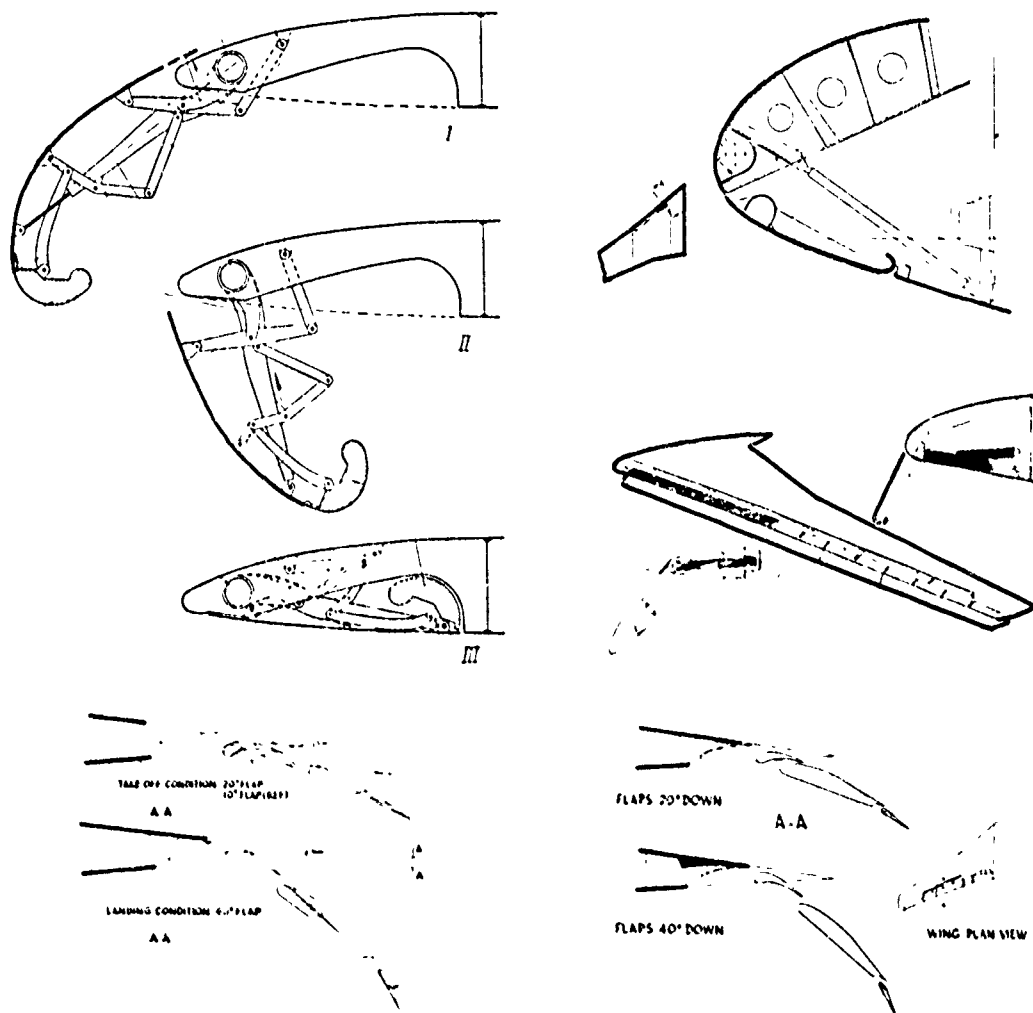
**TAKEOFF AND LANDING
AERODYNAMICS**

FIGURE 1

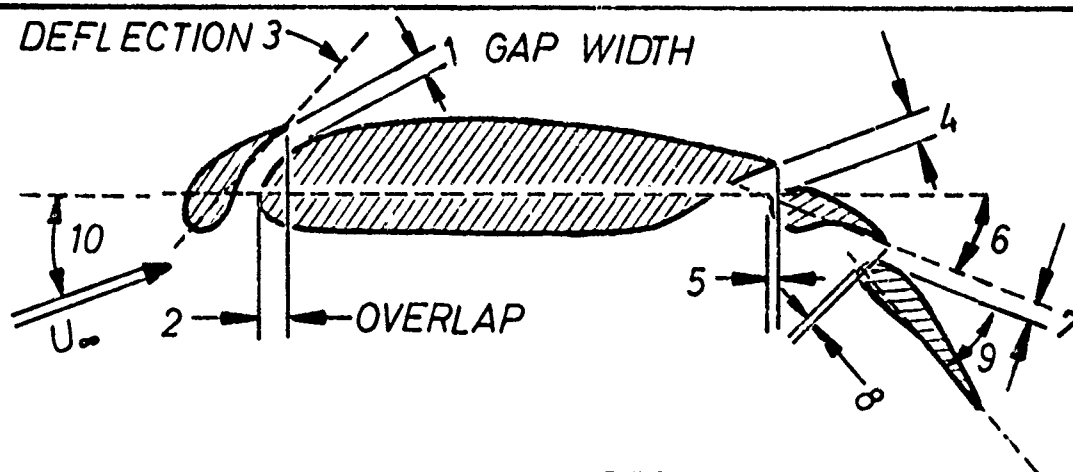


BOEING-727 DRAG POLARS

FIGURE 2



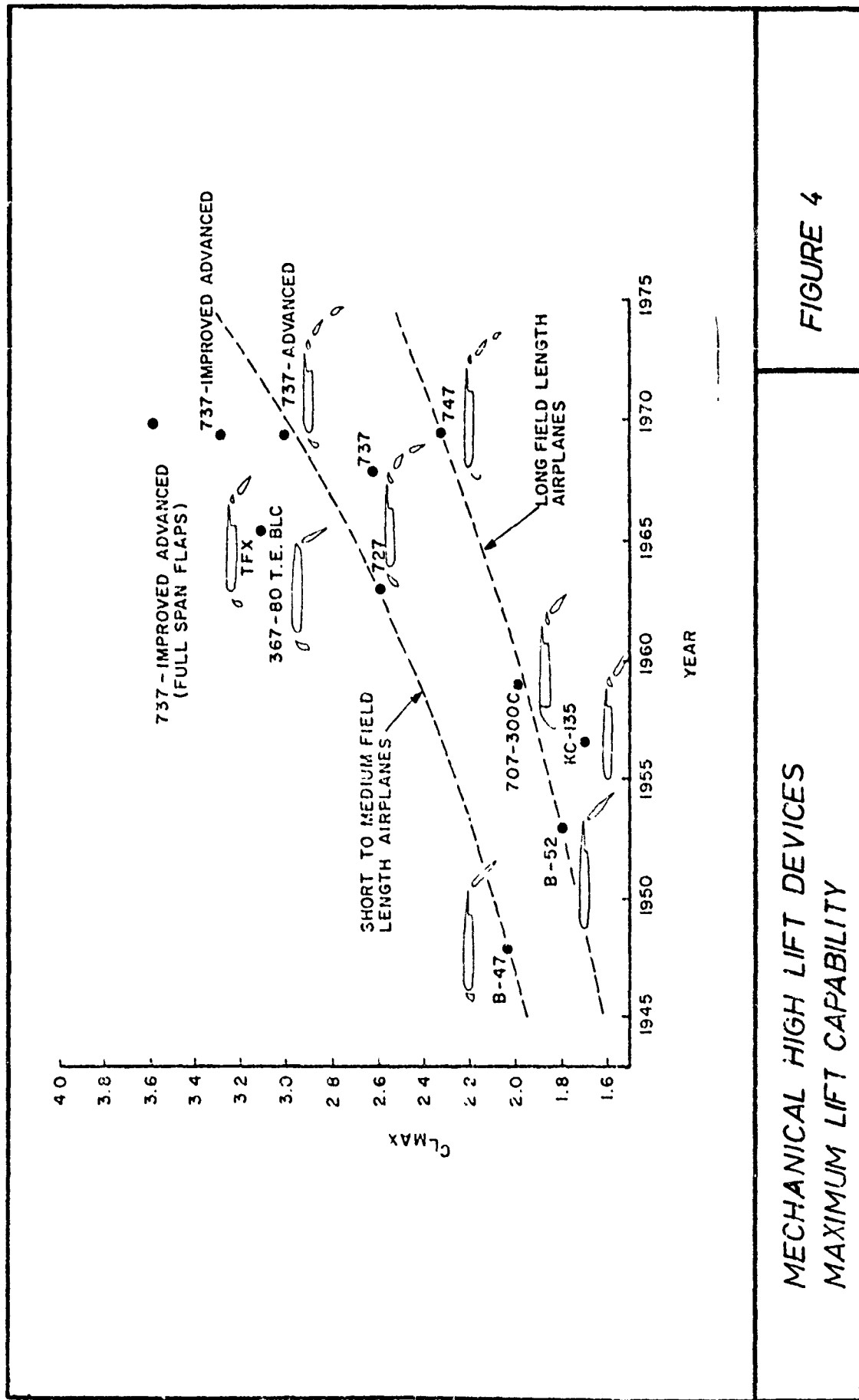
A. HIGH-LIFT DEVICE DETAILS



B. AIRFOIL DEGREES OF FREEDOM

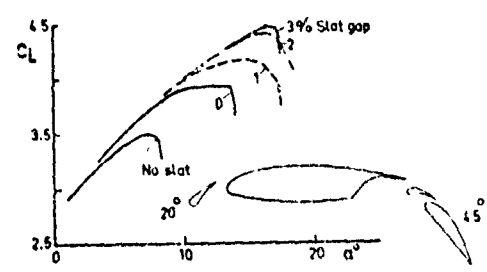
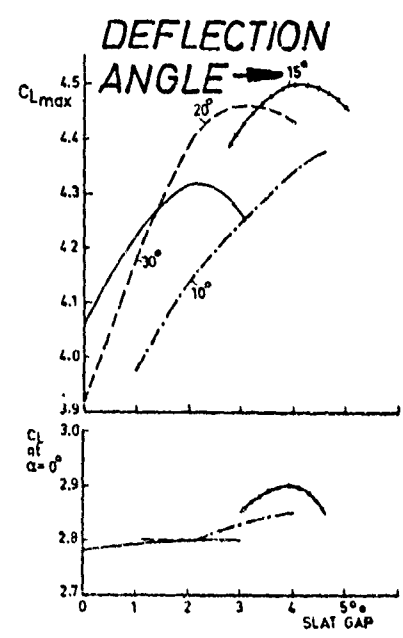
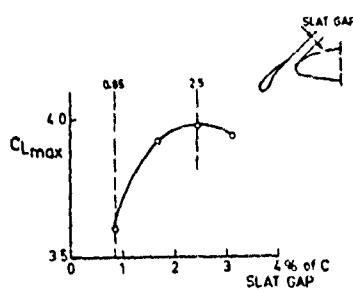
MULTI-ELEMENT AIRFOILS

FIGURE 3

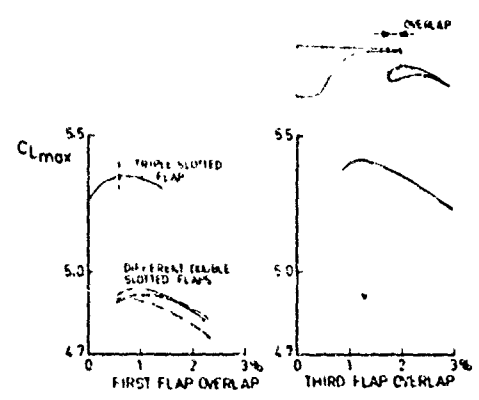
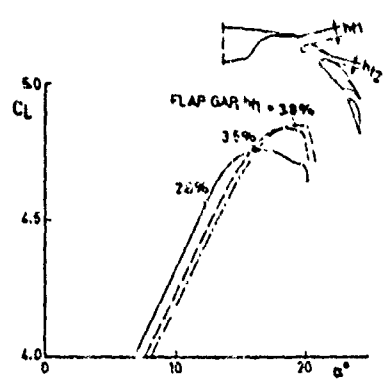


MECHANICAL HIGH LIFT DEVICES
MAXIMUM LIFT CAPABILITY

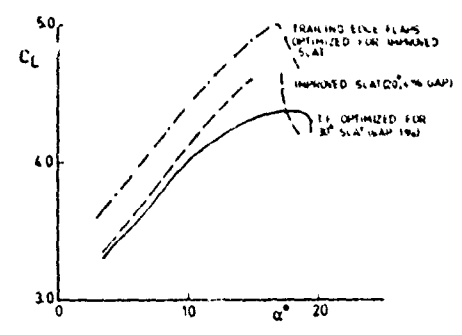
FIGURE 4



L.E. SLAT GAP & DEFLECTION EFFECTS



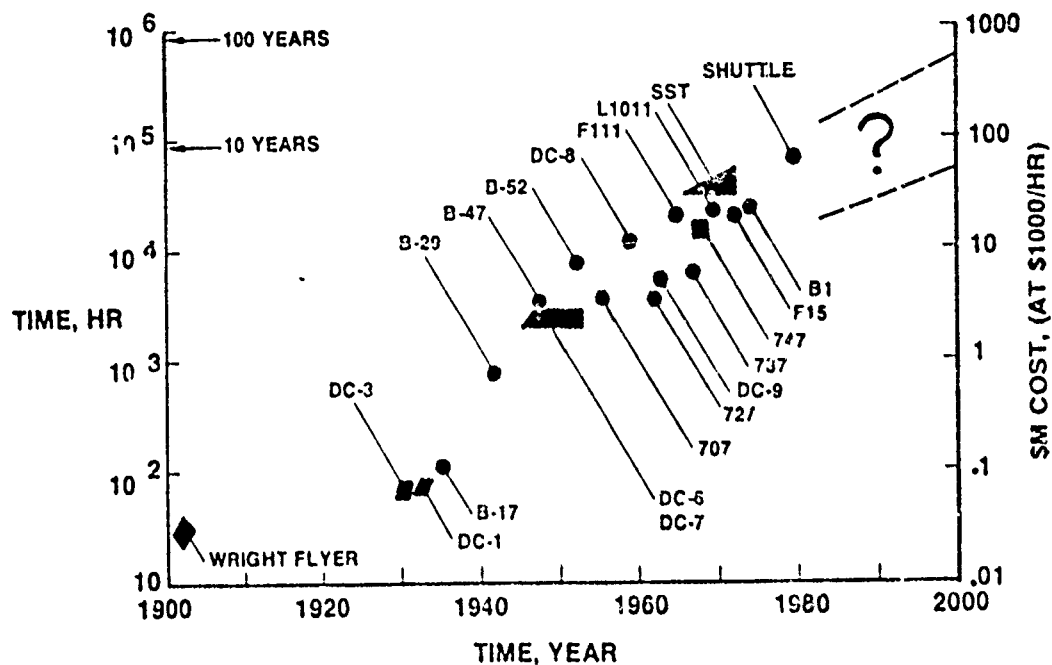
T.E. FLAP GAP & OVERLAP EFFECTS



COMBINED SLAT AND FLAP EFFECTS

FOUR ELEMENT AIRFOIL OPTIMIZATION BY EMPIRICAL METHOD

FIGURE 5

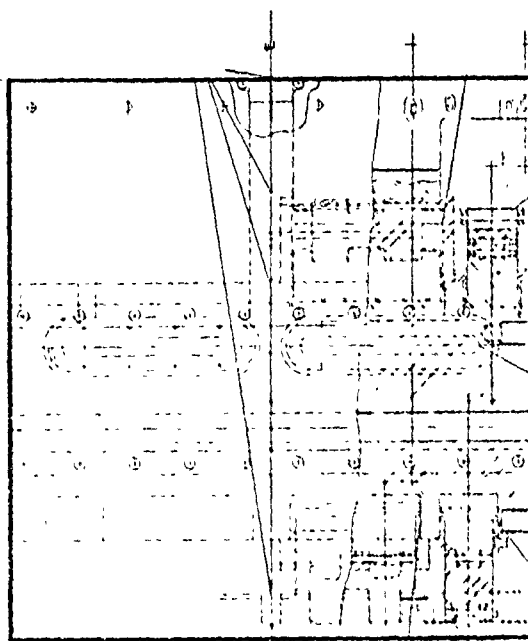
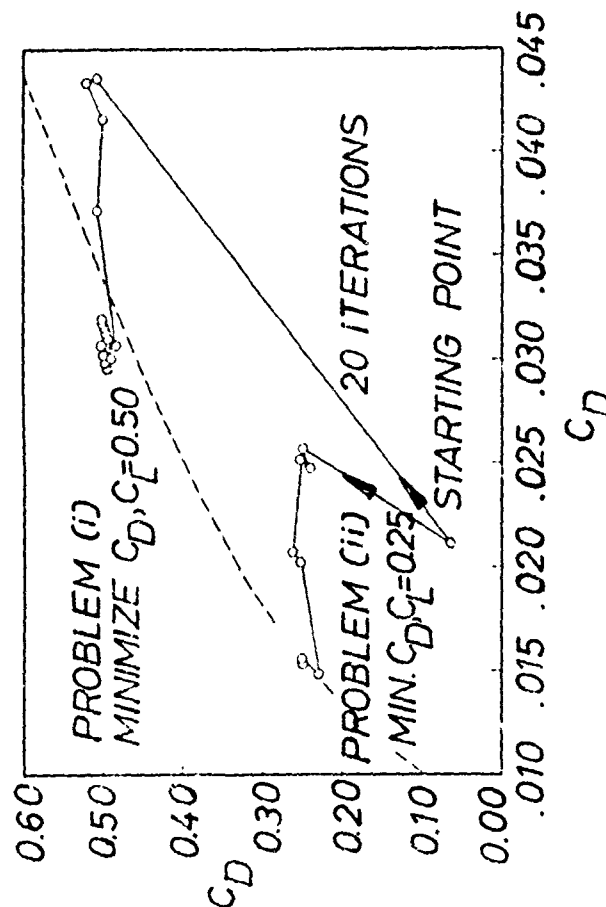


WHAT PRICE ACCURACY ?

- ... 10^{10} CONFIGURATIONS
- ... 1 MEASUREMENT/30 SECONDS
- ... TOTAL TIME $9.51 \cdot 10^5$ YEARS
- ... TOTAL COST $\$ 8.33 \cdot 10^{10}$

WIND TUNNEL TEST PROGRAM
TRENDS

FIGURE 6

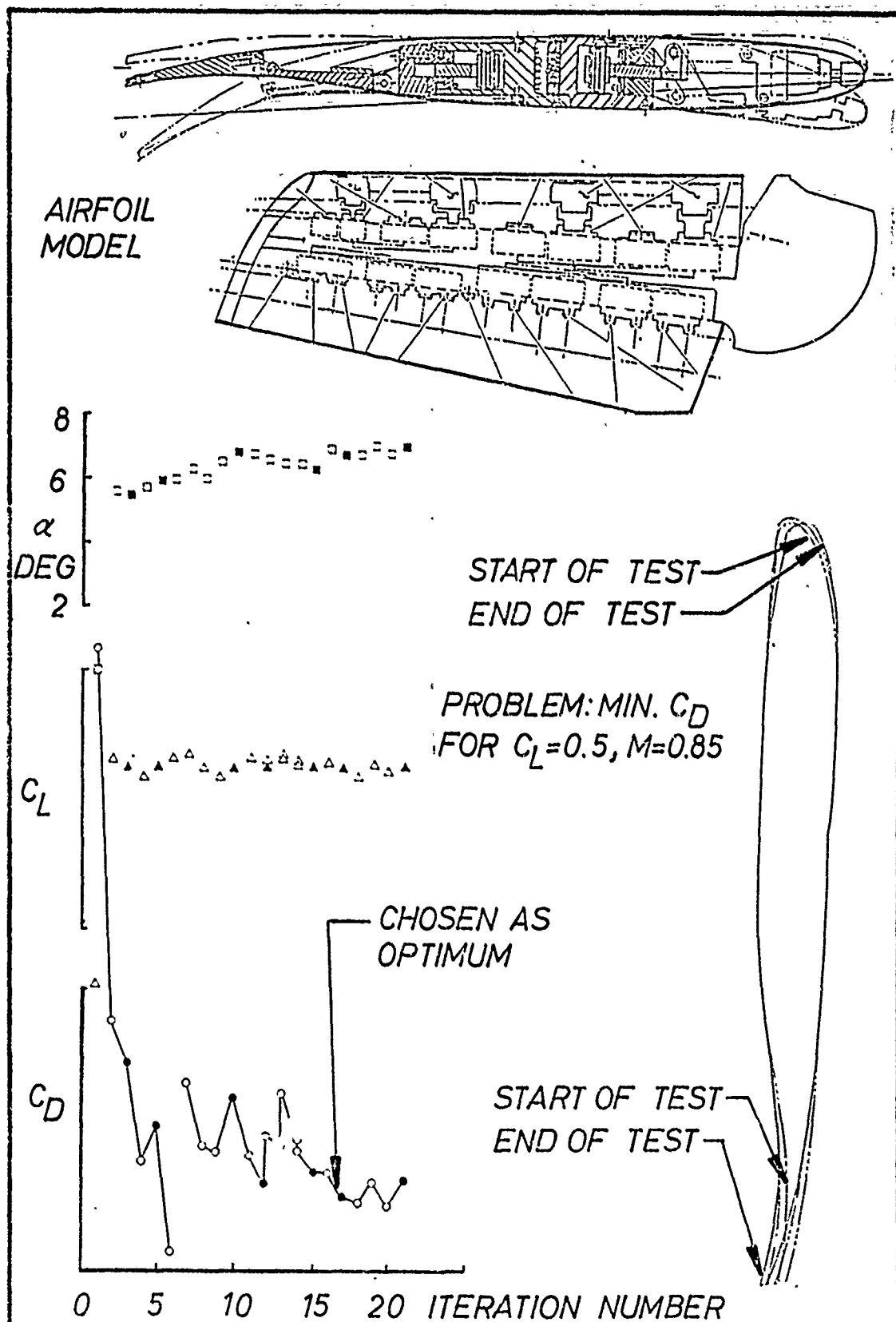


AIRFOIL MODEL



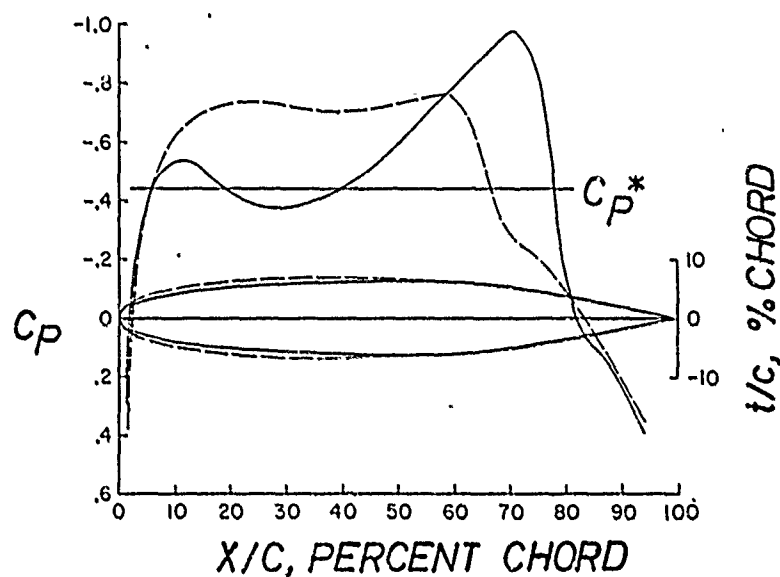
TWO-DIMENSIONAL FLEXIBLE, TRANSONIC AIRFOIL
OPTIMIZATION BY GRADIENT STRATEGY

FIGURE 7

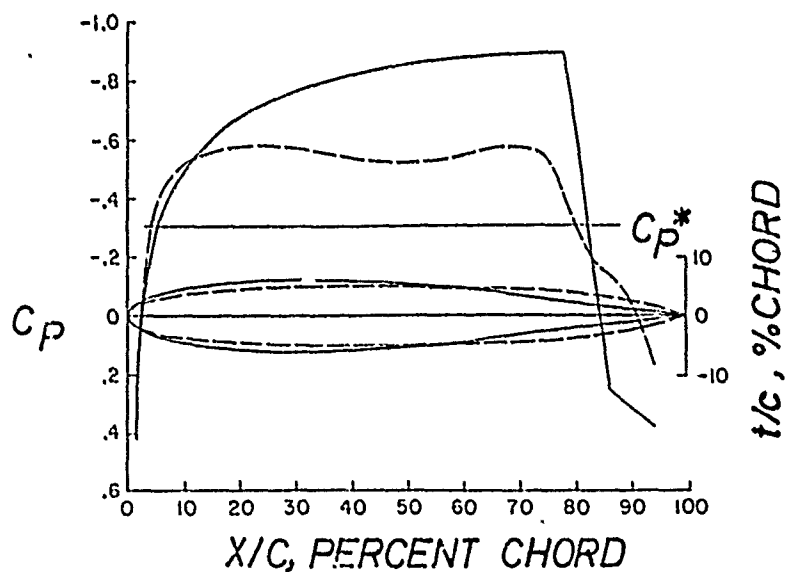


THREE-DIMENSIONAL FLEXIBLE
AIRFOIL OPTIMIZATION

FIGURE 8



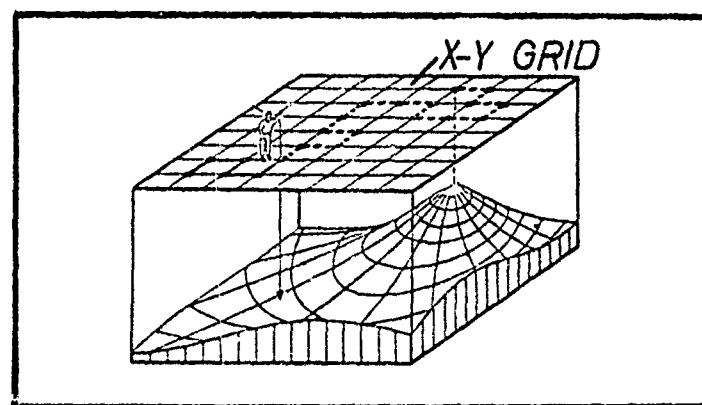
— INITIAL AIRFOIL, $C_D=0.0083$, $V=0.721$
 -- FINAL AIRFOIL, $C_D=0.0009$, $V=0.756$
 VOLUME MAXIMIZATION, $C_D \leq 0.001$, $C_L=0.0$, $M=0.8$



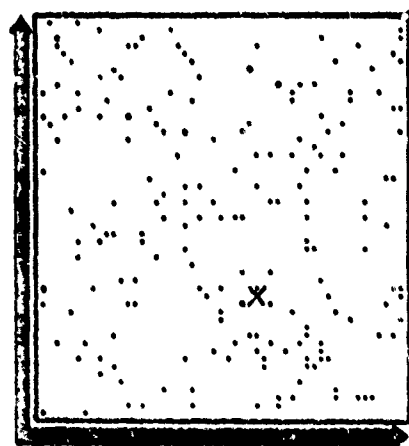
— INITIAL AIRFOIL, $C_D=0.0524$, $V=0.680$
 -- FINAL AIRFOIL, $C_D=0.0007$, $V=0.654$
 DRAG MINIMIZATION, $V \geq 0.65$, $C_L=0.0$, $M=0.85$

TWO-DIMENSIONAL TRANSONIC
 AIRFOIL OPTIMIZATION, GRADIENT ST.

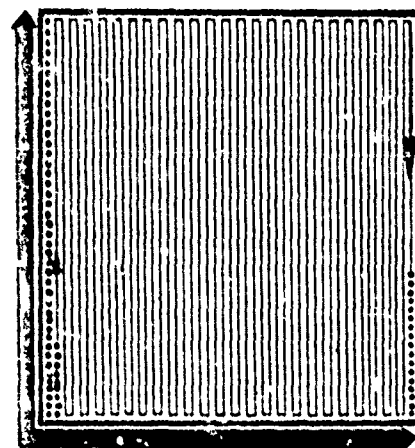
FIGURE 9



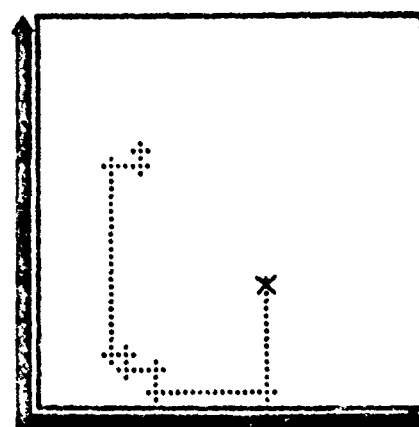
MODEL FOR SIMPLE OPTIMIZATION PROBLEM



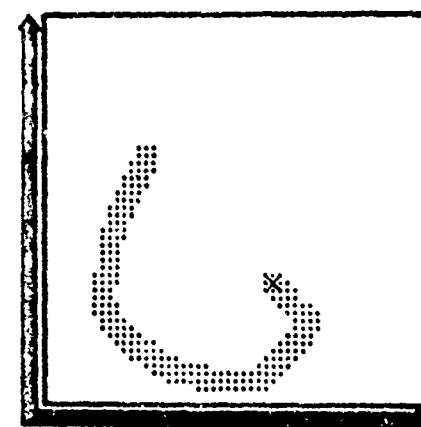
A. RANDOM SOUNDINGS



B. COMPLETE SEARCH



C. GAUSS-SEIDEL STRATEGY



D. GRADIENT STRATEGY

COMPARISON OF OPTIMIZATION STRATEGIES FOR SIMPLE PROBLEM

FIGURE 10

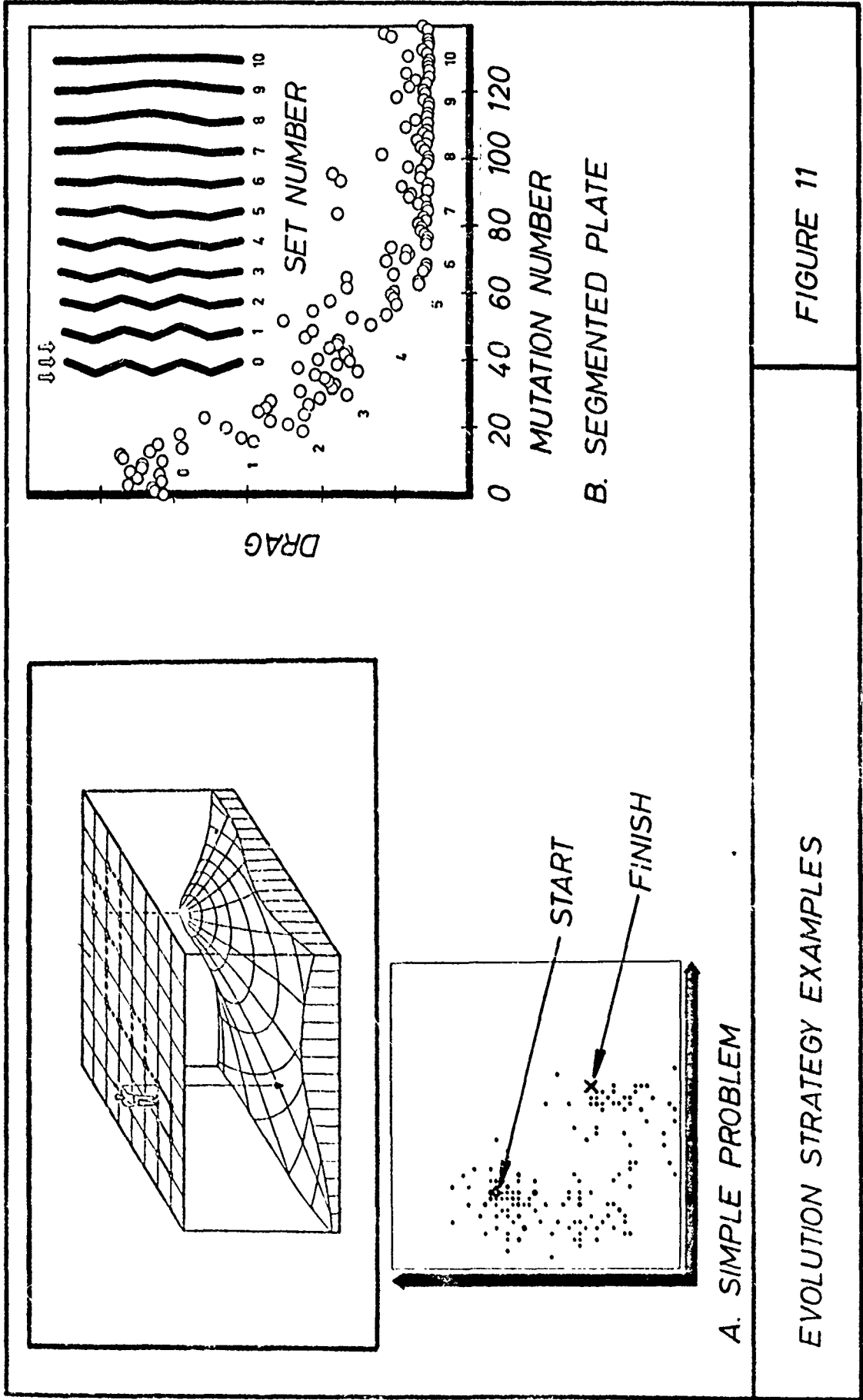
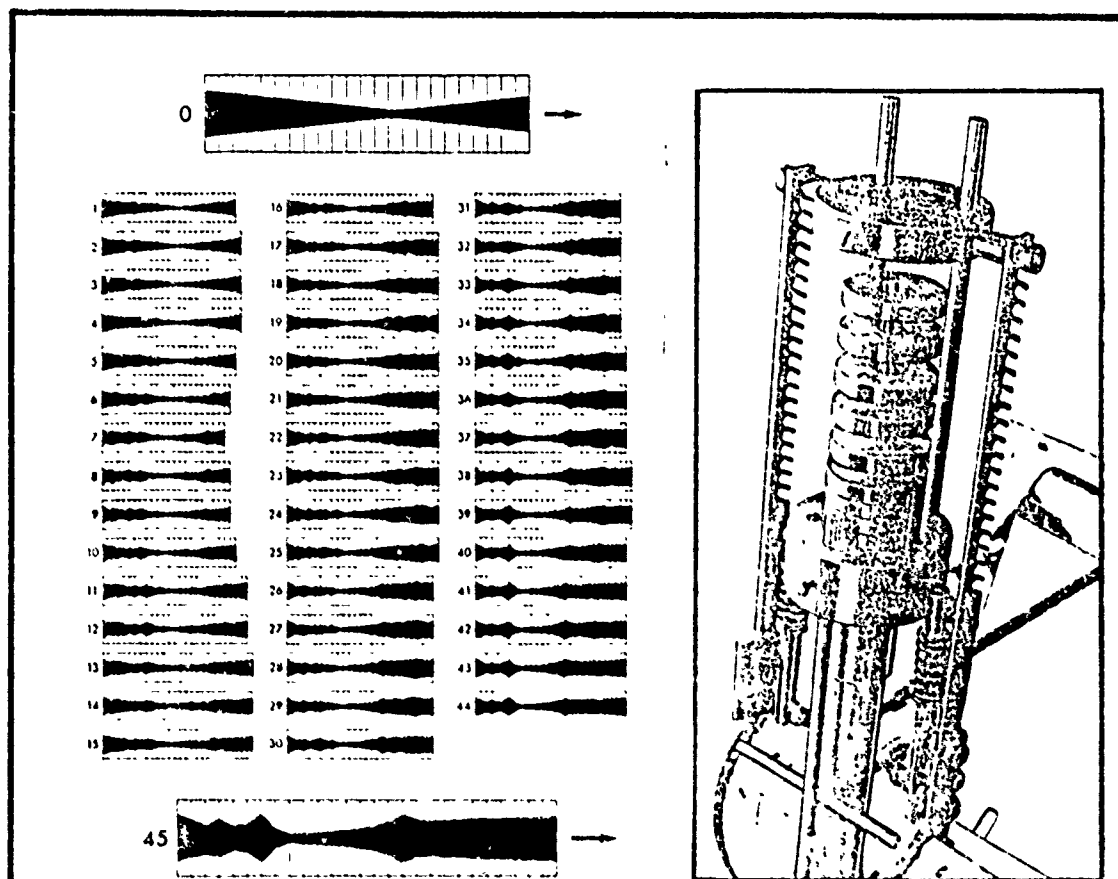
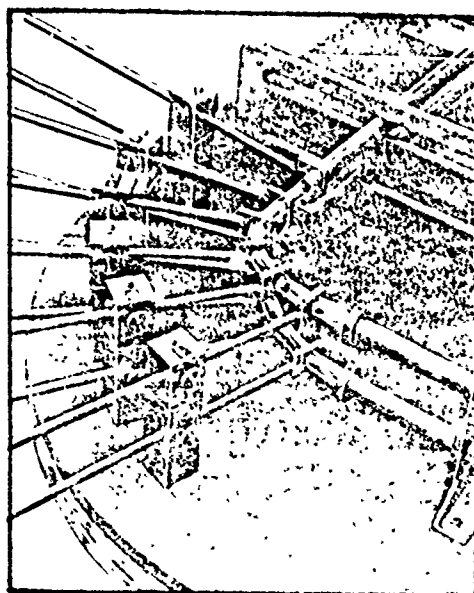


FIGURE 11

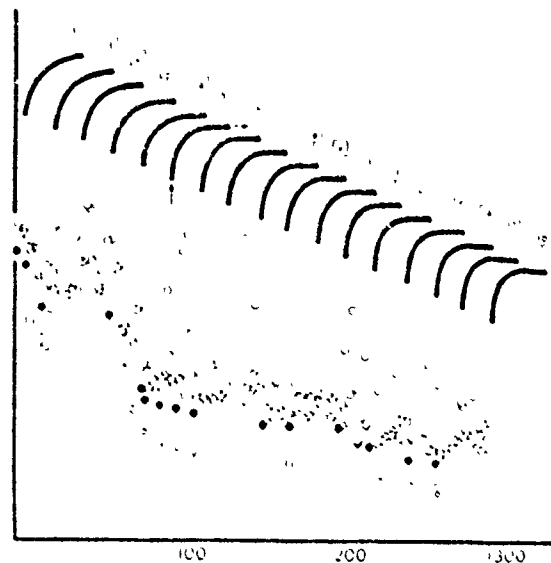
EVOLUTION STRATEGY EXAMPLES



A. TWO-PHASE SUPERSONIC NOZZLE



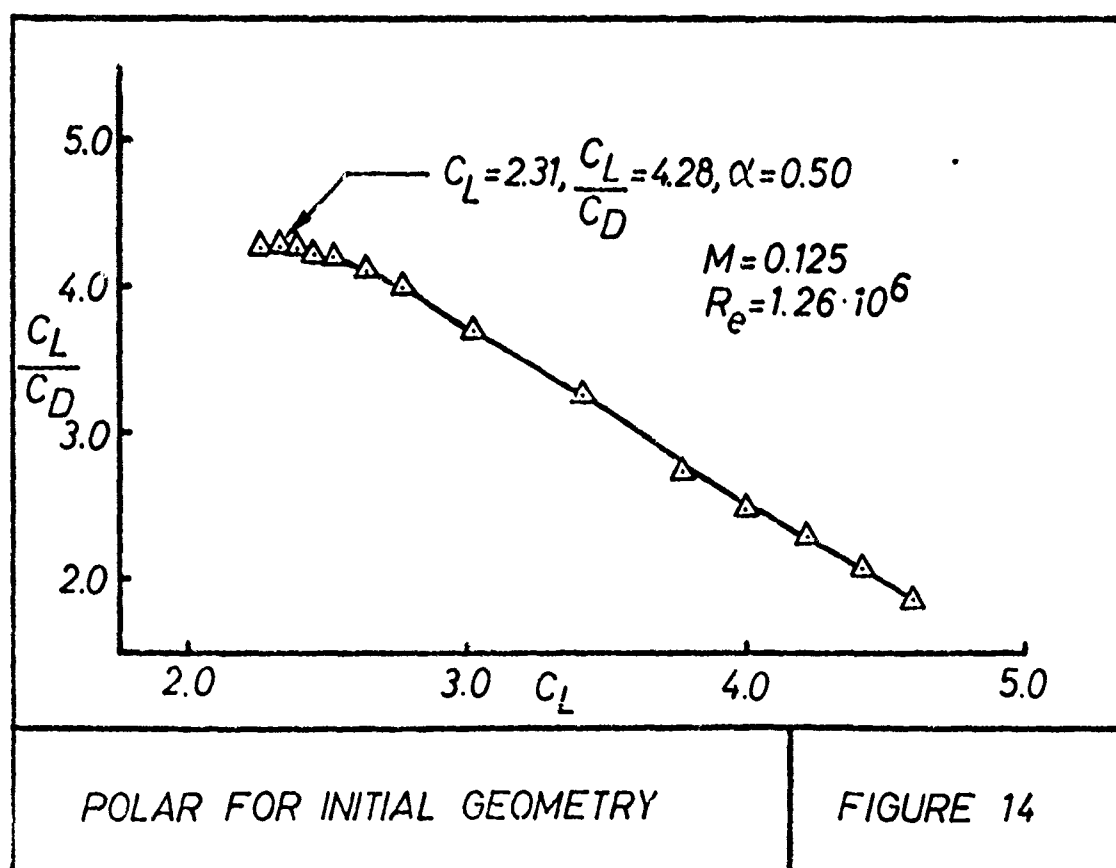
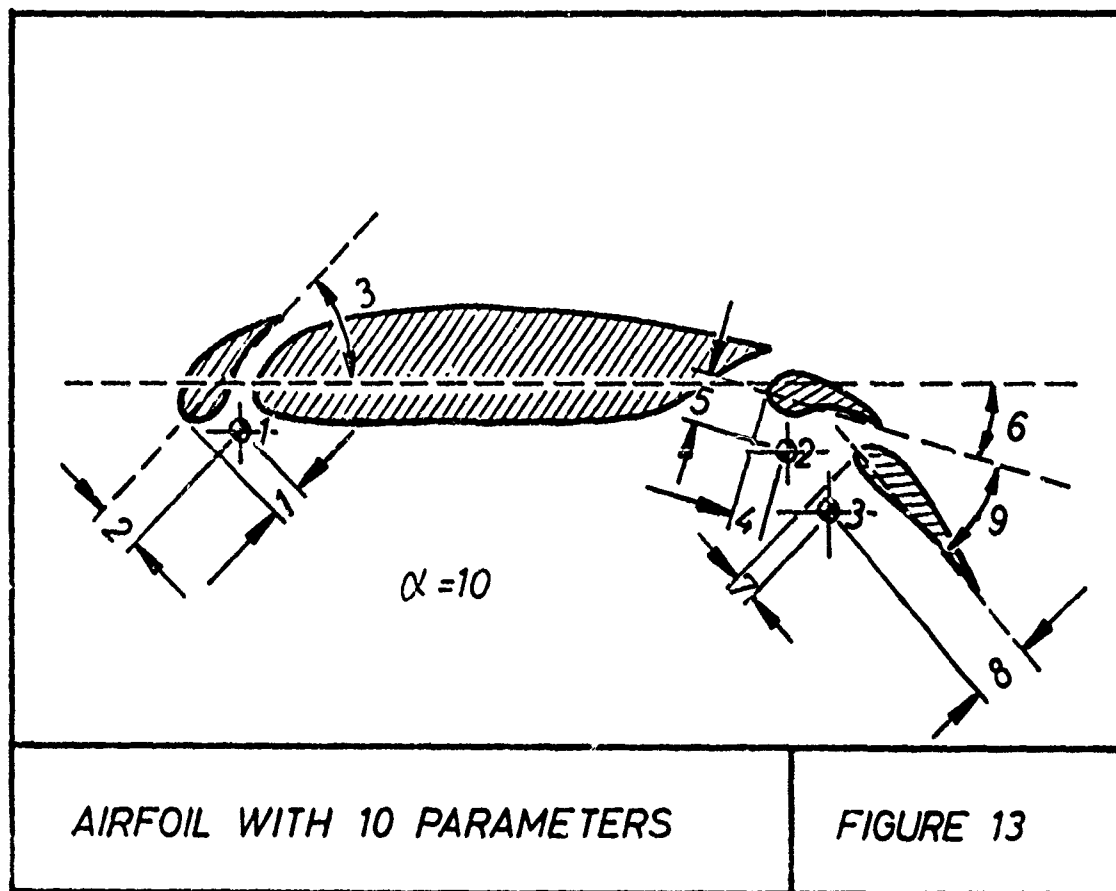
HEAD LOSS

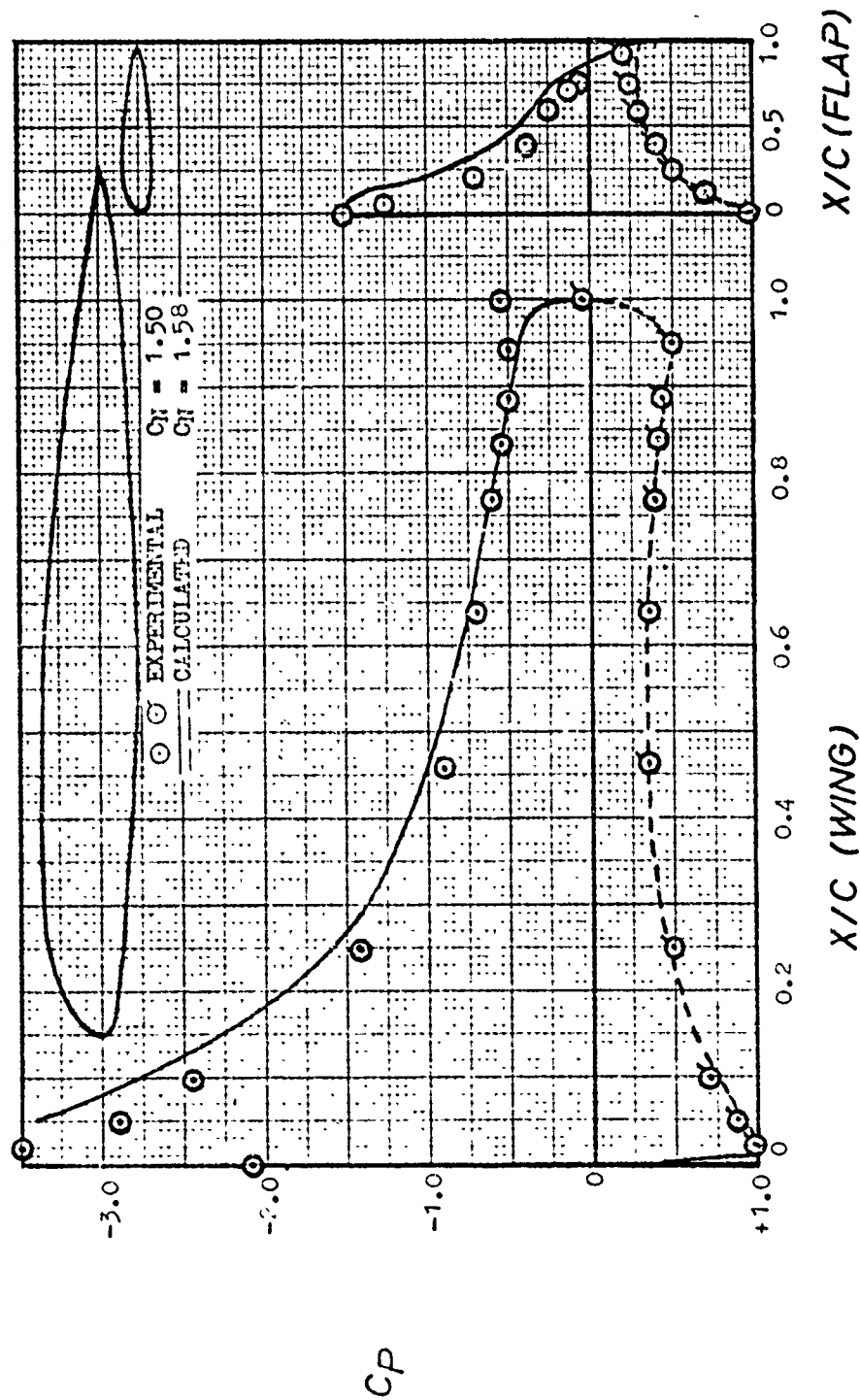


B. 90° FLEXIBLE TUBING BEND

EVOLUTION STRATEGY EXAMPLES
(CONTINUED)

FIGURE 12



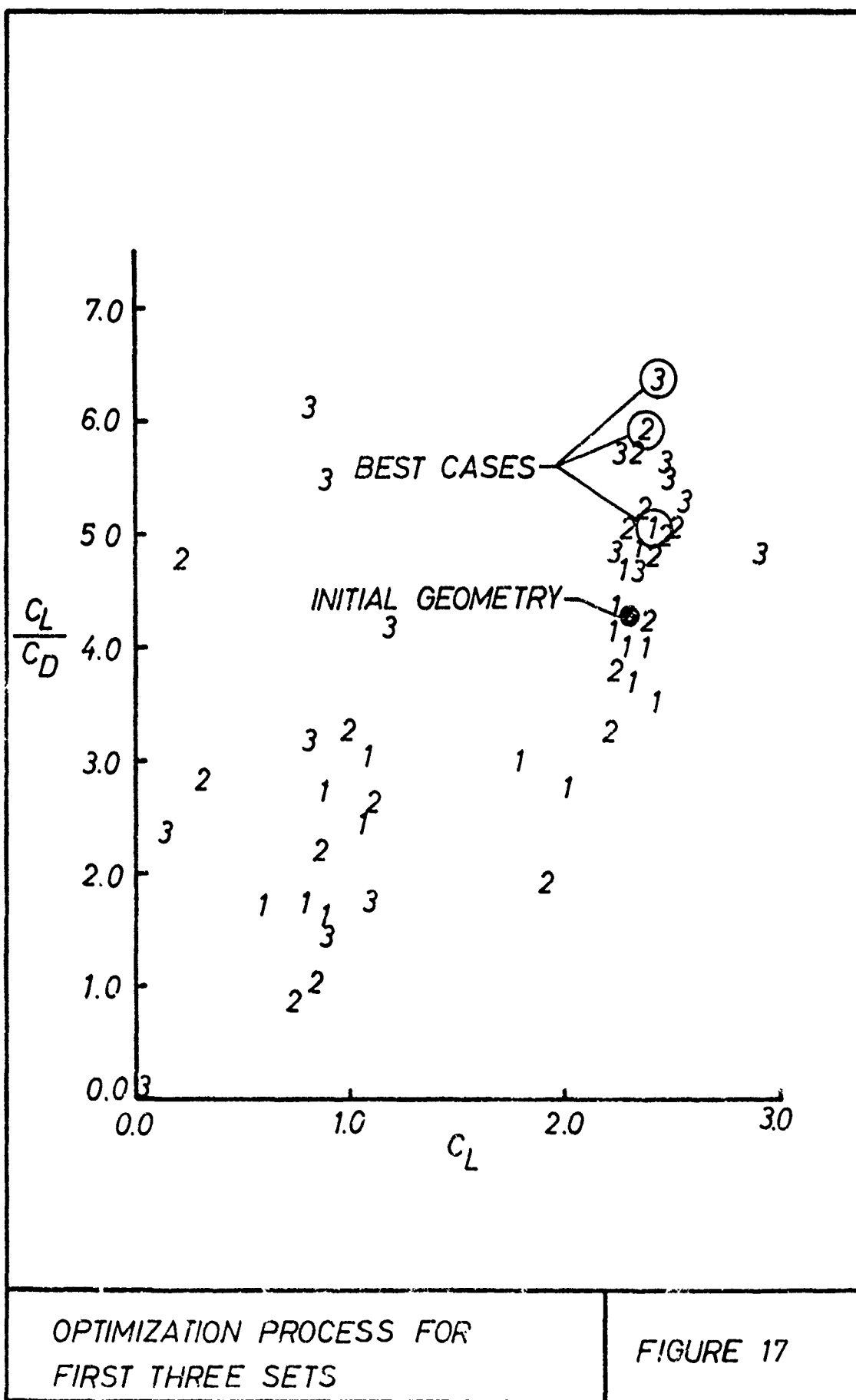


COMPARISON OF EXPERIMENTAL AND PREDICTED PRESSURE DISTRIBUTIONS FOR NACA 23012 AIRFOIL WITH 1 DEGREE FLAP



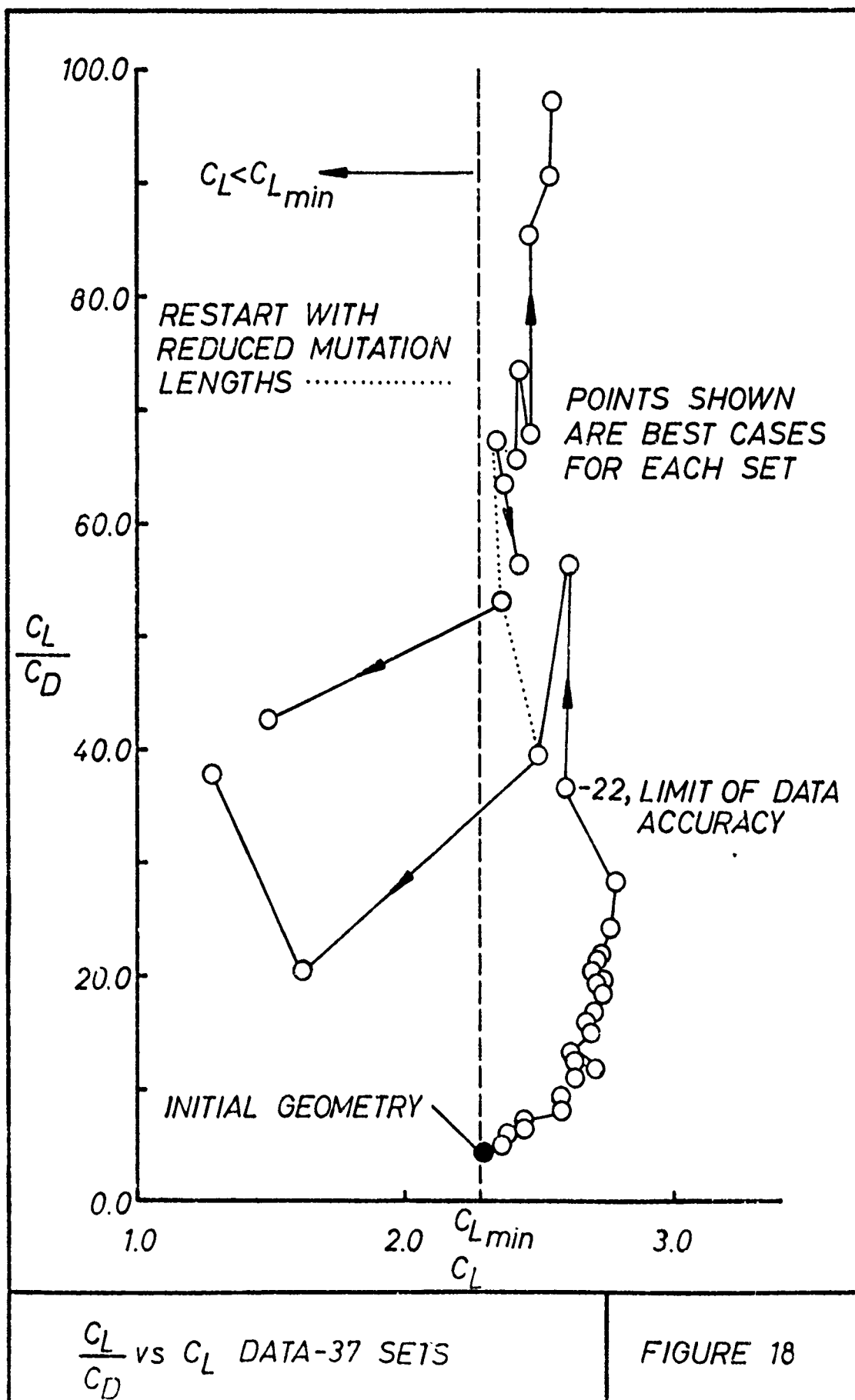
C. PROGRAM OUTPUT

FIGURE 16



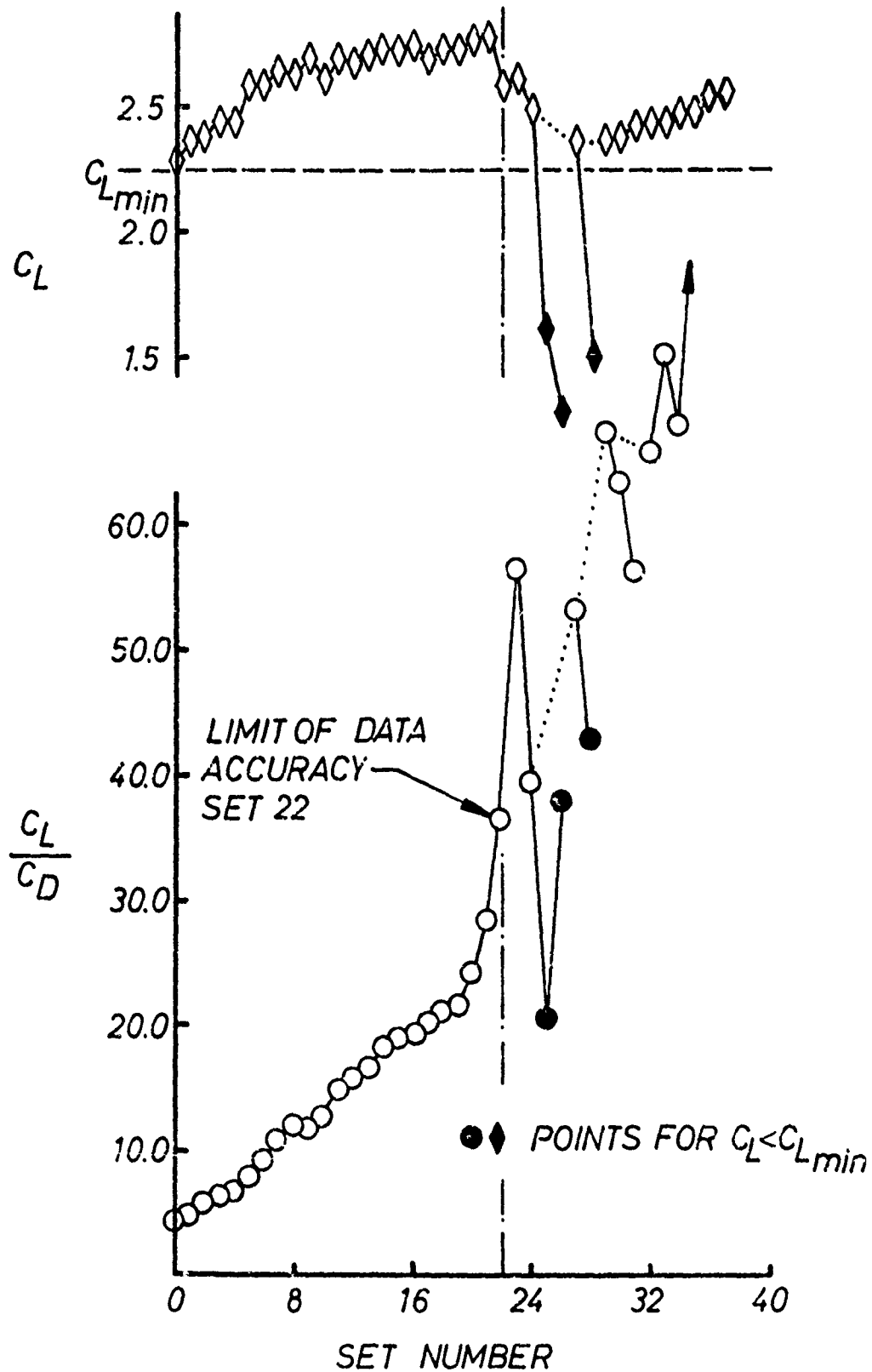
OPTIMIZATION PROCESS FOR
FIRST THREE SETS

FIGURE 17



$\frac{C_L}{C_D}$ vs C_L DATA-37 SETS

FIGURE 18



C_L AND $\frac{C_L}{C_D}$ VS. SET NUMBER

FIGURE 19

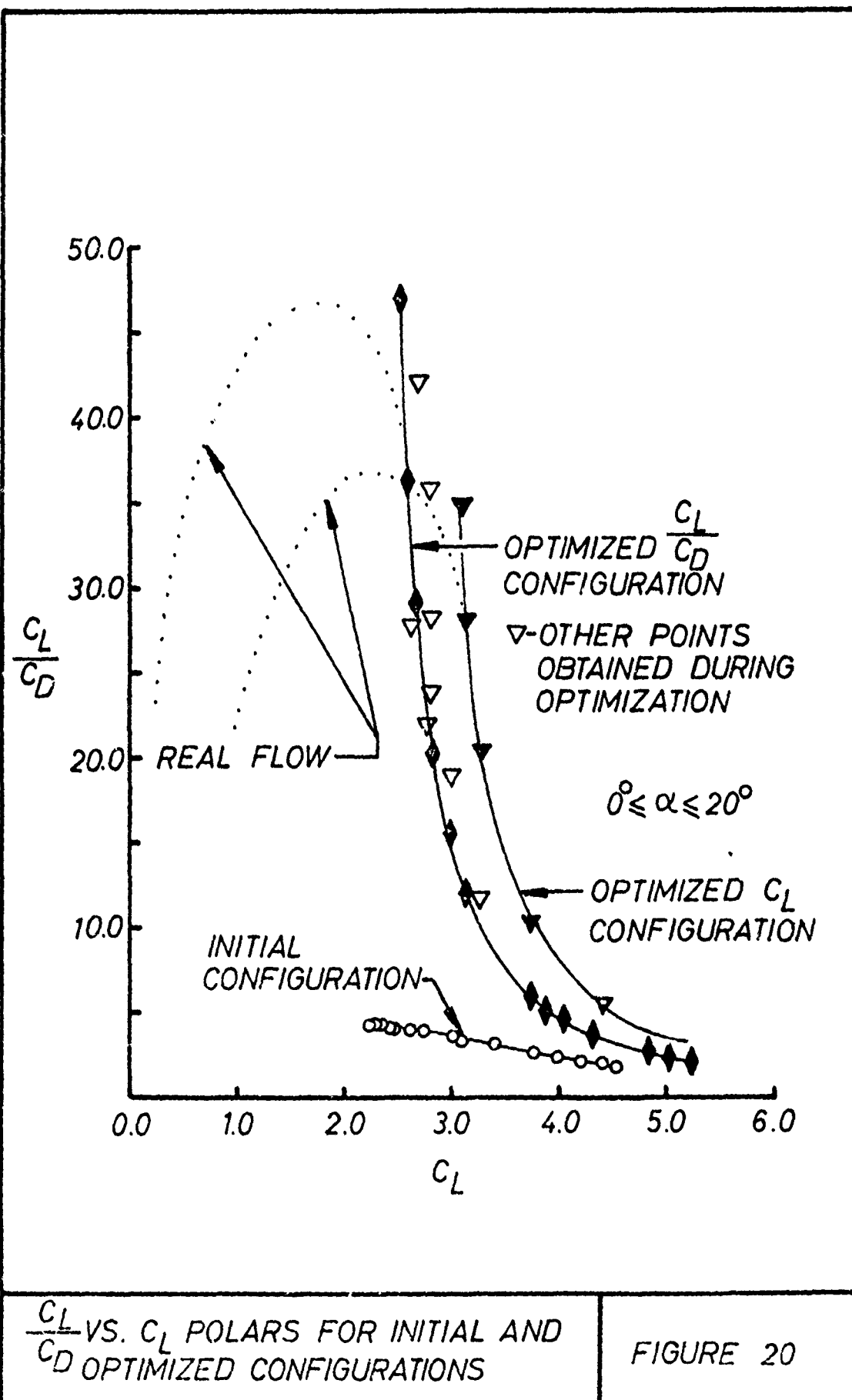


FIGURE 20

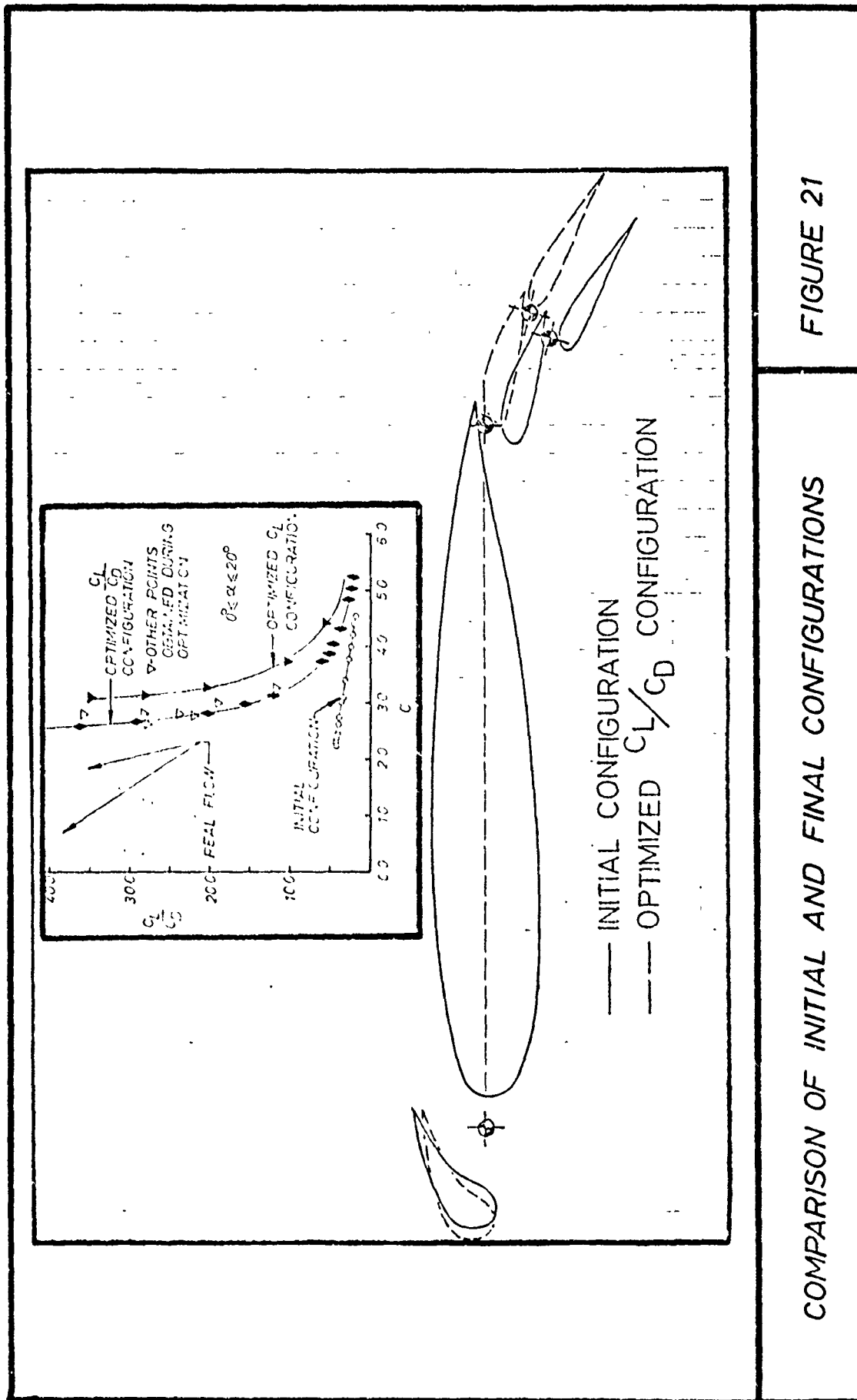


FIGURE 21

COMPARISON OF INITIAL AND FINAL CONFIGURATIONS

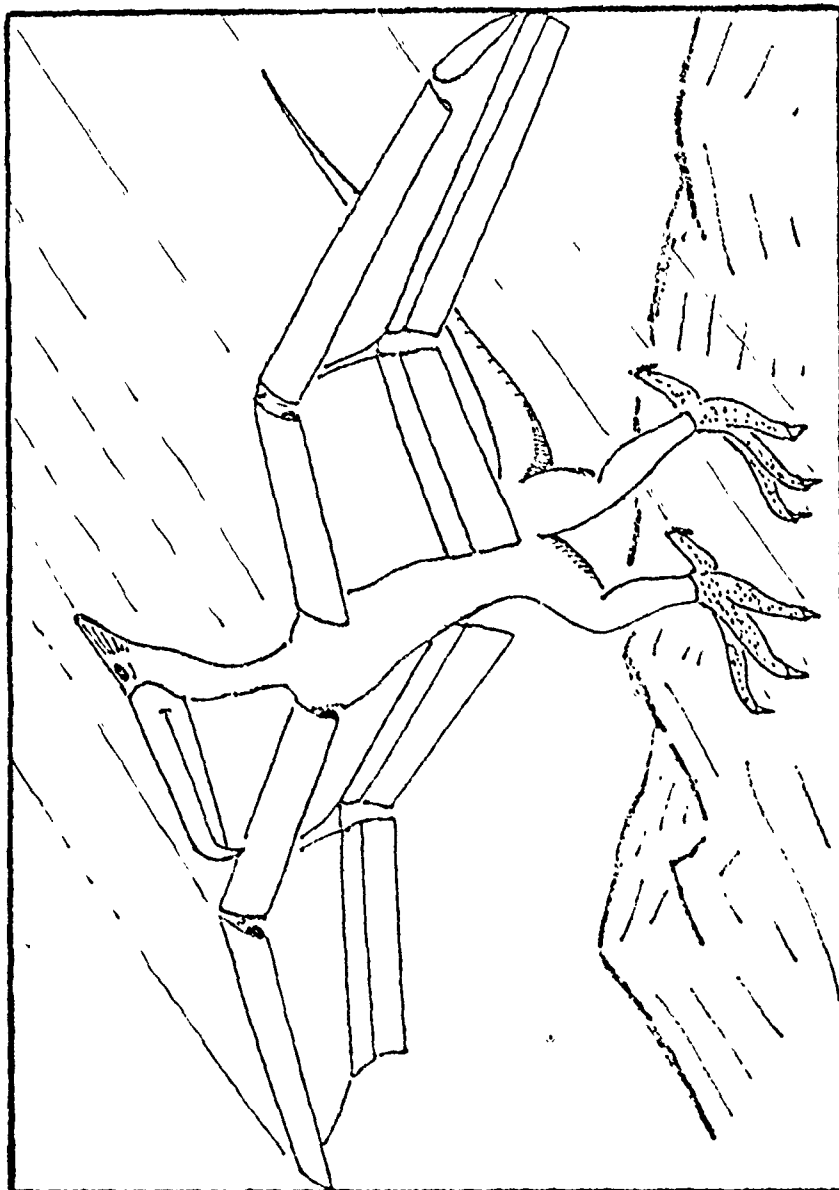


FIGURE 22

EVOLUTION STRATEGY - THE SKY IS THE LIMIT....

APPENDIX (i) AERODYNAMIC COEFFICIENT PROGRAM INPUT

	*BB-PROFILE	A1-725-146	SLOTTED KRUEGER	DOUBLE-SLOTTED TE FLAP OPTIMIZATION				
100	4	85	1					
200	1	23	23					
300	1.6100	-0.4200						
400	0.0000	0.0344	0.0689	0.1378	0.2067	0.2756	0.3445	0.4134
500	0.5512	0.6890	0.8268	0.9646	1.1024	1.2402	1.3780	1.5157
600	1.6535	1.7913	1.9291	2.0670	2.2047	2.3425	2.4803	
700	0.4134	0.5994	0.6683	0.7441	0.7992	0.8543	0.8819	0.8957
800	0.9232	0.9232	0.9163	0.9026	0.8888	0.8612	0.8406	0.8130
900	0.7923	0.7579	0.7303	0.6890	0.6407	0.5925	0.5512	
1000	0.0000	0.0344	0.0689	0.1378	0.2067	0.2756	0.3445	0.4134
1100	0.5512	0.6890	0.8268	0.9646	1.1024	1.2402	1.3780	1.5157
1200	1.6535	1.7913	1.9291	2.0670	2.2047	2.3425	2.4803	
1300	0.4134	0.2070	0.1378	0.0689	0.0207	0.0069	0.0000	0.0207
1400	0.0965	0.2070	0.2894	0.3445	0.3858	0.4272	0.4616	0.4961
1500	0.5236	0.5443	0.5512	0.5512	0.5512	0.5512	0.5512	
1600	2	37	37					
1700	-0.5000	0.0000	12.0000	0.0000				
1800	0.0000	0.0344	0.1033	0.1722	0.2411	0.3100	0.3789	0.4478
1900	0.5167	0.5856	0.6614	0.7303	0.8000	0.8688	0.9377	1.0066
2000	2.4145	2.9929	3.6571	4.3543	5.0988	5.8433	6.5878	7.3323
2100	8.2181	8.6122	8.9264	9.1951	9.6870	10.1004	10.6033	11.2110
2200	11.5596	11.9110	12.2252	12.5091	12.5394			
2300	0.0000	0.1654	0.2632	0.3238	0.3707	0.4079	0.4396	0.4685
2400	0.4919	0.5154	0.5374	0.5843	0.6339	0.6848	0.7372	0.7896
2500	0.8433	0.8929	0.9384	0.9701	0.9894	0.9756	0.9467	0.9067
2600	0.8654	0.8254	0.7796	0.7551	0.6862	0.6228	0.5374	0.4258
2700	0.3596	0.2921	0.2301	0.1791	0.1722			
2800	0.0000	0.0344	0.1033	0.1722	0.2411	0.3100	0.3789	0.4478
2900	0.5167	0.5856	0.6614	0.7303	0.8000	0.8688	0.9377	1.0066
3000	2.4145	2.9929	3.6571	4.3543	5.0988	5.8433	6.5878	7.3323
3100	8.2181	8.6122	8.9264	9.1951	9.6870	10.1004	10.6033	11.2110
3200	11.5596	11.9110	12.2252	12.5091	12.5394			
3300	0.0000	0.1654	0.2632	0.3238	0.3707	0.4079	0.4396	0.4685
3400	0.4919	0.5154	0.5374	0.5843	0.6339	0.6848	0.7372	0.7896
3500	0.8433	0.8929	0.9384	0.9701	0.9894	0.9756	0.9467	0.9067
3600	0.8654	0.8254	0.7796	0.7551	0.6862	0.6228	0.5374	0.4258
3700	0.3596	0.2921	0.2301	0.1791	0.1722			
3800	0.0000	0.0344	0.1033	0.1722	0.2411	0.3100	0.3789	0.4478
3900	0.5167	0.5856	0.6614	0.7303	0.8000	0.8688	0.9377	1.0066
4000	2.4145	2.9929	3.6571	4.3543	5.0988	5.8433	6.5878	7.3323
4100	8.2181	8.6122	8.9264	9.1951	9.6870	10.1004	10.6033	11.2110
4200	11.5596	11.9110	12.2252	12.5091	12.5394			
4300	0.0000	0.1654	0.2632	0.3238	0.3707	0.4079	0.4396	0.4685
4400	0.4919	0.5154	0.5374	0.5843	0.6339	0.6848	0.7372	0.7896
4500	0.8433	0.8929	0.9384	0.9701	0.9894	0.9756	0.9467	0.9067
4600	0.8654	0.8254	0.7796	0.7551	0.6862	0.6228	0.5374	0.4258
4700	0.3596	0.2921	0.2301	0.1791	0.1722			
4800	0.0000	0.0344	0.1033	0.1722	0.2411	0.3100	0.3789	0.4478
4900	0.5167	0.5856	0.6614	0.7303	0.8000	0.8688	0.9377	1.0066
5000	2.4145	2.9929	3.6571	4.3543	5.0988	5.8433	6.5878	7.3323
5100	8.2181	8.6122	8.9264	9.1951	9.6870	10.1004	10.6033	11.2110
5200	11.5596	11.9110	12.2252	12.5091	12.5394			
5300	0.0000	0.1654	0.2632	0.3238	0.3707	0.4079	0.4396	0.4685
5400	0.4919	0.5154	0.5374	0.5843	0.6339	0.6848	0.7372	0.7896
5500	0.8433	0.8929	0.9384	0.9701	0.9894	0.9756	0.9467	0.9067
5600	0.8654	0.8254	0.7796	0.7551	0.6862	0.6228	0.5374	0.4258
5700	0.3596	0.2921	0.2301	0.1791	0.1722			
5800	0.0000	0.0344	0.1033	0.1722	0.2411	0.3100	0.3789	0.4478
5900	0.5167	0.5856	0.6614	0.7303	0.8000	0.8688	0.9377	1.0066
6000	2.4145	2.9929	3.6571	4.3543	5.0988	5.8433	6.5878	7.3323
6100	8.2181	8.6122	8.9264	9.1951	9.6870	10.1004	10.6033	11.2110
6200	11.5596	11.9110	12.2252	12.5091	12.5394			
6300	0.0000	0.1654	0.2632	0.3238	0.3707	0.4079	0.4396	0.4685
6400	0.4919	0.5154	0.5374	0.5843	0.6339	0.6848	0.7372	0.7896
6500	0.8433	0.8929	0.9384	0.9701	0.9894	0.9756	0.9467	0.9067
6600	0.8654	0.8254	0.7796	0.7551	0.6862	0.6228	0.5374	0.4258
6700	0.3596	0.2921	0.2301	0.1791	0.1722			
6800	0.0000	0.0344	0.1033	0.1722	0.2411	0.3100	0.3789	0.4478
6900	0.5167	0.5856	0.6614	0.7303	0.8000	0.8688	0.9377	1.0066
7000	2.4145	2.9929	3.6571	4.3543	5.0988	5.8433	6.5878	7.3323
7100	8.2181	8.6122	8.9264	9.1951	9.6870	10.1004	10.6033	11.2110
7200	11.5596	11.9110	12.2252	12.5091	12.5394			
7300	0.0000	0.1654	0.2632	0.3238	0.3707	0.4079	0.4396	0.4685
7400	0.4919	0.5154	0.5374	0.5843	0.6339	0.6848	0.7372	0.7896
7500	0.8433	0.8929	0.9384	0.9701	0.9894	0.9756	0.9467	0.9067
7600	0.8654	0.8254	0.7796	0.7551	0.6862	0.6228	0.5374	0.4258
7700	0.3596	0.2921	0.2301	0.1791	0.1722			
7800	0.0000	0.0344	0.1033	0.1722	0.2411	0.3100	0.3789	0.4478
7900	0.5167	0.5856	0.6614	0.7303	0.8000	0.8688	0.9377	1.0066
8000	2.4145	2.9929	3.6571	4.3543	5.0988	5.8433	6.5878	7.3323
8100	8.2181	8.6122	8.9264	9.1951	9.6870	10.1004	10.6033	11.2110
8200	11.5596	11.9110	12.2252	12.5091	12.5394			
8300	0.0000	0.1654	0.2632	0.3238	0.3707	0.4079	0.4396	0.4685
8400	0.4919	0.5154	0.5374	0.5843	0.6339	0.6848	0.7372	0.7896
8500	0.8433	0.8929	0.9384	0.9701	0.9894	0.9756	0.9467	0.9067
8600	0.8654	0.8254	0.7796	0.7551	0.6862	0.6228	0.5374	0.4258
8700	0.3596	0.2921	0.2301	0.1791	0.1722			
8800	0.0000	0.0344	0.1033	0.1722	0.2411	0.3100	0.3789	0.4478
8900	0.5167	0.5856	0.6614	0.7303	0.8000	0.8688	0.9377	1.0066
9000	2.4145	2.9929	3.6571	4.3543	5.0988	5.8433	6.5878	7.3323
9100	8.2181	8.6122	8.9264	9.1951	9.6870	10.1004	10.6033	11.2110
9200	11.5596	11.9110	12.2252	12.5091	12.5394			
9300	0.0000	0.1654	0.2632	0.3238	0.3707	0.4079	0.4396	0.4685
9400	0.4919	0.5154	0.5374	0.5843	0.6339	0.6848	0.7372	0.7896
9500	0.8433	0.8929	0.9384	0.9701	0.9894	0.9756	0.9467	0.9067
9600	0.8654	0.8254	0.7796	0.7551	0.6862	0.6228	0.5374	0.4258
9700	0.3596	0.2921	0.2301	0.1791	0.1722			
9800	0.0000	0.0344	0.1033	0.1722	0.2411	0.3100	0.3789	0.4478
9900	0.5167	0.5856	0.6614	0.7303	0.8000	0.8688	0.9377	1.0066
10000	2.4145	2.9929	3.6571	4.3543	5.0988	5.8433	6.5878	7.3323

ELEMENT GEOMETRY

SLOT DATA

FLOW PARAMETERS

APPENDIX (ii) GEOMETRY MODIFICATION PROGRAM

```

100 C -----
200 C
300 C PROGRAM GEOM2 : RANDOM MODIFICATION OF A10G 10 DEGREES
400 C OF FREEDOM
500 C
600 C CAPABILITIES : A. MODIFY 0-10 PARAMETERS
700 C B. MAXIMUM 5 MUTATION LENGTH GROUPS
800 C C. MAXIMUM 10 CASES/LENGTH GROUP
900 C
1000 C DEGREES OF FREEDOM/10 PARAMETERS
1100 C 1 X-LOCATION, 1ST PIVOT POINT
1200 C 2 Y-LOCATION, 1ST PIVOT POINT
1300 C 3 DEFLECTION, 1ST FLAP WRT MAIN AIRFOIL
1400 C 4 X-LOCATION, 2ND PIVOT POINT
1500 C 5 Y-LOCATION, 2ND PIVOT POINT
1600 C 6 DEFLECTION, 2ND FLAP WRT MAIN AIRFOIL
1700 C 7 X-LOCATION, 3RD PIVOT POINT
1800 C 8 Y-LOCATION, 3RD PIVOT POINT
1900 C 9 DEFLECTION, 3RD FLAP WRT 2ND FLAP
2000 C 10 ANGLE OF ATTACK, MAIN AIRFOIL
2100 C * ALL DIMENSIONS IN INCHES OR DEGREES *
2200 C
2300 C INPUT: VARIABLE PURPOSE FORMAT
2400 C MODNUM MODIFICATION SET NUMBER 12
2500 C 11,12 INTEGERS USED BY RANDOM 110,711
2600 C NUMBER GENERATOR, RETURNED
2700 C EACH RUN
2800 C WINC NUMBER OF MUTATION LENGTH 12
2900 C GROUPS, <=5
3000 C NCASE NUMBER CASES/GROUP, <=10 12
3100 C QPAR(1) MODIFICATION CONTROL 1012
3200 C 1=1,10 =1, MODIFY PAR(1)
3300 C =0, DO NOT MODIFY PAR(1)
3400 C NPAR NUMBER OF PARAMETERS TO 12
3500 C BE MODIFIED
3600 C INCR(1) INCR(1):INCR(WINC)=MUTATION WINC*2
3700 C 1=1,2*WINC LENGTHS FOR X=1 PIVOT POINT (F5.2)
3800 C LOCATIONS
3900 C INCR(2):INCR(2*WINC)=
4000 C DEGREE MUTATION DEGREE FOR
4100 C FLAP DEFLECTION, AUPAR
4200 C INITIAL VALUES OF 10 10(F0.2)
4300 C 1=1,10 PARAMETERS
4400 C
4500 C -----
4600 C INTEGER MODNUM,NCASE,NPAR,QPAR(10),11,12,MOD1,11,12,13,MOD2
4700 C INTEGER L4,DWINC
4800 C REAL PAR(5,10,10),IPAR(10),INCR(10),X1,Z1,X2,Z2,X3,Z3,INCR
4900 C REAL SIGMA
5000 C -----X1,Z1,X2,Z2,X3,Z3 SPECIFY RANGE OF MOTION FOR PIVOT POINTS
5100 C -----IN INCHES, HORIZONTAL AND VERTICAL AXIAL DIRECTIONS, AND
5200 C -----CAN BE MODIFIED TO SUIT USER
5300 C DATA X1,Z1,X2,Z2,X3,Z3,MOD1/1.5,1.0,1.5,1.0,1.5,1.0,1.0/
5400 C ACCEPT 100,MODNUM,11,12,WINC,NCASE,(QPAR(1),1=1,10),NPAR
5500 C 100 FORMAT (12,/,110,/,110,/,12,/,12,/,1012,/,12)
5600 C DWINC=WINC*2
5700 C DO 150 1=1,DWINC
5800 C ACCEPT 200,INCR(1)
5900 C 200 FORMAT (F5.2)
6000 C 150 CONTINUE
6100 C ACCEPT 300,(IPAR(1),1=1,10)
6200 C 300 FORMAT (F0.2,9(F0.2))
6300 C -----LOOP FOR WINC MUTATION LENGTHS
6400 C DO 1000 L1=1,WINC
6500 C INCR(L1)=INCR(L1)+0.01
6600 C -----LOOP FOR NUMBER OF CASES/LENGTH GROUP
6700 C DO 900 L2=1,NCASE
6800 C L4=0
6900 C -----LOOP FOR 10 PARAMETERS
7000 C DO 800 L3=1,10
7100 C IF(QPAR(L3).NE.1) GO TO 700
7200 C -----SHOULD PAR(1) BE MODIFIED
7300 C 500 MULT=1
7400 C -----CALL RANDOM NUMBER GENERATOR, RANDOM PARAMETER SELECTION
7500 C CALL RANDU(11,12,L4)
7600 C 12(L4)OP.GE.0.50 GO TO 600
7700 C -----CALL RANDOM NUMBER GENERATOR, POSITIVE OR NEGATIVE INCR.
7800 C CALL RANDU(11,12,SIGMA)
7900 C 11(SIGMA)OP.LE.0.50 CLT=-1
8000 C

```

```

8100      C
8200      C
8300      C
8400      IF(L3.EQ.1) PAR(L1,L2,L3)=IPAR(1)+(MULT*INCR(L1)*X1)
8500      IF(L3.EQ.2) PAR(L1,L2,L3)=1PAR(2)+(MULT*INCR(L1)*Z1)
8600      IF(L3.EQ.3) PAR(L1,L2,L3)=1PAR(3)+(MULT*INCR(L1+NINC))
8700      IF(L3.EQ.4) PAR(L1,L2,L3)=1PAR(4)+(MULT*INCR(L1)*X2)
8800      IF(L3.EQ.5) PAR(L1,L2,L3)=1PAR(5)+(MULT*INCR(L1)*Z2)
8900      IF(L3.EQ.6) PAR(L1,L2,L3)=1PAR(6)+(MULT*INCR(L1+NINC))
9000      IF(L3.EQ.7) PAR(L1,L2,L3)=1PAR(7)+(MULT*INCR(L1)*X3)
9100      IF(L3.EQ.8) PAR(L1,L2,L3)=1PAR(8)+(MULT*INCR(L1)*Z3)
9200      IF(L3.EQ.9) PAR(L1,L2,L3)=1PAR(9)+(MULT*INCR(L1+NINC))
9300      IF(L3.EQ.10) PAR(L1,L2,L3)=1PAR(10)+(MULT*INCR(L1+NINC))
9400      IF(PAR(L1,L2,10).LT.0.0) GOTO 500
9500      GOTO 750
9600      600      L4=L4+1
9700      C-----CHECK TO PREVENT DUPLICATION OF INITIAL GEOMETRY
9800      IF(L4.EQ.NPAR) GOTO 400
9900      700      PAR(L1,L2,L3)=1PAR(L3)
10000     750      CONTINUE
10100     800      CONTINUE
10200     900      CONTINUE
10300     1000     CONTINUE
10400     WRITE (6,1100) MODNUM,11,12,NINC,NCASE
10500     1100     FORMAT (///,7X,'GEOMETRY MODIFICATION',2X,12,/,7X,'I1= ',
10600     X          110,2X,'I2= ',110,2X,'NINC= ',12,2X,'NCASE= ',12,/,9X,
10700     X          'INCR NUM',3X,'% STEP',3X,'DEGREE')
10800     DO 1240 I=1,NINC
10900     INCR(I)=INCR(I)+100.0
11000     WRITE (6,1220) I,INCR(I),INCR(I+NINC)
11100     1220     FORMAT (12X,12,7X,F5.2,4X,F5.3)
11200     CONTINUE
11300     WRITE (6,1200) (GPARG(I),I=1,10)
11400     1200     FORMAT (///,9X,'PAR1 PAR2 PAR3 PAR4 PAR5 PAR6 PAR7',
11500     X          ' PAR8 PAR9 PAR10',/,1 GPARG ' ,10(11,5X))
11600     WRITE (6,1300) (IPAR(I),I=1,10)
11700     1300     FORMAT (' IN.GE.',10(F6.2))
11800     WRITE (6,1400)
11900     1400     FORMAT (' IN CS ')
12000     DO 1700 L1=1,NINC
12100     DO 1600 L2=1,NCASE
12200     L3=(L1-1)*NCASE+L2

12300     WRITE (6,1500) L1,L3,(PAR(L1,L2,J),J=1,10)
12400     1500     FORMAT (/ ,X,12,X,12,X,10(F6.2),/,9X,'CL= ',6X,
12500     X          'CD= ',6X,'CL/CD= ',6X,'CM= ')
12600     1600     CONTINUE
12700     1700     CONTINUE
12800     STOP 'MODIFICATION COMPLETE'
12900     END

```

APPENDIX (iii) RANDOM NUMBER GENERATOR

D.4.9 RANDU Subroutine

The RANDU subroutine computes a pseudo-random number, as a single precision value uniformly distributed in the range:

0.0 .LE. value .LT. 1.0

Format:

CALL RANDU(i1,i2,x)

Arguments:

i1,i2

INTEGER*2 variables or array elements that contain the seed for computing the random number.

x

a real variable or array element where the computed random number is stored.

Notes:

1. The values of i1 and i2 are updated during the computation to contain the updated seed.
2. The algorithm for computing the random number value is as follows:

If i1=0, i2=0, set generator base

$$X(n+1) = 2^{*}16 + 3$$

otherwise

$$X(n+1) = (2^{*}16+3) * X(n) \text{mod } 2^{*}32$$

Store generator base X(n+1) in i1,i2.

Result is X(n+1) scaled to a real value Y(n+1), for 0.0 .LE. Y(n+1) .LT. 1.

GEOMETRY MODIFICATION 1

11= 1214584983 12= 98704257 NINC= 3 NCASE= 6

INCR NUM 1 STEP DEGREE
1 5
2 10
3 15

PAR1	PAR2	PAR3	PAR4	PAR5	PAR6	PAR7	PAR8	PAR9	PAR10
1.50	-0.50-30.00	0.25	0.25	0.00	15.00	0.00	0.20	15.00	0.50
CL= 2.31	CU= 0.54								
1 1	1.50	-0.45-24.50	0.25	0.00	15.00	-0.08	0.23	15.00	0.50
CL= 2.27	CU= 0.487	CL/CD= 4.68							
1 2	1.50	-0.45-30.00	0.17	0.00	14.50	0.00	0.33	15.00	0.50
CL= 2.00	CU= 0.556	CL/CD= 1.62							
1 3	1.50	-0.55-30.00	0.25	0.00	14.50	0.00	0.33	15.00	0.50
CL= 2.28	CU= 0.523	CL/CD= 4.36							
1 4	1.50	-0.50-30.00	0.33	0.00	15.00	-0.08	0.24	15.00	0.50
CL= 0.803	CU= 0.463	CL/CD= 1.73							
1 5	1.50	-0.50-30.00	0.25	0.00	14.50	0.00	0.28	15.00	1.00
CL= 2.29	CU= 0.534	CL/CD= 4.29							
1 6	1.50	-0.45-30.00	0.25	0.00	15.00	-0.08	0.24	15.00	0.00
CL= 2.25	CU= 0.544	CL/CD= 4.14							
2 7	1.50	-0.50-30.00	0.40	0.00	15.00	0.15	0.24	14.00	0.50
CL= 2.02	CU= 0.733	CL/CD= 2.76							
2 8	1.50	-0.50-30.00	0.10	0.00	15.00	0.00	0.28	15.00	0.50
CL= 0.905	CU= 0.330	CL/CD= 2.74							
2 9	1.50	-0.40-29.00	0.25	0.00	15.00	0.15	0.28	14.00	1.50
CL= 2.43	CU= 0.481	CL/CD= 5.05							
2 10	1.50	-0.40-31.00	0.10	0.00	15.00	0.00	0.32	15.00	0.50
CL= 1.07	CU= 0.438	CL/CD= 2.44							
2 11	1.05	-0.60-31.00	0.25	0.00	15.00	0.00	0.28	15.00	0.50
CL= 2.30	CU= 0.573	CL/CD= 4.01							
2 12	1.50	-0.50-29.00	0.75	0.00	16.00	0.15	0.28	15.00	1.50
CL= 2.41	CU= 0.604	CL/CD= 3.99							
3 13	1.27	-0.35-30.00	0.25	0.00	13.00	-0.22	0.28	15.00	0.50
CL= 0.599	CU= 0.346	CL/CD= 1.73							
3 14	1.50	-0.65-30.00	0.03	0.00	13.00	0.00	0.28	17.00	0.50
CL= 1.10	CU= 0.363	CL/CD= 3.63							
3 15	1.50	-0.35-32.00	0.25	0.00	17.00	-0.22	0.28	13.00	0.50
CL= 2.32	CU= 0.629	CL/CD= 3.69							
3 16	1.27	-0.35-28.00	0.47	0.00	13.00	0.22	0.43	15.00	0.50
CL= 1.82	CU= 0.606	CL/CD= 3.00							
3 17	1.27	-0.35-28.00	0.25	0.00	15.00	-0.22	0.28	15.00	0.50
CL= 2.37	CU= 0.483	CL/CD= 4.91							
3 18	1.27	-0.50-30.00	0.25	0.75	15.00	0.00	0.28	15.00	2.50
CL= 2.44	CU= 0.693	CL/CD= 3.52							

GEOMETRY MODIFICATION 2

11= 1234583643 12= 987045569 NINC= 3 NCASE= 6

INCR NUM 1 STEP DEGREE
1 5
2 10
3 15

PAR1	PAR2	PAR3	PAR4	PAR5	PAR6	PAR7	PAR8	PAR9	PAR10
1.27	-0.35-24.00	0.25	0.00	15.00	-0.22	0.22	0.28	15.00	0.50
CL= 2.37	CU= 0.483								
1 1	1.14	-0.40-27.50	0.17	0.00	15.00	-0.14	0.28	15.50	0.00
CL= 0.352	CU= 0.117	CL/CD= 2.84							
1 2	1.27	-0.35-28.50	0.17	0.00	15.00	-0.14	0.28	15.00	0.50
CL= 2.36	CU= 0.469	CL/CD= 5.03							
1 3	1.27	-0.35-28.00	0.25	0.00	15.50	-0.22	0.33	15.50	0.50
CL= 2.42	CU= 0.505	CL/CD= 4.77							
1 4	1.27	-0.40-28.00	0.33	0.00	14.50	-0.22	0.28	15.50	0.50
CL= 0.748	CU= 0.856	CL/CD= 0.874							
1 5	1.35	-0.35-27.50	0.17	0.00	15.50	-0.14	0.28	14.50	0.50
CL= 0.986	CU= 0.301	CL/CD= 3.28							
1 6	1.27	-0.40-28.50	0.33	0.00	15.00	-0.14	0.33	15.50	0.50
CL= 2.24	CU= 0.570	CL/CD= 3.80							
2 7	1.27	-0.45-28.00	0.10	0.00	15.00	-0.22	0.38	15.00	1.50
CL= 2.52	CU= 0.496	CL/CD= 5.08							
2 8	1.12	-0.45-28.00	0.25	0.00	15.00	-0.22	0.28	14.00	0.50
CL= 0.863	CU= 0.822	CL/CD= 1.05							
2 9	1.27	-0.35-29.00	0.40	0.00	15.00	-0.37	0.28	16.00	0.50
CL= 2.22	CU= 0.682	CL/CD= 3.26							
2 10	1.27	-0.25-28.00	0.25	0.00	15.00	-0.22	0.28	15.00	0.50
CL= 2.36	CU= 0.462	CL/CD= 5.15							
2 11	1.12	-0.35-27.00	0.25	0.00	15.00	-0.22	0.28	16.00	0.50
CL= 1.09	CU= 0.423	CL/CD= 2.58							
2 12	1.42	-0.35-27.00	0.25	0.00	14.00	-0.22	0.28	16.00	0.50
CL= 2.39	CU= 0.403	CL/CD= 5.92							
3 13	1.27	-0.20-30.00	0.25	0.75	15.00	0.00	0.28	13.00	2.50
CL= 2.39	CU= 0.561	CL/CD= 4.26							
3 14	1.50	-0.50-30.00	0.25	0.75	13.00	-0.22	0.28	15.00	0.50
CL= 0.876	CU= 0.398	CL/CD= 2.21							
3 15	1.27	-0.20-26.00	0.25	0.75	13.00	0.00	0.28	13.00	0.50
CL= 0.235	CU= 0.049	CL/CD= 4.80							
3 16	1.50	-0.35-26.00	0.25	0.75	15.00	-0.22	0.43	13.00	2.50
CL= 2.44	CU= 0.486	CL/CD= 5.02							
3 17	1.50	-0.35-26.00	0.47	0.00	17.00	0.00	0.43	15.00	2.50
CL= 1.92	CU= 1.00	CL/CD= 1.92							
3 18	1.27	-0.35-28.00	0.25	0.45	15.00	0.00	0.28	13.00	0.50
CL= 2.34	CU= 0.409	CL/CD= 5.72							

GEOMETRY MODIFICATION

11= 1234592385 12= 987682355 W1AC= 3 RCASE= 6

INCR	NUM	% STEP	DEGREE
1		3.	0.50
2		5.	1.00
3		0.10.	2.00

UPAR IN-GE. IN CS	PAR1 1	PAR2 1	PAR3 1	PAR4 1	PAR5 1	PAR6 1	PAR7 1	PAR8 1	PAR9 1
1	1.42	-0.45-26.00	0.25	0.00	13.00	-0.22	0.28	15.00	1.50
2	2.45	0.383	6.40	-1.21					
3	1.42	-0.45-26.00	0.21	0.58	13.00	-0.26	0.31	15.00	2.00
4	1.42	-0.45-26.00	0.25	0.00	13.00	-0.22	0.31	15.00	1.50
5	1.38	-0.45-26.50	0.25	0.00	13.00	-0.22	0.31	15.00	1.50
6	1.42	-0.45-26.50	0.25	0.00	13.50	-0.26	0.28	15.00	2.00
7	1.37	CU=0.368	CU/CD=3.72	CU=-0.916	CU=0.0219	CU=0.0219	CU=0.0219	CU=0.0219	CU=0.0219
8	1.42	-0.45-25.50	0.25	0.63	13.00	-0.22	0.31	15.00	1.00
9	1.42	-0.45-25.50	0.25	0.63	13.00	-0.22	0.31	15.00	1.00
10	1.38	-0.45-26.00	0.25	0.63	13.00	-0.22	0.31	15.00	1.50
11	1.42	-0.45-26.00	0.25	0.63	13.00	-0.22	0.31	15.00	1.50
12	1.42	-0.45-26.00	0.25	0.63	13.00	-0.22	0.31	15.00	1.50
13	1.42	-0.45-26.00	0.25	0.63	13.00	-0.22	0.31	15.00	1.50
14	1.42	-0.45-26.00	0.25	0.63	13.00	-0.22	0.31	15.00	1.50
15	1.42	-0.45-26.00	0.25	0.63	13.00	-0.22	0.31	15.00	1.50
16	1.42	-0.45-26.00	0.25	0.63	13.00	-0.22	0.31	15.00	1.50
17	1.42	-0.45-26.00	0.25	0.63	13.00	-0.22	0.31	15.00	1.50
18	1.42	-0.45-26.00	0.25	0.63	13.00	-0.22	0.31	15.00	1.50
19	1.42	-0.45-26.00	0.25	0.63	13.00	-0.22	0.31	15.00	1.50
20	1.42	-0.45-26.00	0.25	0.63	13.00	-0.22	0.31	15.00	1.50
21	1.42	-0.45-26.00	0.25	0.63	13.00	-0.22	0.31	15.00	1.50
22	1.42	-0.45-26.00	0.25	0.63	13.00	-0.22	0.31	15.00	1.50
23	1.42	-0.45-26.00	0.25	0.63	13.00	-0.22	0.31	15.00	1.50
24	1.42	-0.45-26.00	0.25	0.63	13.00	-0.22	0.31	15.00	1.50
25	1.42	-0.45-26.00	0.25	0.63	13.00	-0.22	0.31	15.00	1.50
26	1.42	-0.45-26.00	0.25	0.63	13.00	-0.22	0.31	15.00	1.50
27	1.42	-0.45-26.00	0.25	0.63	13.00	-0.22	0.31	15.00	1.50
28	1.42	-0.45-26.00	0.25	0.63	13.00	-0.22	0.31	15.00	1.50
29	1.42	-0.45-26.00	0.25	0.63	13.00	-0.22	0.31	15.00	1.50
30	1.42	-0.45-26.00	0.25	0.63	13.00	-0.22	0.31	15.00	1.50
31	1.42	-0.45-26.00	0.25	0.63	13.00	-0.22	0.31	15.00	1.50
32	1.42	-0.45-26.00	0.25	0.63	13.00	-0.22	0.31	15.00	1.50
33	1.42	-0.45-26.00	0.25	0.63	13.00	-0.22	0.31	15.00	1.50
34	1.42	-0.45-26.00	0.25	0.63	13.00	-0.22	0.31	15.00	1.50
35	1.42	-0.45-26.00	0.25	0.63	13.00	-0.22	0.31	15.00	1.50
36	1.42	-0.45-26.00	0.25	0.63	13.00	-0.22	0.31	15.00	1.50
37	1.42	-0.45-26.00	0.25	0.63	13.00	-0.22	0.31	15.00	1.50
38	1.42	-0.45-26.00	0.25	0.63	13.00	-0.22	0.31	15.00	1.50
39	1.42	-0.45-26.00	0.25	0.63	13.00	-0.22	0.31	15.00	1.50
40	1.42	-0.45-26.00	0.25	0.63	13.00	-0.22	0.31	15.00	1.50
41	1.42	-0.45-26.00	0.25	0.63	13.00	-0.22	0.31	15.00	1.50
42	1.42	-0.45-26.00	0.25	0.63	13.00	-0.22	0.31	15.00	1.50
43	1.42	-0.45-26.00	0.25	0.63	13.00	-0.22	0.31	15.00	1.50
44	1.42	-0.45-26.00	0.25	0.63	13.00	-0.22	0.31	15.00	1.50
45	1.42	-0.45-26.00	0.25	0.63	13.00	-0.22	0.31	15.00	1.50
46	1.42	-0.45-26.00	0.25	0.63	13.00	-0.22	0.31	15.00	1.50
47	1.42	-0.45-26.00	0.25	0.63	13.00	-0.22	0.31	15.00	1.50
48	1.42	-0.45-26.00	0.25	0.63	13.00	-0.22	0.31	15.00	1.50
49	1.42	-0.45-26.00	0.25	0.63	13.00	-0.22	0.31	15.00	1.50
50	1.42	-0.45-26.00	0.25	0.63	13.00	-0.22	0.31	15.00	1.50
51	1.42	-0.45-26.00	0.25	0.63	13.00	-0.22	0.31	15.00	1.50
52	1.42	-0.45-26.00	0.25	0.63	13.00	-0.22	0.31	15.00	1.50
53	1.42	-0.45-26.00	0.25	0.63	13.00	-0.22	0.31	15.00	1.50
54	1.42	-0.45-26.00	0.25	0.63	13.00	-0.22	0.31	15.00	1.50
55	1.42	-0.45-26.00	0.25	0.63	13.00	-0.22	0.31	15.00	1.50
56	1.42	-0.45-26.00	0.25	0.63	13.00	-0.22	0.31	15.00	1.50
57	1.42	-0.45-26.00	0.25	0.63	13.00	-0.22	0.31	15.00	1.50
58	1.42	-0.45-26.00	0.25	0.63	13.00	-0.22	0.31	15.00	1.50
59	1.42	-0.45-26.00	0.25	0.63	13.00	-0.22	0.31	15.00	1.50
60	1.42	-0.45-26.00	0.25	0.63	13.00	-0.22	0.31	15.00	1.50
61	1.42	-0.45-26.00	0.25	0.63	13.00	-0.22	0.31	15.00	1.50
62	1.42	-0.45-26.00	0.25	0.63	13.00	-0.22	0.31	15.00	1.50
63	1.42	-0.45-26.00	0.25	0.63	13.00	-0.22	0.31	15.00	1.50
64	1.42	-0.45-26.00	0.25	0.63	13.00	-0.22	0.31	15.00	1.50
65	1.42	-0.45-26.00	0.25	0.63	13.00	-0.22	0.31	15.00	1.50
66	1.42	-0.45-26.00	0.25	0.63	13.00	-0.22	0.31	15.00	1.50
67	1.42	-0.45-26.00	0.25	0.63	13.00	-0.22	0.31	15.00	1.50
68	1.42	-0.45-26.00	0.25	0.63	13.00	-0.22	0.31	15.00	1.50
69	1.42	-0.45-26.00	0.25	0.63	13.00	-0.22	0.31	15.00	1.50
70	1.42	-0.45-26.00	0.25	0.63	13.00	-0.22	0.31	15.00	1.50
71	1.42	-0.45-26.00	0.25	0.63	13.00	-0.22	0.31	15.00	1.50
72	1.42	-0.45-26.00	0.25	0.63	13.00	-0.22	0.31	15.00	1.50
73	1.42	-0.45-26.00	0.25	0.63	13.00	-0.22	0.31	15.00	1.50
74	1.42	-0.45-26.00	0.25	0.63	13.00	-0.22	0.31	15.00	1.50
75	1.42	-0.45-26.00	0.25	0.63	13.00	-0.22	0.31	15.00	1.50
76	1.42	-0.45-26.00	0.25	0.63	13.00	-0.22	0.31	15.00	1.50
77	1.42	-0.45-26.00	0.25	0.63	13.00	-0.22	0.31	15.00	1.50
78	1.42	-0.45-26.00	0.25	0.63	13.00	-0.22	0.31	15.00	1.50
79	1.42	-0.45-26.00	0.25	0.63	13.00	-0.22	0.31	15.00	1.50
80	1.42	-0.45-26.00	0.25	0.63	13.00	-0.22	0.31	15.00	1.50
81	1.42	-0.45-26.00	0.25	0.63	13.00	-0.22	0.31	15.00	1.50
82	1.42	-0.45-26.00	0.25	0.63	13.00	-0.22	0.31	15.00	1.50
83	1.42	-0.45-26.00	0.25	0.63	13.00	-0.22	0.31	15.00	1.50
84	1.42	-0.45-26.00	0.25	0.63	13.00	-0.22	0.31	15.00	1.50
85	1.42	-0.45-26.00	0.25	0.63	13.00	-0.22	0.31	15.00	1.50
86	1.42	-0.45-26.00	0.25	0.63	13.00	-0.22	0.31	15.00	1.50
87	1.42	-0.45-26.00	0.25	0.63	13.00	-0.22	0.31	15.00	1.50
88	1.42	-0.45-26.00	0.25	0.63	13.00	-0.22	0.31	15.00	1.50
89	1.42	-0.45-26.00	0.25	0.63	13.00	-0.22	0.31	15.00	1.50
90	1.42	-0.45-26.00	0.25	0.63	13.00	-0.22	0.31	15.00	1.50
91	1.42	-0.45-26.00	0.25	0.63	13.00	-0.22	0.31	15.00	1.50
92	1.42	-0.45-26.00	0.25	0.63	13.00	-0.22	0.31	15.00	1.50
93	1.42	-0.45-26.00	0.25	0.63	13.00	-0.22	0.31	15.00	1.50
94	1.42	-0.45-26.00	0.25	0.63	13.00	-0.22	0.31	15.00	1.50
95	1.42	-0.45-26.00	0.25	0.63	13.00	-0.22	0.31	15.00	1.50
96	1.42	-0.45-26.00	0.25	0.63	13.00	-0.22	0.31	15.00	1.50
97	1.42	-0.45-26.00	0.25	0.63	13.00	-0.22	0.31	15.00	1.50
98	1.42	-0.45-26.00	0.25	0.63	13.00	-0.22	0.31	15.00	1.50
99	1.42	-0.45-26.00	0.25	0.63	13.00	-0.22	0.31	15.00	1.50
100	1.42	-0.45-26.00	0.25	0.63	13.00	-0.22	0.31	15.00	1.50

GERALD R. NEWMAN b

11= 1234593710 12= 987000723 NINC= 3 NCLSE= 6

INCR. NUM	% STEP	DEGREE
1	5.00	0.25
2	10.00	0.50
3	15.00	0.75

[illegible]

1	2	1.50	-0.42	-25.00	-0.02	0.53	13.75	-0.30	0.40	15.50	1.50
		$CL = 1.03$	$CU = 0.14$	$3CU/CL = 5.34$	$CU_{\text{H}} = -0.44$						
1	3	1.42	-0.42	-25.25	-0.02	0.58	13.75	-0.30	0.40	15.75	1.25
		$CU = 0.985$	$CU_{\text{H}} = 0.180$	$3CU/CL = 5.47$	$CU_{\text{H}} = -0.416$						
1	4	1.50	-0.37	-24.75	0.00	0.58	13.25	-0.22	0.30	15.50	1.75
		$CU = 2.60$	$CU_{\text{H}} = 0.323$	$3CU/CL = 8.05$	$CU_{\text{H}} = -1.30$						
1	5	1.50	-0.37	-25.25	0.00	0.48	13.25	-0.22	0.30	15.75	1.75
		$CU = 1.44$	$CU_{\text{H}} = 0.285$	$3CU/CL = 5.05$	$CU_{\text{H}} = -0.970$						

1	(4)	1.50	-0.44	-14.15	-0.02	0.53	13.50	-0.14	0.26	15.25	1.25
		CL=2.58	CU=0.273	CL/CU=9.45	CH=-1.27						
2	1	1.21	-0.54	-25.50	-0.09	0.53	13.50	-0.07	0.21	16.00	1.53
		CL=0.786	CU=0.0815	CL/CU=9.64	CH=-0.150						
2	2	1.27	-0.44	-25.00	0.41	0.53	14.00	-0.37	0.41	15.50	1.50

2	8	0.21	-0.42	25.00	0.01	0.53	14.00	-0.37	0.44	15.50
		CU=	2.53	CU=	0.41	CU/CU=	6.14	CU=	-1.25	
2	9	1.42	-0.37	24.50	-0.09	0.53	14.00	-0.07	0.31	15.00
		CU=	0.632	CU=	0.103	CU/CU=	6.14	CU=	-0.0749	
2	10	1.51	-0.52	24.50	0.21	0.53	14.00	-0.37	0.31	15.50
		CU=	2.60	CU=	0.387	CU/CU=	6.72	CU=	-1.26	

Case	$\frac{C_1}{C_2}$	$\frac{C_1}{C_2} - 25.00$	$\frac{C_1}{C_2}$	$\frac{C_1}{C_2} - 25.00$	$\frac{C_1}{C_2}$	$\frac{C_1}{C_2} - 25.00$	$\frac{C_1}{C_2}$	$\frac{C_1}{C_2} - 25.00$	$\frac{C_1}{C_2}$	$\frac{C_1}{C_2} - 25.00$	$\frac{C_1}{C_2}$	$\frac{C_1}{C_2} - 25.00$
1	1.51	-0.42	0.06	0.53	13.50	-0.22	0.21	15.50	1.55	-0.42	0.06	0.53
2	1.27	-0.42	0.21	0.53	13.50	-0.37	0.31	15.50	1.55	-0.42	0.06	0.53
3	1.42	-0.42	0.28	0.53	13.50	-0.22	0.40	14.75	0.75	-0.42	0.06	0.53

3 13	$\text{CL} = 2.33$	$\text{CU} = 0.362$	$\text{CL/CU} = 6.44$	$\text{CH} = -1.17$	0.73
3 14	$\text{CL} = 2.72$	$\text{CU} = 0.445$	$\text{CL/CU} = 6.11$	$\text{CH} = -1.24$	2.25
3 15	$\text{CL} = 0.690$	$\text{CU} = 0.850$	$\text{CL/CU} = 0.812$	$\text{CH} = -0.0878$	1.50

[illegible]

3 18
CL = 0.508 CU = 0.149 CL/CU = 3.41 CR = -0.125
1.19 -0.42 -25.75 0.06 0.58 12.5 -0.22 0.46 15.50 1.50

2

11= 1234565947 12= 98764723 NVC= 3 10CASE= 6

INCH	NUM	STEP	DEGRTEE
1		2.50	0.13
2		5.00	0.25
4		7.50	0.38

OPAN 10 CS	PAN1 1	PAN2 1	PAN3 1	PAN4 1	PAN5 1	PAN6 1	PAN7 1	PAN8 1	PAN9 1	PAN10 1
1.50	-0.42-24.75	-0.02	0.53	13.50	-0.14	0.10	15.25	1.25		
2.58	0.273	9.45	-1.27							
1 1	1.40	-0.44-24.85	-0.02	0.53	13.50	-0.10	0.14	15.13	1.25	
	CL=1.09	CU=0.218	CL/CU=5.00	CU=-0.56	CU=0.56	CU=0.56	CU=0.56	CU=0.56	CU=0.56	CU=0.56
1 2	1.50	-0.44-24.75	-0.02	0.53	13.50	-0.10	0.14	15.30	1.30	
	CL=2.59	CU=0.285	CL/CU=9.09	CU=-1.27	CU=1.27	CU=1.27	CU=1.27	CU=1.27	CU=1.27	CU=1.27
1 3	1.50	-0.42-24.75	-0.02	0.53	13.50	-0.14	0.23	15.34	1.25	
	CL=2.59	CU=0.281	CL/CU=9.22	CU=-1.27	CU=1.27	CU=1.27	CU=1.27	CU=1.27	CU=1.27	CU=1.27
1 4	1.40	-0.42-24.75	-0.02	0.53	13.50	-0.10	0.20	15.30	1.13	
	CL=2.58	CU=0.268	CL/CU=9.63	CU=-1.27	CU=1.27	CU=1.27	CU=1.27	CU=1.27	CU=1.27	CU=1.27
1 5	1.54	-0.44-24.75	-0.02	0.53	13.35	-0.10	0.24	15.25	1.30	
	CL=0.902	CU=0.148	CL/CU=6.09	CU=-0.36	CU=0.36	CU=0.36	CU=0.36	CU=0.36	CU=0.36	CU=0.36
1 6	1.54	-0.42-24.85	-0.02	0.53	13.65	-0.14	0.20	15.25	1.30	
	CL=2.59	CU=0.268	CL/CU=8.99	CU=-1.26	CU=1.26	CU=1.26	CU=1.26	CU=1.26	CU=1.26	CU=1.26
2 7	1.42	-0.47-24.75	-0.05	0.55	13.50	-0.14	0.21	15.00	1.25	
	CL=2.53	CU=0.310	CL/CU=8.16	CU=-1.25	CU=1.25	CU=1.25	CU=1.25	CU=1.25	CU=1.25	CU=1.25
2 8	1.50	-0.42-24.75	-0.02	0.54	13.50	-0.00	0.15	15.25	1.15	
	CL=2.56	CU=0.279	CL/CU=9.15	CU=-1.26	CU=1.26	CU=1.26	CU=1.26	CU=1.26	CU=1.26	CU=1.26
2 9	1.50	-0.42-24.75	-0.10	0.50	13.25	-0.14	0.21	15.25	1.25	
	CL=0.749	CU=0.0446	CL/CU=16.80	CU=-0.162	CU=0.162	CU=0.162	CU=0.162	CU=0.162	CU=0.162	CU=0.162
3 10	1.50	-0.37-24.75	-0.02	0.48	13.75	-0.14	0.21	15.25	1.25	
	CL=2.65	CU=0.245	CL/CU=10.82	CU=-1.28	CU=1.28	CU=1.28	CU=1.28	CU=1.28	CU=1.28	CU=1.28
3 11	1.50	-0.42-24.75	-0.06	0.53	13.50	-0.14	0.21	15.25	1.25	
	CL=2.51	CU=0.282	CL/CU=8.90	CU=-1.24	CU=1.24	CU=1.24	CU=1.24	CU=1.24	CU=1.24	CU=1.24
3 12	1.50	-0.37-24.75	-0.10	0.53	13.45	-0.06	0.31	15.50	1.15	
	CL=1.09	CU=0.213	CL/CU=5.12	CU=-0.573	CU=0.573	CU=0.573	CU=0.573	CU=0.573	CU=0.573	CU=0.573
3 13	1.39	-0.49-24.75	-0.02	0.60	13.13	-0.25	0.19	15.25	1.25	
	CL=0.728	CU=0.0518	CL/CU=1.40	CU=-0.226	CU=0.226	CU=0.226	CU=0.226	CU=0.226	CU=0.226	CU=0.226
3 14	1.50	-0.47-24.30	0.09	0.53	13.13	-0.03	0.20	15.25	0.80	
	CL=1.25	CU=0.191	CL/CU=6.65	CU=-0.555	CU=0.555	CU=0.555	CU=0.555	CU=0.555	CU=0.555	CU=0.555
3 15	1.39	-0.42-24.75	-0.02	0.53	13.50	-0.14	0.20	15.25	1.15	
	CL=2.57	CU=0.283	CL/CU=9.08	CU=-1.27	CU=1.27	CU=1.27	CU=1.27	CU=1.27	CU=1.27	CU=1.27
3 16	1.39	-0.34-25.13	-0.02	0.53	13.50	-0.25	0.19	15.63	1.15	
	CL=0.976	CU=0.488	CL/CU=2.00	CU=-0.242	CU=0.242	CU=0.242	CU=0.242	CU=0.242	CU=0.242	CU=0.242
3 17	1.50	-0.42-24.30	0.09	0.45	13.50	-0.14	0.33	15.25	1.25	
	CL=2.61	CU=0.287	CL/CU=9.09	CU=-1.24	CU=1.24	CU=1.24	CU=1.24	CU=1.24	CU=1.24	CU=1.24
3 18	1.50	-0.42-24.38	-0.02	0.53	13.13	-0.14	0.33	14.88	1.15	
	CL=0.828	CU=-0.0538	CL/CU=15.29	CU=-0.412	CU=0.412	CU=0.412	CU=0.412	CU=0.412	CU=0.412	CU=0.412

GEOMETRY MULTIPLICATION

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11= 1234580320 12= 487030883 11AC= 3 NCASE= 6
```

PACK NUM	% STEP	DEGREE
1	2.50	0.13
2	5.00	0.25
3	7.50	0.38

UPPER 10. CS	PAK1 1	PAK2 1	PAK3 1	PAK4 1	PAK5 1	PAK6 1	PAK7 1	PAK8 1	PAK10 1
1.50	-0.37-24.75	-0.02	1	0.48	13.75	-0.14	0.21	15.25	1.25
2.65	CU= 0.245	10.82	-1.28						
1.02	-0.37-24.75	-0.00	1	0.48	13.75	-0.18	0.18	15.38	1.30
CU= 0.967	CU= 1.03	CL/CU= 0.939	CU= -0.415						
1.54	-0.37-24.75	-0.02	1	0.45	13.75	-0.14	0.18	15.38	1.25
CU= 1.43	CU= 0.273	CL/CU= 5.24	CU= -0.925						
1.58	-0.40-24.83	-0.02	1	0.50	13.75	-0.14	0.18	15.13	1.13
CU= 1.83	CU= 0.465	CL/CU= 3.94	CU= -1.50						
1.54	-0.34-24.75	-0.02	1	0.45	13.75	-0.18	0.21	15.25	1.13
CU= 1.17	CU= 0.691	CL/CU= 1.69	CU= -0.650						
1.02	-0.40-24.88	-0.00	1	0.50	13.88	-0.18	0.18	15.13	1.30
CU=	CU=	CL/CU=	CU=						
1.54	-0.40-24.83	-0.00	1	0.48	13.75	-0.14	0.18	15.13	1.13
CU= 0.722	CU= 0.049	CL/CU= 48.5	CU= -0.145						
1.00	-0.37-24.50	-0.10	1	0.48	13.75	-0.14	0.16	15.00	1.00
CU= 2.64	CU= 0.213	CL/CU= 12.4	CU= -1.29						
1.54	-0.37-25.00	-0.00	1	0.48	13.75	-0.06	0.26	15.25	1.55
CU= 2.63	CU= 0.247	CL/CU= 9.49	CU= -1.25						
1.06	-0.37-24.75	-0.02	1	0.53	14.00	-0.22	0.21	15.25	1.30
CU= 1.07	CU= 0.600	CL/CU= 1.62	CU= -0.404						
1.00	-0.32-25.00	-0.02	1	0.53	13.75	-0.06	0.21	15.25	1.25
CU= 2.61	CU= 0.246	CL/CU= 10.6	CU= -1.26						
1.50	-0.32-24.75	-0.00	1	0.43	13.75	-0.14	0.21	15.25	1.05
CU=	CU=	CL/CU=	CU=						
1.50	-0.37-25.00	-0.10	1	0.48	13.75	-0.22	0.26	15.50	1.50
CU= 1.34	CU= 0.519	CL/CU= 2.58	CU= -0.853						
1.69	-0.37-24.75	-0.07	1	0.48	14.13	-0.25	0.21	15.63	0.88
CU= 2.65	CU= 0.249	CL/CU= 10.6	CU= -1.30						
1.09	-0.44-24.75	-0.13	1	0.41	13.38	-0.14	0.28	15.25	0.90
CU=	CU=	CL/CU=	CU=						
1.09	-0.37-24.75	-0.02	1	0.48	13.75	-0.25	0.21	15.25	0.90
CU=	CU=	CL/CU=	CU=						
1.47	-0.37-24.38	-0.02	1	0.56	13.75	-0.03	0.21	15.25	1.25
CU= 1.16	CU= 0.207	CL/CU= 5.60	CU= -0.407						
1.09	-0.30-24.38	-0.09	1	0.41	13.75	-0.25	0.21	14.88	1.25
CU= 0.930	CU= 0.254	CL/CU= 3.66	CU= -0.290						
1.47	-0.37-24.38	-0.13	1	0.46	13.38	-0.25	0.21	15.25	1.25
CU= 1.17	CU= 0.220	CL/CU= 5.32	CU= -0.488						

GEOMETRY MULTIPLICATION 19

11= 12345673 12= 987654321 NINC= 3 NCASE= 6

LOCK NUM % STEP DEGREE
1 2.50 3.75 0.400
2 7.50 11.25 0.600

GEAR	PAIR1	PAIR2	PAIR3	PAIR4	PAIR5	PAIR6	PAIR7	PAIR8	PAIR9
1 1	1.77	-0.44-24.13	0.01	0.41	13.75	-0.03	0.09	15.00	1.36
1 1	2.71	0.228	11.9	-1.28					
1 1	1.77	-0.44-24.13	0.01	0.41	13.75	-0.03	0.09	14.80	1.36
1 2	1.71	-0.40-23.93	0.07	0.41	13.75	-0.09	0.09	14.80	1.36
1 3	1.77	-0.44-24.13	0.01	0.41	13.75	-0.09	0.09	15.00	1.36
1 4	1.71	-0.40-23.93	0.07	0.41	13.75	-0.03	0.09	15.20	1.56
1 5	1.77	-0.44-24.13	0.01	0.41	13.75	-0.03	0.13	15.00	1.18
1 6	1.71	-0.40-23.93	0.07	0.41	13.75	-0.03	0.13	15.00	1.58
2 7	1.77	-0.44-24.13	0.01	0.41	13.75	-0.14	0.02	15.00	1.78
2 8	1.71	-0.40-23.93	0.07	0.41	13.75	-0.14	0.17	15.40	1.38
2 9	1.77	-0.44-24.13	0.01	0.41	13.75	-0.03	0.09	14.60	1.38
2 10	1.71	-0.40-23.93	0.07	0.41	13.75	-0.03	0.09	15.00	1.38
2 11	1.77	-0.44-24.13	0.01	0.41	13.75	-0.03	0.09	15.00	1.36
2 12	1.71	-0.40-23.93	0.07	0.41	13.75	-0.14	0.02	15.00	1.38
2 13	1.77	-0.44-24.13	0.01	0.41	13.75	-0.03	0.09	15.60	0.78
2 14	1.71	-0.40-23.93	0.07	0.41	13.75	-0.03	-0.02	15.00	1.38
3 15	1.77	-0.44-24.13	0.01	0.41	13.75	-0.03	0.09	15.60	1.38
3 16	1.71	-0.40-23.93	0.07	0.41	13.75	-0.03	0.09	15.00	0.76
3 17	1.77	-0.44-24.13	0.01	0.41	13.75	-0.03	-0.02	14.40	1.38

GEOMETRY MULTIPLICATION 9

11= 12345673 12= 987654321 NINC= 3 NCASE= 6

LOCK NUM % STEP DEGREE
1 2.50 3.75 0.400
2 7.50 11.25 0.600

GEAR	PAIR1	PAIR2	PAIR3	PAIR4	PAIR5	PAIR6	PAIR7	PAIR8	PAIR9
1 1	1.77	-0.44-24.13	0.01	0.41	13.75	-0.03	0.09	15.00	1.36
1 1	2.71	0.228	11.9	-1.28					
1 1	1.77	-0.44-24.13	0.01	0.41	13.75	-0.03	0.09	14.80	1.36
1 2	1.71	-0.40-23.93	0.07	0.41	13.75	-0.09	0.09	14.80	1.36
1 3	1.77	-0.44-24.13	0.01	0.41	13.75	-0.09	0.09	15.00	1.36
1 4	1.71	-0.40-23.93	0.07	0.41	13.75	-0.03	0.09	15.20	1.56
1 5	1.77	-0.44-24.13	0.01	0.41	13.75	-0.03	0.13	15.00	1.18
1 6	1.71	-0.40-23.93	0.07	0.41	13.75	-0.03	0.13	15.00	1.58
2 7	1.77	-0.44-24.13	0.01	0.41	13.75	-0.14	0.02	15.00	1.78
2 8	1.71	-0.40-23.93	0.07	0.41	13.75	-0.14	0.17	15.40	1.38
2 9	1.77	-0.44-24.13	0.01	0.41	13.75	-0.03	0.09	14.60	1.38
2 10	1.71	-0.40-23.93	0.07	0.41	13.75	-0.03	0.09	15.00	1.38
2 11	1.77	-0.44-24.13	0.01	0.41	13.75	-0.03	0.09	15.00	1.36
2 12	1.71	-0.40-23.93	0.07	0.41	13.75	-0.14	0.02	15.00	1.38
2 13	1.77	-0.44-24.13	0.01	0.41	13.75	-0.03	0.09	15.60	0.78
2 14	1.71	-0.40-23.93	0.07	0.41	13.75	-0.03	-0.02	15.00	1.38
3 15	1.77	-0.44-24.13	0.01	0.41	13.75	-0.03	0.09	15.60	1.38
3 16	1.71	-0.40-23.93	0.07	0.41	13.75	-0.03	0.09	15.00	0.76
3 17	1.77	-0.44-24.13	0.01	0.41	13.75	-0.03	-0.02	14.40	1.38

GEOMETRY MODIFICATION 11

11= 123455927 12= 987652413 MINC= 3 NCASE= 6

INCH NUM # STEP DEGREE
1 1 5.00 0.500
2 2 11.25 0.500
3 3 16.50 0.500

PAR1	PAR2	PAR3	PAR4	PAR5	PAR6	PAR7	PAR8	PAR9	PAR10
1.77	-0.44-24.13	0.01	0.01	0.30	13.75	-0.03	0.09	15.00	0.78
2.70	0.203	12.9	-1.26						
1 1	1.09	-0.50-24.13	0.07	0.30	13.75	-0.03	0.09	15.00	1.08
	CU= 2.57	CU= 0.250	CL/CU= 10.4	CU= -1.23					
1 2	1.09	-0.50-24.13	0.07	0.30	13.75	-0.03	0.09	15.00	0.78
	CU= 2.57	CU= 0.250	CL/CU= 10.4	CU= -1.23					
1 4	1.77	-0.50-24.13	0.01	0.30	13.75	-0.03	0.09	15.00	1.08
	CU= 2.57	CU= 0.250	CL/CU= 10.4	CU= -1.23					
1 5	1.77	-0.50-24.13	0.01	0.30	13.75	-0.03	0.09	15.00	0.78
	CU= 2.57	CU= 0.250	CL/CU= 10.4	CU= -1.23					
1 6	1.77	-0.50-24.13	0.01	0.30	13.75	-0.03	0.09	15.00	0.78
	CU= 2.57	CU= 0.250	CL/CU= 10.4	CU= -1.23					
2 1	1.77	-0.50-24.13	0.01	0.30	13.75	-0.03	0.09	15.00	0.78
	CU= 2.57	CU= 0.250	CL/CU= 10.4	CU= -1.23					
2 8	1.77	-0.50-24.13	0.01	0.30	13.75	-0.03	0.09	15.00	0.78
	CU= 2.57	CU= 0.250	CL/CU= 10.4	CU= -1.23					
2 9	1.77	-0.50-24.13	0.01	0.30	13.75	-0.03	0.09	15.00	0.78
	CU= 2.57	CU= 0.250	CL/CU= 10.4	CU= -1.23					
2 10	1.77	-0.50-24.13	0.01	0.30	13.75	-0.03	0.09	15.00	0.78
	CU= 2.57	CU= 0.250	CL/CU= 10.4	CU= -1.23					
2 11	1.77	-0.50-24.13	0.01	0.30	13.75	-0.03	0.09	15.00	0.78
	CU= 2.57	CU= 0.250	CL/CU= 10.4	CU= -1.23					
2 12	1.77	-0.50-24.13	0.01	0.30	13.75	-0.03	0.09	15.00	0.78
	CU= 2.57	CU= 0.250	CL/CU= 10.4	CU= -1.23					
3 13	1.77	-0.50-24.13	0.01	0.30	13.75	-0.03	0.09	15.00	0.78
	CU= 2.57	CU= 0.250	CL/CU= 10.4	CU= -1.23					
3 14	1.77	-0.50-24.13	0.01	0.30	13.75	-0.03	0.09	15.00	0.78
	CU= 2.57	CU= 0.250	CL/CU= 10.4	CU= -1.23					
3 15	1.77	-0.50-24.13	0.01	0.30	13.75	-0.03	0.09	15.00	0.78
	CU= 2.57	CU= 0.250	CL/CU= 10.4	CU= -1.23					
3 16	1.77	-0.50-24.13	0.01	0.30	13.75	-0.03	0.09	15.00	0.78
	CU= 2.57	CU= 0.250	CL/CU= 10.4	CU= -1.23					

GEOMETRY MODIFICATION 12

11= 1234559170 12= 987653643 MINC= 3 NCASE= 6

INCH NUM # STEP DEGREE
1 1 5.00 0.500
2 2 11.25 0.500
3 3 16.50 0.500

PAR1	PAR2	PAR3	PAR4	PAR5	PAR6	PAR7	PAR8	PAR9	PAR10
1.77	-0.44-24.13	0.01	0.01	0.30	13.75	-0.03	0.09	15.00	0.78
2.70	0.182	14.8	-1.28						
1 1	1.09	-0.50-24.13	0.07	0.30	13.75	-0.11	0.09	15.30	1.08
	CU= 2.74	CU= 0.436	CL/CU= 6.28	CU= -1.32					
1 2	1.09	-0.50-24.13	0.07	0.30	13.75	-0.05	0.09	15.30	0.78
	CU= 2.74	CU= 0.436	CL/CU= 6.28	CU= -1.32					
1 3	1.09	-0.50-24.13	0.01	0.30	13.75	-0.11	0.09	15.30	0.78
	CU= 2.74	CU= 0.436	CL/CU= 6.28	CU= -1.32					
1 4	1.09	-0.50-24.13	0.01	0.30	13.75	-0.05	0.09	15.30	0.78
	CU= 2.74	CU= 0.436	CL/CU= 6.28	CU= -1.32					
1 5	1.09	-0.50-24.13	0.01	0.30	13.75	-0.05	0.09	15.30	0.78
	CU= 2.74	CU= 0.436	CL/CU= 6.28	CU= -1.32					
1 6	1.09	-0.50-24.13	0.01	0.30	13.75	-0.05	0.09	15.30	0.78
	CU= 2.74	CU= 0.436	CL/CU= 6.28	CU= -1.32					
2 1	1.09	-0.50-24.13	0.01	0.30	13.75	-0.05	0.09	15.30	0.78
	CU= 2.74	CU= 0.436	CL/CU= 6.28	CU= -1.32					
2 8	1.09	-0.50-24.13	0.01	0.30	13.75	-0.05	0.09	15.30	0.78
	CU= 2.74	CU= 0.436	CL/CU= 6.28	CU= -1.32					
2 9	1.09	-0.50-24.13	0.01	0.30	13.75	-0.05	0.09	15.30	0.78
	CU= 2.74	CU= 0.436	CL/CU= 6.28	CU= -1.32					
2 10	1.09	-0.50-24.13	0.01	0.30	13.75	-0.05	0.09	15.30	0.78
	CU= 2.74	CU= 0.436	CL/CU= 6.28	CU= -1.32					
2 11	1.09	-0.50-24.13	0.01	0.30	13.75	-0.05	0.09	15.30	0.78
	CU= 2.74	CU= 0.436	CL/CU= 6.28	CU= -1.32					
2 12	1.09	-0.50-24.13	0.01	0.30	13.75	-0.05	0.09	15.30	0.78
	CU= 2.74	CU= 0.436	CL/CU= 6.28	CU= -1.32					
3 13	1.09	-0.50-24.13	0.01	0.30	13.75	-0.05	0.09	15.30	0.78
	CU= 2.74	CU= 0.436	CL/CU= 6.28	CU= -1.32					
3 14	1.09	-0.50-24.13	0.01	0.30	13.75	-0.05	0.09	15.30	0.78
	CU= 2.74	CU= 0.436	CL/CU= 6.28	CU= -1.32					
3 15	1.09	-0.50-24.13	0.01	0.30	13.75	-0.05	0.09	15.30	0.78
	CU= 2.74	CU= 0.436	CL/CU= 6.28	CU= -1.32					
3 16	1.09	-0.50-24.13	0.01	0.30	13.75	-0.05	0.09	15.30	0.78
	CU= 2.74	CU= 0.436	CL/CU= 6.28	CU= -1.32					

100-10689-10

11 = 1,454,254 12 = 987008531 13.14C = 3 14.5B = 0

[illegible]

UPAR 11-06. IR. CS.	P4P1	P4P2	P4P3	P4P4	P4P5	P4P6	P4P7	P4P8	P4P9	P4P10
1 0	1.64	-1.64	-24.13	0.01	0.30	14.05	-0.02	0.05	15.30	0.40
1 1	2.68	0.170	15.6	-1.29						
1 2	1.64	-0.44	-24.13	0.01	0.30	14.05	-0.02	0.05	15.30	0.40
1 3	2.68	0.171	15.7	-1.29						
1 4	1.64	-0.44	-24.13	0.01	0.30	14.05	-0.02	0.05	15.30	0.40
1 5	2.68	0.170	15.7	-1.29						
1 6	1.64	-0.44	-24.13	0.01	0.30	14.05	-0.02	0.05	15.30	0.40
1 7	2.68	0.170	15.7	-1.29						
1 8	1.64	-0.44	-24.13	0.01	0.30	14.05	-0.02	0.05	15.30	0.40
1 9	2.68	0.170	15.7	-1.29						
1 10	1.64	-0.44	-24.13	0.01	0.30	14.05	-0.02	0.05	15.30	0.40
1 11	2.68	0.170	15.7	-1.29						
1 12	1.64	-0.44	-24.13	0.01	0.30	14.05	-0.02	0.05	15.30	0.40
1 13	2.68	0.170	15.7	-1.29						
1 14	1.64	-0.44	-24.13	0.01	0.30	14.05	-0.02	0.05	15.30	0.40
1 15	2.68	0.170	15.7	-1.29						
1 16	1.64	-0.44	-24.13	0.01	0.30	14.05	-0.02	0.05	15.30	0.40
1 17	2.68	0.170	15.7	-1.29						
1 18	1.64	-0.44	-24.13	0.01	0.30	14.05	-0.02	0.05	15.30	0.40
1 19	2.68	0.170	15.7	-1.29						
1 20	1.64	-0.44	-24.13	0.01	0.30	14.05	-0.02	0.05	15.30	0.40
1 21	2.68	0.170	15.7	-1.29						
1 22	1.64	-0.44	-24.13	0.01	0.30	14.05	-0.02	0.05	15.30	0.40
1 23	2.68	0.170	15.7	-1.29						
1 24	1.64	-0.44	-24.13	0.01	0.30	14.05	-0.02	0.05	15.30	0.40
1 25	2.68	0.170	15.7	-1.29						
1 26	1.64	-0.44	-24.13	0.01	0.30	14.05	-0.02	0.05	15.30	0.40
1 27	2.68	0.170	15.7	-1.29						
1 28	1.64	-0.44	-24.13	0.01	0.30	14.05	-0.02	0.05	15.30	0.40
1 29	2.68	0.170	15.7	-1.29						
1 30	1.64	-0.44	-24.13	0.01	0.30	14.05	-0.02	0.05	15.30	0.40
1 31	2.68	0.170	15.7	-1.29						
1 32	1.64	-0.44	-24.13	0.01	0.30	14.05	-0.02	0.05	15.30	0.40
1 33	2.68	0.170	15.7	-1.29						
1 34	1.64	-0.44	-24.13	0.01	0.30	14.05	-0.02	0.05	15.30	0.40
1 35	2.68	0.170	15.7	-1.29						
1 36	1.64	-0.44	-24.13	0.01	0.30	14.05	-0.02	0.05	15.30	0.40
1 37	2.68	0.170	15.7	-1.29						
1 38	1.64	-0.44	-24.13	0.01	0.30	14.05	-0.02	0.05	15.30	0.40
1 39	2.68	0.170	15.7	-1.29						
1 40	1.64	-0.44	-24.13	0.01	0.30	14.05	-0.02	0.05	15.30	0.40
1 41	2.68	0.170	15.7	-1.29						
1 42	1.64	-0.44	-24.13	0.01	0.30	14.05	-0.02	0.05	15.30	0.40
1 43	2.68	0.170	15.7	-1.29						
1 44	1.64	-0.44	-24.13	0.01	0.30	14.05	-0.02	0.05	15.30	0.40
1 45	2.68	0.170	15.7	-1.29						
1 46	1.64	-0.44	-24.13	0.01	0.30	14.05	-0.02	0.05	15.30	0.40
1 47	2.68	0.170	15.7	-1.29						
1 48	1.64	-0.44	-24.13	0.01	0.30	14.05	-0.02	0.05	15.30	0.40
1 49	2.68	0.170	15.7	-1.29						
1 50	1.64	-0.44	-24.13	0.01	0.30	14.05	-0.02	0.05	15.30	0.40
1 51	2.68	0.170	15.7	-1.29						
1 52	1.64	-0.44	-24.13	0.01	0.30	14.05	-0.02	0.05	15.30	0.40
1 53	2.68	0.170	15.7	-1.29						
1 54	1.64	-0.44	-24.13	0.01	0.30	14.05	-0.02	0.05	15.30	0.40
1 55	2.68	0.170	15.7	-1.29						
1 56	1.64	-0.44	-24.13	0.01	0.30	14.05	-0.02	0.05	15.30	0.40
1 57	2.68	0.170	15.7	-1.29						
1 58	1.64	-0.44	-24.13	0.01	0.30	14.05	-0.02	0.05	15.30	0.40
1 59	2.68	0.170	15.7	-1.29						
1 60	1.64	-0.44	-24.13	0.01	0.30	14.05	-0.02	0.05	15.30	0.40
1 61	2.68	0.170	15.7	-1.29						
1 62	1.64	-0.44	-24.13	0.01	0.30	14.05	-0.02	0.05	15.30	0.40
1 63	2.68	0.170	15.7	-1.29						
1 64	1.64	-0.44	-24.13	0.01	0.30	14.05	-0.02	0.05	15.30	0.40
1 65	2.68	0.170	15.7	-1.29						
1 66	1.64	-0.44	-24.13	0.01	0.30	14.05	-0.02	0.05	15.30	0.40
1 67	2.68	0.170	15.7	-1.29						
1 68	1.64	-0.44	-24.13	0.01	0.30	14.05	-0.02	0.05	15.30	0.40
1 69	2.68	0.170	15.7	-1.29						
1 70	1.64	-0.44	-24.13	0.01	0.30	14.05	-0.02	0.05	15.30	0.40
1 71	2.68	0.170	15.7	-1.29						
1 72	1.64	-0.44	-24.13	0.01	0.30	14.05	-0.02	0.05	15.30	0.40
1 73	2.68	0.170	15.7	-1.29						
1 74	1.64	-0.44	-24.13	0.01	0.30	14.05	-0.02	0.05	15.30	0.40
1 75	2.68	0.170	15.7	-1.29						
1 76	1.64	-0.44	-24.13	0.01	0.30	14.05	-0.02	0.05	15.30	0.40
1 77	2.68	0.170	15.7	-1.29						
1 78	1.64	-0.44	-24.13	0.01	0.30	14.05	-0.02	0.05	15.30	0.40
1 79	2.68	0.170	15.7	-1.29						
1 80	1.64	-0.44	-24.13	0.01	0.30	14.05	-0.02	0.05	15.30	0.40
1 81	2.68	0.170	15.7	-1.29						
1 82	1.64	-0.44	-24.13	0.01	0.30	14.05	-0.02	0.05	15.30	0.40
1 83	2.68	0.170	15.7	-1.29						
1 84	1.64	-0.44	-24.13	0.01	0.30	14.05	-0.02	0.05	15.30	0.40
1 85	2.68	0.170	15.7	-1.29						
1 86	1.64	-0.44	-24.13	0.01	0.30	14.05	-0.02	0.05	15.30	0.40
1 87	2.68	0.170	15.7	-1.29						
1 88	1.64	-0.44	-24.13	0.01	0.30	14.05	-0.02	0.05	15.30	0.40
1 89	2.68	0.170	15.7	-1.29						
1 90	1.64	-0.44	-24.13	0.01	0.30	14.05	-0.02	0.05	15.30	0.40
1 91	2.68	0.170	15.7	-1.29						
1 92	1.64	-0.44	-24.13	0.01	0.30	14.05	-0.02	0.05	15.30	0.40
1 93	2.68	0.170	15.7	-1.29						
1 94	1.64	-0.44	-24.13	0.01	0.30	14.05	-0.02	0.05	15.30	0.40
1 95	2.68	0.170	15.7	-1.29						
1 96	1.64	-0.44	-24.13	0.01	0.30	14.05	-0.02	0.05	15.30	0.40
1 97	2.68	0.170	15.7	-1.29						
1 98	1.64	-0.44	-24.13	0.01	0.30	14.05	-0.02	0.05	15.30	0.40
1 99	2.68	0.170	15.7	-1.29						
1 100	1.64	-0.44	-24.13	0.01	0.30	14.05	-0.02	0.05	15.30	0.40

GEOMETRIC MODIFICATION 15

J1= 123456789 J2= 987654321 NINC= 3 NCASE= 6

BACK NUM 4 STEP DEGREE
1 0.70
2 1.40
3 2.10

UPAR IN CS	PAR1	PAR2	PAR3	PAR4	PAR5	PAR6	PAR7	PAR8	PAR9	PAR10
1 1	1.67	-0.44-24.28	-0.05	0.26	13.90	-0.05	0.00	15.30	0.56	
1 1	1.67	-0.45-24.32	-0.04	0.27	13.94	-0.05	0.00	15.30	0.52	
1 2	1.67	-0.44-24.32	-0.05	0.26	13.90	-0.05	0.00	15.30	0.52	
1 1	1.67	-0.45-24.32	-0.04	0.27	13.94	-0.05	0.00	15.30	0.52	
1 4	1.67	-0.43-24.32	-0.05	0.26	13.90	-0.05	0.00	15.34	0.56	
1 1	1.67	-0.44-24.28	-0.05	0.26	13.90	-0.05	0.00	15.34	0.56	
1 0	1.67	-0.45-24.28	-0.04	0.26	13.90	-0.05	0.00	15.30	0.56	
1 1	1.67	-0.44-24.28	-0.05	0.26	13.90	-0.05	0.00	15.22	0.56	
1 1	1.67	-0.44-24.28	-0.05	0.26	13.90	-0.05	0.00	15.22	0.48	
1 1	1.67	-0.44-24.28	-0.05	0.26	13.90	-0.05	0.00	15.30	0.48	
2 11	1.67	-0.45-24.28	-0.04	0.26	13.90	-0.05	0.00	15.22	0.48	
2 12	1.67	-0.44-24.28	-0.05	0.26	13.90	-0.05	0.00	15.22	0.48	
2 13	1.67	-0.44-24.28	-0.05	0.26	13.90	-0.05	0.00	15.22	0.48	
3 14	1.67	-0.44-24.28	-0.05	0.26	13.90	-0.05	0.00	15.18	0.44	
3 15	1.67	-0.44-24.28	-0.05	0.26	13.90	-0.05	0.00	15.18	0.68	
3 16	1.67	-0.44-24.28	-0.05	0.26	13.90	-0.05	0.00	15.18	0.56	
3 17	1.67	-0.44-24.28	-0.05	0.26	13.90	-0.05	0.00	15.18	0.68	
3 18	1.67	-0.44-24.28	-0.05	0.26	13.90	-0.05	0.00	15.18	0.56	

GEOMETRIC MODIFICATION 16

J1= 123456789 J2= 987654321 NINC= 3 NCASE= 6

BACK NUM 4 STEP DEGREE
1 0.70
2 1.40
3 2.10

UPAR IN CS	PAR1	PAR2	PAR3	PAR4	PAR5	PAR6	PAR7	PAR8	PAR9	PAR10
1 1	1.67	-0.44-24.28	-0.05	0.26	13.90	-0.05	0.00	15.22	0.48	
1 1	1.67	-0.45-24.28	-0.04	0.26	13.94	-0.05	0.00	15.22	0.52	
1 2	1.67	-0.44-24.32	-0.05	0.26	13.90	-0.05	0.00	15.22	0.52	
1 1	1.67	-0.45-24.32	-0.04	0.26	13.94	-0.05	0.00	15.22	0.52	
1 1	1.67	-0.43-24.28	-0.05	0.26	13.90	-0.05	0.00	15.22	0.48	
1 1	1.67	-0.44-24.28	-0.05	0.26	13.90	-0.05	0.00	15.22	0.52	
1 0	1.67	-0.45-24.28	-0.04	0.26	13.90	-0.05	0.00	15.22	0.48	
1 1	1.67	-0.44-24.28	-0.05	0.26	13.90	-0.05	0.00	15.22	0.56	
1 1	1.67	-0.43-24.28	-0.05	0.26	13.90	-0.05	0.00	15.22	0.56	
1 1	1.67	-0.44-24.28	-0.05	0.26	13.90	-0.05	0.00	15.22	0.48	
1 1	1.67	-0.44-24.28	-0.05	0.26	13.90	-0.05	0.00	15.22	0.48	
2 11	1.67	-0.45-24.28	-0.04	0.26	13.90	-0.05	0.00	15.22	0.48	
2 12	1.67	-0.44-24.28	-0.05	0.26	13.90	-0.05	0.00	15.14	0.40	
2 13	1.67	-0.44-24.28	-0.05	0.26	13.90	-0.05	0.00	15.22	0.48	
3 14	1.67	-0.44-24.28	-0.05	0.26	13.90	-0.05	0.00	15.22	0.60	
3 15	1.67	-0.44-24.28	-0.05	0.26	13.90	-0.05	0.00	15.22	0.36	
3 16	1.67	-0.44-24.28	-0.05	0.26	13.90	-0.05	0.00	15.34	0.48	
3 17	1.67	-0.44-24.28	-0.05	0.26	13.90	-0.05	0.00	15.22	0.60	
3 18	1.67	-0.44-24.28	-0.05	0.26	13.90	-0.05	0.00	15.22	0.36	

GEORGE J. RYAN MULTIMEDIA COLLECTION 17

11= 174547542 12= 987665801 NINC= 3 NCASI= 6

BACK 1:6M 3 51E.P DTGKLF

[illegible]

QUAM IN-CE- FUS	PAR1 1	PAR2 1	PAR3 1	PAR4 1	PAR5 1	PAR6 1	PAR7 1	PAR8 1	PAR9 1
	1.67	-0.42-24.28	-0.05	0.70	13.78	-0.07	0.00	15.22	0.60
	2.738	0.141	19.42	-1.328					
1 1	1.67	-0.41-24.24	-0.03	0.70	13.78	-0.07	0.00	15.22	0.60
	CL=2.732	CU=0.141	CL/CU=19.38	CF=-1.318					
1 2	1.67	-0.43-24.22	-0.07	0.72	13.64	-0.05	0.01	15.22	0.60
	CL=	CU=	CL/CU=						
1 3	1.67	-0.42-24.28	-0.03	0.70	13.84	-0.07	0.00	15.22	0.54
	CL=	CU=	CL/CU=						
1 4	1.65	-0.42-24.28	-0.05	0.75	13.78	-0.05	0.01	15.22	0.54
	CL=	CU=	CL/CU=						
1 5	1.67	-0.43-24.27	-0.05	0.70	13.78	-0.07	0.00	15.16	0.60
	CL=2.754	CU=0.144	CL/CU=19.125	CF=-1.24					
1 6	1.67	-0.41-24.28	-0.07	0.70	13.78	-0.07	0.00	15.22	0.60
	CL=	CU=	CL/CU=						
2 7	1.67	-0.34-24.28	-0.08	0.70	13.60	-0.10	0.00	15.22	0.48
	CL=2.699	CU=0.133	CL/CU=20.29	CF=-1.318					
2 8	1.67	-0.41-24.10	-0.45	0.70	13.78	-0.10	0.00	15.34	0.72
	CL=2.726	CU=0.147	CL/CU=18.61	CF=-1.316					
2 9	1.66	-0.34-24.16	-0.04	0.74	13.66	-0.04	0.02	15.22	0.72
	CL=2.743	CU=0.140	CL/CU=	CF=-1.321					
2 10	1.70	-0.40-24.28	-0.05	0.75	13.78	-0.10	-0.02	15.34	0.60
	CL=2.742	CU=0.140	CL/CU=19.59	CF=-1.321					
2 11	1.67	-0.42-24.10	-0.45	0.70	13.78	-0.10	0.00	15.22	0.72
	CL=2.770	CU=0.146	CL/CU=18.72	CF=-1.327					
2 12	1.67	-0.40-24.16	-0.05	0.70	13.78	-0.10	0.02	15.10	0.46
	CL=	CU=	CL/CU=						
3 13	1.67	-0.42-24.28	-0.05	0.70	13.78	-0.12	-0.03	15.04	0.78
	CL=	CU=	CL/CU=						
3 14	1.67	-0.42-24.26	0.00	0.70	13.78	-0.07	0.00	15.40	0.42
	CL=2.717	CU=0.144	CL/CU=16.87	CF=-1.319					
3 15	1.67	-0.42-24.46	-0.10	0.70	13.78	-0.02	0.00	15.22	0.78
	CL=2.755	CU=0.145	CL/CU=19.00	CF=-1.324					
3 16	1.67	-0.45-24.46	-0.05	0.70	13.78	-0.07	-0.03	15.22	0.60
	CL=	CU=	CL/CU=						
3 17	1.62	-0.42-24.28	-0.10	0.75	13.06	-0.12	0.00	15.04	0.42
	CL=	CU=	CL/CU=						
3 18	1.67	-0.42-24.46	-0.05	0.70	13.78	-0.12	0.03	15.04	0.60
	CL=	CU=	CL/CU=						

GEOMETRY MULTPLICATION

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11= 1234508993 12= 987060051 H10C= 3 NCASL= 6
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INCR	NUM	%	STEP	DEGREE
1			1.05	0.000
2			2.10	0.120
3			3.15	0.160

PARAM	PAN1	PAN2	PAN3	PAN4	PAN5	PAN6	PAN7	PAN8	PAN9	PAN10
1st Gr.	1	1	1	1	1	1	1	1	1	1
1st CS	2	6	9	0	13	3	20	2	9	-1
1	1.07	-0.44-24.72	-0.10	0.20	13.66	-0.10	0.00	15.22	0.46	
1	1.07	-0.43-24.72	-0.10	0.21	13.72	-0.10	0.01	15.22	0.48	
1	1.05	-0.44-24.72	-0.10	0.20	13.66	-0.08	0.00	15.22	0.54	
1	1.07	-0.44-24.72	-0.10	0.21	13.66	-0.10	0.00	15.22	0.48	
1	1.05	-0.44-24.72	-0.10	0.20	13.66	-0.08	0.00	15.22	0.54	
1	1.07	-0.44-24.72	-0.10	0.21	13.66	-0.10	0.00	15.22	0.48	
1	1.05	-0.44-24.72	-0.10	0.20	13.66	-0.08	0.00	15.22	0.54	
1	1.07	-0.44-24.72	-0.10	0.21	13.66	-0.10	0.00	15.22	0.48	
1	1.05	-0.44-24.72	-0.10	0.20	13.66	-0.08	0.00	15.22	0.54	
1	1.07	-0.44-24.72	-0.10	0.21	13.66	-0.10	0.00	15.22	0.48	
1	1.05	-0.44-24.72	-0.10	0.20	13.66	-0.08	0.00	15.22	0.54	
1	1.07	-0.44-24.72	-0.10	0.21	13.66	-0.10	0.00	15.22	0.48	
1	1.05	-0.44-24.72	-0.10	0.20	13.66	-0.08	0.00	15.22	0.54	
1	1.07	-0.44-24.72	-0.10	0.21	13.66	-0.10	0.00	15.22	0.48	
1	1.05	-0.44-24.72	-0.10	0.20	13.66	-0.08	0.00	15.22	0.54	
1	1.07	-0.44-24.72	-0.10	0.21	13.66	-0.10	0.00	15.22	0.48	
1	1.05	-0.44-24.72	-0.10	0.20	13.66	-0.08	0.00	15.22	0.54	
1	1.07	-0.44-24.72	-0.10	0.21	13.66	-0.10	0.00	15.22	0.48	
1	1.05	-0.44-24.72	-0.10	0.20	13.66	-0.08	0.00	15.22	0.54	
1	1.07	-0.44-24.72	-0.10	0.21	13.66	-0.10	0.00	15.22	0.48	
1	1.05	-0.44-24.72	-0.10	0.20	13.66	-0.08	0.00	15.22	0.54	
1	1.07	-0.44-24.72	-0.10	0.21	13.66	-0.10	0.00	15.22	0.48	
1	1.05	-0.44-24.72	-0.10	0.20	13.66	-0.08	0.00	15.22	0.54	
1	1.07	-0.44-24.72	-0.10	0.21	13.66	-0.10	0.00	15.22	0.48	
1	1.05	-0.44-24.72	-0.10	0.20	13.66	-0.08	0.00	15.22	0.54	
1	1.07	-0.44-24.72	-0.10	0.21	13.66	-0.10	0.00	15.22	0.48	
1	1.05	-0.44-24.72	-0.10	0.20	13.66	-0.08	0.00	15.22	0.54	
1	1.07	-0.44-24.72	-0.10	0.21	13.66	-0.10	0.00	15.22	0.48	
1	1.05	-0.44-24.72	-0.10	0.20	13.66	-0.08	0.00	15.22	0.54	
1	1.07	-0.44-24.72	-0.10	0.21	13.66	-0.10	0.00	15.22	0.48	
1	1.05	-0.44-24.72	-0.10	0.20	13.66	-0.08	0.00	15.22	0.54	
1	1.07	-0.44-24.72	-0.10	0.21	13.66	-0.10	0.00	15.22	0.48	
1	1.05	-0.44-24.72	-0.10	0.20	13.66	-0.08	0.00	15.22	0.54	
1	1.07	-0.44-24.72	-0.10	0.21	13.66	-0.10	0.00	15.22	0.48	
1	1.05	-0.44-24.72	-0.10	0.20	13.66	-0.08	0.00	15.22	0.54	
1	1.07	-0.44-24.72	-0.10	0.21	13.66	-0.10	0.00	15.22	0.48	
1	1.05	-0.44-24.72	-0.10	0.20	13.66	-0.08	0.00	15.22	0.54	
1	1.07	-0.44-24.72	-0.10	0.21	13.66	-0.10	0.00	15.22	0.48	
1	1.05	-0.44-24.72	-0.10	0.20	13.66	-0.08	0.00	15.22	0.54	
1	1.07	-0.44-24.72	-0.10	0.21	13.66	-0.10	0.00	15.22	0.48	
1	1.05	-0.44-24.72	-0.10	0.20	13.66	-0.08	0.00	15.22	0.54	
1	1.07	-0.44-24.72	-0.10	0.21	13.66	-0.10	0.00	15.22	0.48	
1	1.05	-0.44-24.72	-0.10	0.20	13.66	-0.08	0.00	15.22	0.54	
1	1.07	-0.44-24.72	-0.10	0.21	13.66	-0.10	0.00	15.22	0.48	
1	1.05	-0.44-24.72	-0.10	0.20	13.66	-0.08	0.00	15.22	0.54	
1	1.07	-0.44-24.72	-0.10	0.21	13.66	-0.10	0.00	15.22	0.48	
1	1.05	-0.44-24.72	-0.10	0.20	13.66	-0.08	0.00	15.22	0.54	
1	1.07	-0.44-24.72	-0.10	0.21	13.66	-0.10	0.00	15.22	0.48	
1	1.05	-0.44-24.72	-0.10	0.20	13.66	-0.08	0.00	15.22	0.54	
1	1.07	-0.44-24.72	-0.10	0.21	13.66	-0.10	0.00	15.22	0.48	
1	1.05	-0.44-24.72	-0.10	0.20	13.66	-0.08	0.00	15.22	0.54	
1	1.07	-0.44-24.72	-0.10	0.21	13.66	-0.10	0.00	15.22	0.48	
1	1.05	-0.44-24.72	-0.10	0.20	13.66	-0.08	0.00	15.22	0.54	
1	1.07	-0.44-24.72	-0.10	0.21	13.66	-0.10	0.00	15.22	0.48	
1	1.05	-0.44-24.72	-0.10	0.20	13.66	-0.08	0.00	15.22	0.54	
1	1.07	-0.44-24.72	-0.10	0.21	13.66	-0.10	0.00	15.22	0.48	
1	1.05	-0.44-24.72	-0.10	0.20	13.66	-0.08	0.00	15.22	0.54	
1	1.07	-0.44-24.72	-0.10	0.21	13.66	-0.10	0.00	15.22	0.48	
1	1.05	-0.44-24.72	-0.10	0.20	13.66	-0.08	0.00	15.22	0.54	
1	1.07	-0.44-24.72	-0.10	0.21	13.66	-0.10	0.00	15.22	0.48	
1	1.05	-0.44-24.72	-0.10	0.20	13.66	-0.08	0.00	15.22	0.54	
1	1.07	-0.44-24.72	-0.10	0.21	13.66	-0.10	0.00	15.22	0.48	
1	1.05	-0.44-24.72	-0.10	0.20	13.66	-0.08	0.00	15.22	0.54	
1	1.07	-0.44-24.72	-0.10	0.21	13.66	-0.10	0.00	15.22	0.48	
1	1.05	-0.44-24.72	-0.10	0.20	13.66	-0.08	0.00	15.22	0.54	
1	1.07	-0.44-24.72	-0.10	0.21	13.66	-0.10	0.00	15.22	0.48	
1	1.05	-0.44-24.72	-0.10	0.20	13.66	-0.08	0.00	15.22	0.54	
1	1.07	-0.44-24.72	-0.10	0.21	13.66	-0.10	0.00	15.22	0.48	
1	1.05	-0.44-24.72	-0.10	0.20	13.66	-0.08	0.00	15.22	0.54	
1	1.07	-0.44-24.72	-0.10	0.21	13.66	-0.10	0.00	15.22	0.48	
1	1.05	-0.44-24.72	-0.10	0.20	13.66	-0.08	0.00	15.22	0.54	
1	1.07	-0.44-24.72	-0.10	0.21	13.66	-0.10	0.00	15.22	0.48	
1	1.05	-0.44-24.72	-0.10	0.20	13.66	-0.08	0.00	15.22	0.54	
1	1.07	-0.44-24.72	-0.10	0.21	13.66	-0.10	0.00	15.22	0.48	
1	1.05	-0.44-24.72	-0.10	0.20	13.66	-0.08	0.00	15.22	0.54	
1	1.07	-0.44-24.72	-0.10	0.21	13.66	-0.10	0.00	15.22	0.48	
1	1.05	-0.44-24.72	-0.10	0.20	13.66	-0.08	0.00	15.22	0.54	
1	1.07	-0.44-24.72	-0.10	0.21	13.66	-0.10	0.00	15.22	0.48	
1	1.05	-0.44-24.72	-0.10	0.20	13.66	-0.08	0.00	15.22	0.54	
1	1.07	-0.44-24.72	-0.10	0.21	13.66	-0.10	0.00	15.22	0.48	
1	1.05	-0.44-24.72	-0.10	0.20	13.66	-0.08	0.00	15.22	0.54	
1	1.07	-0.44-24.72	-0.10	0.21	13.66	-0.10	0.00	15.22	0.48	
1	1.05	-0.44-24.72	-0.10	0.20	13.66	-0.08	0.00	15.22	0.54	
1	1.07	-0.44-24.72	-0.10	0.21	13.66	-0.10	0.00	15.22	0.48	
1	1.05	-0.44-24.72	-0.10	0.20	13.66	-0.08	0.00	15.22	0.54	
1	1.07	-0.44-24.72	-0.10	0.21	13.66	-0.10	0.00	15.22	0.48	
1	1.05	-0.44-24.72	-0.10	0.20	13.66	-0.08	0.00	15.22	0.54	
1	1.07	-0.44-24.72	-0.10	0.21	13.66	-0.10	0.00	15.22	0.48	
1	1.05	-0.44-24.72	-0.10	0.20	13.66	-0.08	0.00	15.22	0.54	
1	1.07	-0.44-24.72	-0.10	0.21	13.66	-0.10	0.00	15.22	0.48	
1	1.05	-0.44-24.72	-0.10	0.20	13.66	-0.08	0.00	15.22	0.54	
1	1.07	-0.44-24.72	-0.10	0.21	13.66	-0.10	0.00	15.22	0.48	
1	1.05	-0.44-24.72	-0.10	0.20	13.66	-0.08	0.00	15.22	0.54	
1	1.07	-0.44-24.72	-0.10	0.21	13.66	-0.10	0.00	15.22	0.48	
1	1.05	-0.44-24.72	-0.10	0.20	13.66	-0.08	0.00	15.22	0.54	
1	1.07	-0.44-24.72	-0.10	0.21	13.66	-0.10	0.00	15.22	0.48	
1	1.05	-0.44-24.72	-0.10	0.20	13.66	-0.08	0.00	15.22	0.54	
1	1.07	-0.44-24.72	-0.10	0.21	13.66	-0.10	0.00	15.22	0.48	
1	1.05	-0.44-24.72	-0.10	0.20	13.66	-0.08	0.00	15.22	0.54	
1	1.07	-0.44-24.72	-0.10	0.21	13.66	-0.10	0.00	15.22	0.48	
1	1.05	-0.44-24.72	-0.10	0.20	13.66	-0.08	0.00	15.22	0.54	
1	1.07	-0.44-24.72	-0.10	0.21	13.66	-0.10	0.00	15.22	0.48	
1	1.05	-0.44-24.72	-0.10	0.20	13.66	-0.08	0.00	15.22	0.54	
1	1.07	-0.44-24.72	-0.10	0.21	13.66	-0.10	0.00	15.22	0.48	
1	1.05	-0.44-24.72	-0.10	0.20	13.66	-0.08	0.00	15.22	0.54	
1	1.07	-0.44-24.72	-0.10	0.21	13.66	-0.10	0.00	15.22	0.48	
1	1.05	-0.44-24.72	-0.10	0.20	13.66	-0.08	0.00	15.22	0.54	
1	1.07	-0.44-24.72	-0.10	0.21	13.66	-0.10	0.00	15.22	0.48	
1	1.05	-0.44-24.72	-0.10	0.20	13.66	-0.08	0.00	15.22	0.54	
1	1.07	-0.44-24.72	-0.10	0.21	13.66	-0.10	0.00	15.22	0.48	
1	1.05	-0.44-24.72	-0.10	0.20	13.66	-0.08	0.00	15.22	0.54	
1	1.07	-0.44-24.72	-0.10	0.21	13.66	-0.10	0.00	15.22	0.48	
1	1.05	-0.44-24.72	-0.10	0.20	13.66	-0.08	0.00	15.22	0.54	
1	1.07	-0.44-24.72	-0.10	0.21	13.66	-0.10	0.00	15.22	0.48	
1	1.05	-0.44-24.72	-0.10	0.20	13.66	-0.08	0.00	15.22	0.54	
1	1.07	-0.44-24.72	-0.10	0.21	13.66	-0.10	0.00	15.22	0.48	
1	1.05	-0.44-24.72	-0.10	0.20	13.66	-0.08	0.00	15.22	0.54	
1	1.07	-0.44-24.72	-0.10	0.21	13.66	-0.10	0.00	15.22	0.48	

GEOMETRY MODIFICATION 19

11= 1/34589408 12= 987052913 MINC= 3 NCASE= 6

INCR NUM % STEP DEGREE
1 1.00 0.000
2 2.10 0.000
3 3.15 0.000

UPAR IN CS	PAR1	PAR2	PAR3	PAR4	PAR5	PAR6	PAR7	PAR8	PAR9	PAR10
1 1	1.67	-0.44-24.16	-0.08	0.24	13.66	-0.10	0.00	15.22	0.46	0.46
		2.725	0.128	21.30	21.30	-1.330				
1 2	1.67	-0.44-24.16	-0.08	0.24	13.66	-0.09	0.00	15.28	0.46	0.46
		2.732	0.127	21.31	21.31	-1.329				
1 3	1.67	-0.44-24.16	-0.08	0.24	13.66	-0.08	0.00	15.16	0.46	0.46
		2.740	0.127	21.32	21.32	-1.327				
1 4	1.67	-0.44-24.16	-0.08	0.24	13.66	-0.07	0.00	15.16	0.46	0.46
		2.748	0.127	21.33	21.33	-1.326				
1 5	1.67	-0.44-24.16	-0.08	0.24	13.66	-0.06	0.00	15.16	0.46	0.46
		2.756	0.127	21.34	21.34	-1.325				
1 6	1.67	-0.44-24.16	-0.08	0.24	13.66	-0.05	0.00	15.16	0.46	0.46
		2.764	0.127	21.35	21.35	-1.324				
1 7	1.67	-0.44-24.16	-0.08	0.24	13.66	-0.04	0.00	15.16	0.46	0.46
		2.772	0.127	21.36	21.36	-1.323				
1 8	1.67	-0.44-24.16	-0.08	0.24	13.66	-0.03	0.00	15.16	0.46	0.46
		2.780	0.127	21.37	21.37	-1.322				
1 9	1.67	-0.44-24.16	-0.08	0.24	13.66	-0.02	0.00	15.16	0.46	0.46
		2.788	0.127	21.38	21.38	-1.321				
1 10	1.67	-0.44-24.16	-0.08	0.24	13.66	-0.01	0.00	15.16	0.46	0.46
		2.796	0.127	21.39	21.39	-1.320				
1 11	1.67	-0.44-24.16	-0.08	0.24	13.66	0.00	0.00	15.16	0.46	0.46
		2.804	0.127	21.40	21.40	-1.319				
1 12	1.67	-0.44-24.16	-0.08	0.24	13.66	0.01	0.00	15.16	0.46	0.46
		2.812	0.127	21.41	21.41	-1.318				
1 13	1.67	-0.44-24.16	-0.08	0.24	13.66	0.02	0.00	15.16	0.46	0.46
		2.820	0.127	21.42	21.42	-1.317				
1 14	1.67	-0.44-24.16	-0.08	0.24	13.66	0.03	0.00	15.16	0.46	0.46
		2.828	0.127	21.43	21.43	-1.316				
1 15	1.67	-0.44-24.16	-0.08	0.24	13.66	0.04	0.00	15.16	0.46	0.46
		2.836	0.127	21.44	21.44	-1.315				
1 16	1.67	-0.44-24.16	-0.08	0.24	13.66	0.05	0.00	15.16	0.46	0.46
		2.844	0.127	21.45	21.45	-1.314				
1 17	1.67	-0.44-24.16	-0.08	0.24	13.66	0.06	0.00	15.16	0.46	0.46
		2.852	0.127	21.46	21.46	-1.313				
1 18	1.67	-0.44-24.16	-0.08	0.24	13.66	0.07	0.00	15.16	0.46	0.46
		2.860	0.127	21.47	21.47	-1.312				
1 19	1.67	-0.44-24.16	-0.08	0.24	13.66	0.08	0.00	15.16	0.46	0.46
		2.868	0.127	21.48	21.48	-1.311				
1 20	1.67	-0.44-24.16	-0.08	0.24	13.66	0.09	0.00	15.16	0.46	0.46
		2.876	0.127	21.49	21.49	-1.310				
1 21	1.67	-0.44-24.16	-0.08	0.24	13.66	0.10	0.00	15.16	0.46	0.46
		2.884	0.127	21.50	21.50	-1.309				
1 22	1.67	-0.44-24.16	-0.08	0.24	13.66	0.11	0.00	15.16	0.46	0.46
		2.892	0.127	21.51	21.51	-1.308				
1 23	1.67	-0.44-24.16	-0.08	0.24	13.66	0.12	0.00	15.16	0.46	0.46
		2.900	0.127	21.52	21.52	-1.307				
1 24	1.67	-0.44-24.16	-0.08	0.24	13.66	0.13	0.00	15.16	0.46	0.46
		2.908	0.127	21.53	21.53	-1.306				
1 25	1.67	-0.44-24.16	-0.08	0.24	13.66	0.14	0.00	15.16	0.46	0.46
		2.916	0.127	21.54	21.54	-1.305				
1 26	1.67	-0.44-24.16	-0.08	0.24	13.66	0.15	0.00	15.16	0.46	0.46
		2.924	0.127	21.55	21.55	-1.304				
1 27	1.67	-0.44-24.16	-0.08	0.24	13.66	0.16	0.00	15.16	0.46	0.46
		2.932	0.127	21.56	21.56	-1.303				
1 28	1.67	-0.44-24.16	-0.08	0.24	13.66	0.17	0.00	15.16	0.46	0.46
		2.940	0.127	21.57	21.57	-1.302				
1 29	1.67	-0.44-24.16	-0.08	0.24	13.66	0.18	0.00	15.16	0.46	0.46
		2.948	0.127	21.58	21.58	-1.301				
1 30	1.67	-0.44-24.16	-0.08	0.24	13.66	0.19	0.00	15.16	0.46	0.46
		2.956	0.127	21.59	21.59	-1.300				
1 31	1.67	-0.44-24.16	-0.08	0.24	13.66	0.20	0.00	15.16	0.46	0.46
		2.964	0.127	21.60	21.60	-1.299				
1 32	1.67	-0.44-24.16	-0.08	0.24	13.66	0.21	0.00	15.16	0.46	0.46
		2.972	0.127	21.61	21.61	-1.298				
1 33	1.67	-0.44-24.16	-0.08	0.24	13.66	0.22	0.00	15.16	0.46	0.46
		2.980	0.127	21.62	21.62	-1.297				
1 34	1.67	-0.44-24.16	-0.08	0.24	13.66	0.23	0.00	15.16	0.46	0.46
		2.988	0.127	21.63	21.63	-1.296				
1 35	1.67	-0.44-24.16	-0.08	0.24	13.66	0.24	0.00	15.16	0.46	0.46
		2.996	0.127	21.64	21.64	-1.295				
1 36	1.67	-0.44-24.16	-0.08	0.24	13.66	0.25	0.00	15.16	0.46	0.46
		3.004	0.127	21.65	21.65	-1.294				
1 37	1.67	-0.44-24.16	-0.08	0.24	13.66	0.26	0.00	15.16	0.46	0.46
		3.012	0.127	21.66	21.66	-1.293				
1 38	1.67	-0.44-24.16	-0.08	0.24	13.66	0.27	0.00	15.16	0.46	0.46
		3.020	0.127	21.67	21.67	-1.292				
1 39	1.67	-0.44-24.16	-0.08	0.24	13.66	0.28	0.00	15.16	0.46	0.46
		3.028	0.127	21.68	21.68	-1.291				
1 40	1.67	-0.44-24.16	-0.08	0.24	13.66	0.29	0.00	15.16	0.46	0.46
		3.036	0.127	21.69	21.69	-1.290				
1 41	1.67	-0.44-24.16	-0.08	0.24	13.66	0.30	0.00	15.16	0.46	0.46
		3.044	0.127	21.70	21.70	-1.289				
1 42	1.67	-0.44-24.16	-0.08	0.24	13.66	0.31	0.00	15.16	0.46	0.46
		3.052	0.127	21.71	21.71	-1.288				
1 43	1.67	-0.44-24.16	-0.08	0.24	13.66	0.32	0.00	15.16	0.46	0.46
		3.060	0.127	21.72	21.72	-1.287				
1 44	1.67	-0.44-24.16	-0.08	0.24	13.66	0.33	0.00	15.16	0.46	0.46
		3.068	0.127	21.73	21.73	-1.286				
1 45	1.67	-0.44-24.16	-0.08	0.24	13.66	0.34	0.00	15.16	0.46	0.46
		3.076	0.127	21.74	21.74	-1.285				
1 46	1.67	-0.44-24.16	-0.08	0.24	13.66	0.35	0.00	15.16	0.46	0.46
		3.084	0.127	21.75	21.75	-1.284				
1 47	1.67	-0.44-24.16	-0.08	0.24	13.66	0.36	0.00	15.16	0.46	0.46
		3.092	0.127	21.76	21.76	-1.283				
1 48	1.67	-0.44-24.16	-0.08	0.24	13.66	0.37	0.00	15.16	0.46	0.46
		3.100	0.127	21.77	21.77	-1.282				
1 49	1.67	-0.44-24.16	-0.08	0.24	13.66	0.38	0.00	15.16	0.46	0.46
		3.108	0.127	21.78	21.78	-1.281				
1 50	1.67	-0.44-24.16	-0.08	0.24	13.66	0.39	0.00	15.16	0.46	0.46
		3.116	0.127	21.79	21.79	-1.280				
1 51	1.67	-0.44-24.16	-0.08	0.24	13.66	0.40	0.00	15.16	0.46	0.46
		3.124	0.127	21.80	21.80	-1.279				
1 52	1.67	-0.44-24.16	-0.08	0.24	13.66	0.41	0.00	15.16	0.46	0.46
		3.132	0.127	21.81	21.81	-1.278				
1 53	1.67	-0.44-24.16	-0.08	0.24	13.66	0.42	0.00	15.16	0.46	0.46
		3.140	0.127	21.82	21.82	-1.277				
1 54	1.67	-0.44-24.16	-0.08	0.24	13.66	0.43	0.00	15.16	0.46	0.46
		3.148	0.127	21.83	21.83	-1.276				
1 55	1.67	-0.44-24.16	-0.08	0.24	13.66	0.44	0.00	15.16	0.46	0.46
		3.156	0.127	21.84	21.84	-1.275				
1 56	1.67	-0.44-24.16	-0.08	0.24	13.66	0.45	0.00	15.16	0.46	0.46
		3.164	0.127	21.85	21.85	-1.274				
1 57	1.67	-0.44-24.16	-0.08	0.24	13.66	0.46	0.00	15.16	0.46	0.46
		3.172	0.127	21.86	21.86	-1.273				
1 58	1.67	-0.44-24.16	-0.08	0.24	13.66	0.47	0.00	15.16	0.46	0.46
		3.180	0.127	21.87	21.87	-1.272				
1 59	1.67	-0.44-24.16	-0.08	0.24	13.66	0.48	0.00	15.16	0.46	0.46
		3.188	0.127	21.88	21.88	-1.271				
1 60	1.67	-0.44-24.16	-0.08	0.24	13.66	0.49	0.00	15.16	0.46	0.46
		3.196	0.127	21.89	21.89	-1.270				
1 61	1.67	-0.44-24.16	-0.08	0.24	13.66	0.50	0.00	15.16	0.46	0.46
		3.204	0.127	21.90	21.90	-1.269				
1 62	1.67	-0.44-24.16	-0.08	0.24	13.66	0.51	0.00	15.16	0.46	0.46
		3.212	0.127	21.91	21.91	-1.268				
1 63	1.67	-0.44-24.16	-0.08	0.24	13.66	0.52	0.00	15.16	0	

GEOMETRIC MULTIPLICATION 22

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11= 123456432 12= 987690347 NJNC= 3 NCASr= 6
```

16-CH 100M	8 STRIP	DEGREE
1	1.10	0.100
2	1.20	1.400
3	1.30	2.100

[illegible]

GEOMETRIC MODIFICATION 25

11= 123456789 12= 987654321 N1MC= 3 N2MC= 0

1NCR 1 2 3
1.25 0.800
2.50 3.400
3.75 4.600

OPAR IN CS	PAR1 1	PAR2 1	PAR3 1	PAR4 1	PAR5 1	PAR6 1	PAR7 1	PAR8 1	PAR9 1	PAR10 1
1 1	1.53	-0.37	-0.22	-0.14	0.21	0.36	-0.10	0.15	18.36	0.48
1 2	2.502	0.0635	39.40	-1.240						
1 3	1.49	-0.37	-0.22	-0.14	0.21	0.36	-0.10	0.15	18.36	0.48
1 4	1.53	-0.37	-0.22	-0.14	0.21	0.36	-0.10	0.15	18.36	0.48
1 5	1.53	-0.37	-0.22	-0.14	0.21	0.36	-0.10	0.15	18.36	0.48
1 6	1.53	-0.37	-0.22	-0.14	0.21	0.36	-0.10	0.15	18.36	0.48
1 7	1.53	-0.37	-0.22	-0.14	0.21	0.36	-0.10	0.15	18.36	0.48
1 8	1.53	-0.37	-0.22	-0.14	0.21	0.36	-0.10	0.15	18.36	0.48
1 9	1.53	-0.37	-0.22	-0.14	0.21	0.36	-0.10	0.15	18.36	0.48
1 10	1.53	-0.37	-0.22	-0.14	0.21	0.36	-0.10	0.15	18.36	0.48
1 11	1.53	-0.37	-0.22	-0.14	0.21	0.36	-0.10	0.15	18.36	0.48
1 12	1.53	-0.37	-0.22	-0.14	0.21	0.36	-0.10	0.15	18.36	0.48
1 13	1.53	-0.37	-0.22	-0.14	0.21	0.36	-0.10	0.15	18.36	0.48
1 14	1.53	-0.37	-0.22	-0.14	0.21	0.36	-0.10	0.15	18.36	0.48
1 15	1.53	-0.37	-0.22	-0.14	0.21	0.36	-0.10	0.15	18.36	0.48
1 16	1.53	-0.37	-0.22	-0.14	0.21	0.36	-0.10	0.15	18.36	0.48
1 17	1.53	-0.37	-0.22	-0.14	0.21	0.36	-0.10	0.15	18.36	0.48
1 18	1.53	-0.37	-0.22	-0.14	0.21	0.36	-0.10	0.15	18.36	0.48
1 19	1.53	-0.37	-0.22	-0.14	0.21	0.36	-0.10	0.15	18.36	0.48
1 20	1.53	-0.37	-0.22	-0.14	0.21	0.36	-0.10	0.15	18.36	0.48

GEOMETRIC MODIFICATION 26

11= 123456789 12= 987654321 N1MC= 3 N2MC= 0

1NCR 1 2 3
1.25 0.800
2.50 3.400
3.75 4.600

OPAR IN CS	PAR1 1	PAR2 1	PAR3 1	PAR4 1	PAR5 1	PAR6 1	PAR7 1	PAR8 1	PAR9 1	PAR10 1
1 1	1.53	-0.37	-0.22	-0.14	0.21	0.36	-0.10	0.15	18.36	0.48
1 2	2.502	0.0635	39.40	-1.240						
1 3	1.49	-0.37	-0.22	-0.14	0.21	0.36	-0.10	0.15	18.36	0.48
1 4	1.53	-0.37	-0.22	-0.14	0.21	0.36	-0.10	0.15	18.36	0.48
1 5	1.53	-0.37	-0.22	-0.14	0.21	0.36	-0.10	0.15	18.36	0.48
1 6	1.53	-0.37	-0.22	-0.14	0.21	0.36	-0.10	0.15	18.36	0.48
1 7	1.53	-0.37	-0.22	-0.14	0.21	0.36	-0.10	0.15	18.36	0.48
1 8	1.53	-0.37	-0.22	-0.14	0.21	0.36	-0.10	0.15	18.36	0.48
1 9	1.53	-0.37	-0.22	-0.14	0.21	0.36	-0.10	0.15	18.36	0.48
1 10	1.53	-0.37	-0.22	-0.14	0.21	0.36	-0.10	0.15	18.36	0.48
1 11	1.53	-0.37	-0.22	-0.14	0.21	0.36	-0.10	0.15	18.36	0.48
1 12	1.53	-0.37	-0.22	-0.14	0.21	0.36	-0.10	0.15	18.36	0.48
1 13	1.53	-0.37	-0.22	-0.14	0.21	0.36	-0.10	0.15	18.36	0.48
1 14	1.53	-0.37	-0.22	-0.14	0.21	0.36	-0.10	0.15	18.36	0.48
1 15	1.53	-0.37	-0.22	-0.14	0.21	0.36	-0.10	0.15	18.36	0.48
1 16	1.53	-0.37	-0.22	-0.14	0.21	0.36	-0.10	0.15	18.36	0.48
1 17	1.53	-0.37	-0.22	-0.14	0.21	0.36	-0.10	0.15	18.36	0.48
1 18	1.53	-0.37	-0.22	-0.14	0.21	0.36	-0.10	0.15	18.36	0.48
1 19	1.53	-0.37	-0.22	-0.14	0.21	0.36	-0.10	0.15	18.36	0.48
1 20	1.53	-0.37	-0.22	-0.14	0.21	0.36	-0.10	0.15	18.36	0.48

GEOMETRY MODIFICATION 29

11= 1234567430 12= 987671553 MINC= 3 NCASE= 6

INCP NUM 3 STEP DEGREE
1 1 0.50
2 1.50
3 2.85

UPAR IN CS	PAR1	PAR2	PAR3	PAR4	PAR5	PAR6	PAR7	PAR8	PAR9	PAR10
1	1.53	-0.37-22.32	-0.10	0.27	8.36	-0.19	0.01	15.36	0.48	
2	3.3	0.0447	53.02	-1.177						
3	1.54	-0.37-22.32	-0.10	0.27	7.76	-0.19	0.01	16.56	0.48	
4	1.53	-0.37-22.32	-0.10	0.27	7.76	-0.19	0.01	16.56	0.48	
5	1.52	-0.37-22.32	-0.10	0.27	7.76	-0.19	0.01	16.56	0.48	
6	1.54	-0.37-22.32	-0.10	0.27	7.76	-0.19	0.01	16.56	0.48	
7	1.53	-0.37-22.32	-0.10	0.27	7.76	-0.19	0.01	16.56	0.48	
8	1.54	-0.37-22.32	-0.10	0.27	7.76	-0.19	0.01	16.56	0.48	
9	1.53	-0.37-22.32	-0.10	0.27	7.76	-0.19	0.01	16.56	0.48	
10	1.54	-0.37-22.32	-0.10	0.27	7.76	-0.19	0.01	16.56	0.48	
11	1.53	-0.37-22.32	-0.10	0.27	7.76	-0.19	0.01	16.56	0.48	
12	1.54	-0.37-22.32	-0.10	0.27	7.76	-0.19	0.01	16.56	0.48	
13	1.53	-0.37-22.32	-0.10	0.27	7.76	-0.19	0.01	16.56	0.48	
14	1.54	-0.37-22.32	-0.10	0.27	7.76	-0.19	0.01	16.56	0.48	
15	1.53	-0.37-22.32	-0.10	0.27	7.76	-0.19	0.01	16.56	0.48	
16	1.54	-0.37-22.32	-0.10	0.27	7.76	-0.19	0.01	16.56	0.48	
17	1.53	-0.37-22.32	-0.10	0.27	7.76	-0.19	0.01	16.56	0.48	
18	1.54	-0.37-22.32	-0.10	0.27	7.76	-0.19	0.01	16.56	0.48	

GEOMETRY MODIFICATION 30

11= 1234567431 12= 987671553 MINC= 3 NCASE= 6

INCP NUM 3 STEP DEGREE
1 1 0.50
2 1.50
3 2.85

UPAR IN CS	PAR1	PAR2	PAR3	PAR4	PAR5	PAR6	PAR7	PAR8	PAR9	PAR10
1	1.53	-0.37-22.32	-0.10	0.27	8.36	-0.19	0.01	15.36	0.48	
2	3.356	0.0350	67.31	-1.168						
3	1.53	-0.37-22.32	-0.10	0.27	8.36	-0.19	0.01	15.36	0.48	
4	1.54	-0.37-22.32	-0.10	0.27	8.36	-0.19	0.01	15.36	0.48	
5	1.53	-0.37-22.32	-0.10	0.27	8.36	-0.19	0.01	15.36	0.48	
6	1.54	-0.37-22.32	-0.10	0.27	8.36	-0.19	0.01	15.36	0.48	
7	1.53	-0.37-22.32	-0.10	0.27	8.36	-0.19	0.01	15.36	0.48	
8	1.54	-0.37-22.32	-0.10	0.27	8.36	-0.19	0.01	15.36	0.48	
9	1.53	-0.37-22.32	-0.10	0.27	8.36	-0.19	0.01	15.36	0.48	
10	1.54	-0.37-22.32	-0.10	0.27	8.36	-0.19	0.01	15.36	0.48	
11	1.53	-0.37-22.32	-0.10	0.27	8.36	-0.19	0.01	15.36	0.48	
12	1.54	-0.37-22.32	-0.10	0.27	8.36	-0.19	0.01	15.36	0.48	
13	1.53	-0.37-22.32	-0.10	0.27	8.36	-0.19	0.01	15.36	0.48	
14	1.54	-0.37-22.32	-0.10	0.27	8.36	-0.19	0.01	15.36	0.48	
15	1.53	-0.37-22.32	-0.10	0.27	8.36	-0.19	0.01	15.36	0.48	
16	1.54	-0.37-22.32	-0.10	0.27	8.36	-0.19	0.01	15.36	0.48	
17	1.53	-0.37-22.32	-0.10	0.27	8.36	-0.19	0.01	15.36	0.48	
18	1.54	-0.37-22.32	-0.10	0.27	8.36	-0.19	0.01	15.36	0.48	

GEOMETRY MODIFICATION 32
11= 1234594648 12= 987600275 NINC= 3 HCASE= 6
INCR NUM & STEP DEGREE SELECT ONLY CL-
1 0.50
2 1.00
3 1.50
4 2.00
5 2.50
6 3.00

UPAR IN CS	PART 1	PART 2	PART 3	PART 4	PART 5	PART 6	PART 7	PART 8	PART 9	PART 10
1	1.54	-0.37-22.32	-0.10	0.27	8.36	-0.19	0.01	15.36	0.50	
2	1.54	-0.37-22.32	-0.09	0.27	8.36	-0.20	0.01	15.36	0.50	
3	1.55	-0.37-22.32	-0.11	0.27	8.36	-0.18	0.01	14.36	0.50	
4	1.55	-0.37-22.32	-0.11	0.27	8.36	-0.20	0.00	16.36	0.50	
5	1.55	-0.37-22.32	-0.09	0.27	8.36	-0.18	0.01	14.36	0.50	
6	1.55	-0.37-22.32	-0.11	0.27	8.36	-0.18	0.01	15.36	0.50	
7	1.54	-0.37-22.32	-0.09	0.27	8.36	-0.18	0.01	15.36	0.50	
8	1.54	-0.37-22.32	-0.12	0.26	10.36	-0.19	0.01	17.36	0.50	
9	1.54	-0.37-22.32	-0.10	0.27	8.36	-0.20	0.00	17.36	2.50	
10	1.54	-0.37-22.32	-0.12	0.26	10.36	-0.20	0.01	17.36	2.50	
11	1.54	-0.37-22.32	-0.12	0.27	8.36	-0.19	0.01	15.36	0.50	
12	1.54	-0.37-22.32	-0.12	0.27	8.36	-0.19	0.01	13.36	2.50	
13	1.54	-0.37-22.32	-0.10	0.27	8.36	-0.19	0.01	15.36	0.50	
14	1.54	-0.37-22.32	-0.12	0.26	10.36	-0.19	0.01	15.36	0.50	
15	1.54	-0.37-22.32	-0.12	0.26	10.36	-0.19	0.01	15.36	0.50	
16	1.54	-0.37-22.32	-0.10	0.27	8.36	-0.17	0.03	12.36	3.50	
17	1.54	-0.37-22.32	-0.10	0.27	8.36	-0.17	0.03	15.36	0.50	
18	1.54	-0.37-22.32	-0.08	0.26	5.36	-0.19	0.03	12.36	0.50	
19	1.52	-0.36-25.32	-0.10	0.26	8.36	-0.17	0.03	18.36	3.50	

GEOMETRY MODIFICATION 31
11= 1234594648 12= 987600275 NINC= 3 HCASE= 6
INCR NUM & STEP DEGREE SELECT ONLY CL-
1 0.50
2 1.00
3 1.50
4 2.00
5 2.50
6 3.00

UPAR IN CS	PART 1	PART 2	PART 3	PART 4	PART 5	PART 6	PART 7	PART 8	PART 9	PART 10
1	1.55	-0.36-22.32	-0.10	0.26	8.36	-0.19	0.01	15.36	0.46	
2	1.55	-0.36-22.32	-0.11	0.26	8.36	-0.19	0.01	15.66	0.76	
3	1.55	-0.36-22.32	-0.11	0.26	8.36	-0.20	0.01	15.06	0.46	
4	1.55	-0.36-22.32	-0.10	0.26	8.36	-0.20	0.01	15.36	0.76	
5	1.56	-0.36-22.32	-0.10	0.26	8.36	-0.19	0.00	15.06	0.46	
6	1.55	-0.36-22.32	-0.10	0.26	8.36	-0.19	0.00	15.36	0.46	
7	1.55	-0.36-22.32	-0.09	0.25	8.36	-0.16	0.01	15.36	0.76	
8	1.53	-0.35-22.32	-0.10	0.26	8.36	-0.19	0.01	14.76	1.06	
9	1.55	-0.35-22.32	-0.09	0.27	8.36	-0.19	0.01	15.36	0.46	
10	1.53	-0.36-22.32	-0.09	0.27	8.36	-0.19	0.01	15.96	0.46	
11	1.55	-0.35-22.32	-0.12	0.26	8.36	-0.17	0.00	14.76	1.06	
12	1.56	-0.36-22.32	-0.09	0.25	8.36	-0.19	0.01	15.96	0.46	
13	1.55	-0.37-22.32	-0.10	0.26	8.36	-0.20	0.01	15.96	0.46	
14	1.55	-0.36-22.32	-0.12	0.26	8.36	-0.19	0.00	15.36	0.46	
15	1.55	-0.36-22.32	-0.10	0.27	8.36	-0.17	0.00	14.46	0.46	
16	1.55	-0.36-22.32	-0.10	0.27	8.36	-0.17	0.01	16.76	0.46	
17	1.53	-0.38-23.32	-0.10	0.26	8.36	-0.19	0.00	15.36	1.36	
18	1.57	-0.36-22.32	-0.10	0.26	8.36	-0.21	0.01	15.36	1.36	
19	1.55	-0.36-22.32	-0.12	0.27	8.36	-0.19	0.03	16.76	0.46	

APPENDIX (iv-b) INITIAL AND FINAL CONFIGURATION POLAR DATA

ANGLE OF ATTACK	INITIAL GEOMETRY		FINAL GEOMETRY	
	C_L	C_L/C_d	C_L	C_L/C_d
Degrees				
0.0	2.26	4.25	2.52	47.0
0.5	2.33	4.26	2.60	36.3
1.0	2.39	4.25	2.67	29.2
1.5	2.45	4.22	-	-
2.0	2.52	4.20	2.83	20.4
3.0	2.64	4.10	2.90	15.5
4.0	2.77	3.99	3.14	12.2
5.0	-	-	-	-
6.0	3.03	3.70	-	-
7.0	3.11	3.57	-	-
8.0	-	-	3.76	5.97
9.0	3.41	3.25	3.90	5.27
10.0	3.48	3.11	4.05	4.84
12.0	3.77	2.73	4.33	3.91
14.0	4.00	2.48	4.60	3.29
16.0	4.22	2.29	4.84	2.82
18.0	4.41	2.06	5.06	2.44
20.0	4.59	1.87	5.25	2.14

APPENDIX (iv-c) $C_1/C_d - C_1$ PLOT FOR ALL CONFIGURATIONS

